```
お 象代数H 2024.9.19.
Def aH q G if H is a subgroup of G and 2 g Hq SH
                                                         for every geg
                                         or ghach, they
                                         gH = Hg
 Rmk: 1, 2, 3 gare equivalent
2g. SLn(F) \ GLn(F) (b/c det (g'hg) = det(g'). det(h).det(g)
                                         = det(h) = 1 for h ()()()
                                                          96Ln(F)
Def Let N & G, and let G/N := { gN | g ∈ G}
     define \bullet: G_N \times G_N \rightarrow G_N by (g_N) \cdot (g_N) = (g_1g_N)
Prop. Then (G/N, ·) is a group, called factor group or quotient group
           is well-defined (Change the representive element
                                    by gN = ghN for hEN)
          ((g_1N) \cdot (g_2N)) \cdot (g_3N) = (g_1N) \cdot (g_2N) \cdot (g_3N)
           N is the identity for (6/n).
          (gN) s inverse is (g'N)
       GLn(Fp)/SLn(Fp) = P-1, GLn(Fp)/SLn(Fp) Cp-1. for prime p
       for g = GLn(fp) , g = g, h, deth)=1, g=1"1.,), a=det g) =0
       Easily, [a.] a & [Fpx] < GLn(Fp).
```

Question: how to define "essentially the same" V=F3 { (a,0,0) | a ∈ F} { (a, a, o) | b ∈ F }) 1-1 \$ Def. The groups G and H are said to be isomorphic if there exists a bijection $\phi: G \rightarrow H$ s.t. $\phi(g,g_{\iota}) = \phi(g_{\iota}) * \phi(g_{\iota})$ for every g, g, ∈ G, φ is a honomorphism 29.1. G = [(00) | a & Fx}, H = [(bb) | b & Fx} G, H are isomorphic: let $\phi: G \to H$ $\begin{pmatrix} a \\ a \end{pmatrix} \mapsto \begin{pmatrix} a \\ a \end{pmatrix}$ 2. G= {(c) | c = Fp}, H= (Fp+) G. H are isomorphic : let \$:6 -> H (1 c) +> C (b/c (1 c1)(1 c2)=(1 c1+62)) G is homomorphic to H if a mapping $\phi: G \rightarrow H$ s.t. Def. $\phi: g_1g_2 \rightarrow g_1^{\phi}g_2^{\phi} \quad \text{or } \phi(g_1g_2) = \phi(g_1) \phi(g_2)$ eg. (++ G=[9] [a, b= F(50)], H=[90] a= H(50) φ: [a b] D [G o] homomorphism

