

“Bayesian Latent Class Models to evaluate  
diagnostic tests  
in the absence of a gold standard”  
Day 1

Training workshop Zurich  
Sonja Hartmann & Valerie Hungerbühler

# Welcome

- Introduce yourself please
- Add info on country of origin, mr/doct/prof
- Self-assessment

Intro cost action

Wednesday 14 July 2021	Date	Start	End	Speaker(s)	Title
				Lecture Room Y17-M-05	
		9:00	10:15	Sonja Hartnack & Valerie Hungerbühler	Welcome & Introduction
		10:15	11:15	Sonja Hartnack	Brief historical sketch of BLCMs
		11:15	11:45	Coffee break	
		11:45	12:20	Sonja Hartnack & Valerie Hungerbühler	Hands-on Hui-Walter models I
		12:20	12:55	Sonja Hartnack	Hands-on Hui-Walter models II
		12:55	14:00	Lunch Break	
		14:00	14:30	Sonja Hartnack	Conditional dependencies
		14:30	15:00	Sonja Hartnack & Valerie Hungerbühler	Hands-on exercises
		15:00	15:30	Sonja Hartnack & Valerie Hungerbühler	Hands-on exercises
		15:30	16:00	Coffee break	
		16:00	16:30	Sonja Hartnack & HARMONY consortium	Question rounds to core group experts
		16:30	17:00	Sonja Hartnack	MCMC modeling

# House keeping notes

## **Information for Guests**

The University of Zurich provides several options for our guests to connect to the Internet:

### **1. eduroam WLAN**

Most universities and research institutions use eduroam. Members of such institutions have Internet access in the public areas of UZH via the eduroam WLAN network. We recommend testing eduroam access at your home university in advance to ensure that the configuration is correct.

### **2. Internet Access for Guests via UZH WLAN**

As a guest at UZH, you can access the Internet everywhere where there is WLAN access: Simply select the uzh-guest WLAN network. After doing so, accept the Terms of Service and fill in the registration form with your mobile phone number. You will subsequently receive an access code by text message, which allows you to unlock Internet access.

This option is available for all cell phone carriers that allow the receiving of SMS in Switzerland.

# Historical sketch LCM

- 1980 Hui-Walter paradigm

BIOMETRICS 36, 167–171  
March, 1980

## **Estimating the Error Rates of Diagnostic Tests**

**S. L. Hui<sup>1</sup> and S. D. Walter**

# Two tests, one population

Population 1

		T2+	T2-
D+	T1+	$P1 * Se1 * Se2$	$P1 * Se1 * (1 - Se2)$
	T1-	$P1 * (1 - Se1) * Se2$	$P1 * (1 - Se1) * (1 - Se2)$
		T2+	T2-
D-	T1+	$(1 - P1) * (1 - Sp1) * (1 - Sp2)$	$(1 - P1) * (1 - Sp1) * Sp2$
	T1-	$(1 - P1) * Sp1 * (1 - Sp2)$	$(1 - P1) * Sp1 * Sp2$

# Two tests, one population

Population 1

T1+T2+:	$P1*Se1*Se2+(1-P1)*(1-Sp1)*(1-Sp2)$
T1+T2-:	$P1*Se1*(1-Se2)+(1-P1)*(1-Sp1)*Sp2$
T1-T2+:	$P1*(1-Se1)*Se2+(1-P1)*Sp1*(1-Sp2)$
T1-T2-:	$P1*(1-Se1)*(1-Se2)+(1-P1)*Sp1*Sp2$

- 5 parameter and 3 degrees of freedom
  - Non identifiable model



# Two tests, two populations

## Population 1

$$T1+T2+: P1 * Se1 * Se2 + (1-P1) * (1-Sp1) * (1-Sp2)$$

$$T1+T2-: P1 * Se1 * (1-Se2) + (1-P1) * (1-Sp1) * Sp2$$

$$T1-T2+: P1 * (1-Se1) * Se2 + (1-P1) * Sp1 * (1-Sp2)$$

$$T1-T2-: P1 * (1-Se1) * (1-Se2) + (1-P1) * Sp1 * Sp2$$

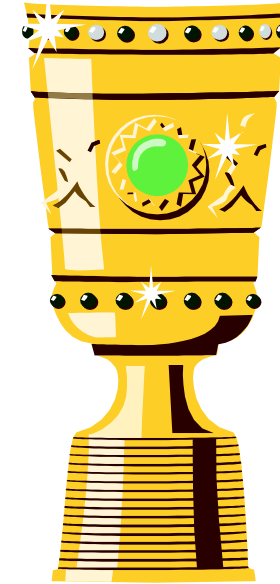
## Population 2

$$T1+T2+: P2 * Se1 * Se2 + (1-P2) * (1-Sp1) * (1-Sp2)$$

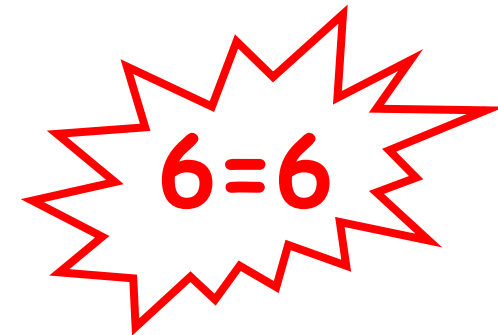
$$T1+T2-: P2 * Se1 * (1-Se2) + (1-P2) * (1-Sp1) * Sp2$$

$$T1-T2+: P2 * (1-Se1) * Se2 + (1-P2) * Sp1 * (1-Sp2)$$

$$T1-T2-: P2 * (1-Se1) * (1-Se2) + (1-P2) * Sp1 * Sp2$$



Identifiable model!



# Hui-Walter Paradigm (1980)

$$S \geq \frac{R}{(2^{R-1} - 1)}$$

S: Populations, R: Tests

## Assumptions

1. The population is divided into two or more populations in which two or more tests are evaluated,
2. sensitivity and specificity are the same in all populations.
3. The tests are conditionally independent given the disease status.

$$P(T_1^+ | T_2^+) = P(T_1^+ | T_2^-)$$

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**TABLE 2.** Maximum Number of Estimable Parameters and Number of Parameters to Be Estimated in the Absence of Conditional Independence and Under Conditional Independence as a Function of the Number of Tests per Subject

<b>Number of Tests</b>	<b>Maximum Number of Estimable Parameters</b>	<b>Parameters to be Estimated Under Conditional Dependence</b>	<b>Parameters to Be Estimated Under Conditional Independence</b>
1	1	3	3
2	3	7	5
3	7	15	7
4	15	31	9
5	31	63	11
h	$2^h - 1$	$2^{h+1} - 1$	$2h + 1$

Berkvens D et al. (2006) Estimating Disease Prevalence in a Bayesian Framework Using Probabilistic Constraints.

doi: 10.1097/01.ede.0000198422.64801.8d

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prior beta distributions

prevalence

$$\pi = P(D)$$

sensitivity

$$\eta_i = P(+|D, T_i)$$

specificity

$$\theta_i = P(-|\bar{D}, T_i)$$

$$\pi \sim \text{Beta}(a_\pi, b_\pi)$$

$$\eta_i \sim \text{Beta}(a_{\eta_i}, b_{\eta_i})$$

$$\theta_i \sim \text{Beta}(a_{\theta_i}, b_{\theta_i})$$

$$\text{Posterior} \propto \text{Likelihood} * \text{Prior}$$

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- 2007 Plummer **Just another Gibbs sampler (JAGS)**

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*OIE Manual of Diagnostic Tests and Vaccines for Terrestrial Animals*  
**endorsed BLCM (2016)**