EDA Lab 2

<u>Simulated Annealing Approach to the Travelling Tournament Problem</u>

Overview:

Travelling Tournament Problem is a well-known problem in sports timetabling that addresses the difficulty in creating a time-table when team travel is the main issue. Simulated annealing is one of the approaches that use a double round-robin and annealing algorithm to get an optimized solution for this problem.

This algorithm consists of the following features:

- 1. TTSA separates the tournament constraints and the pattern constraints into hard and soft constraints and explores both feasible and infeasible schedules.
- 2. TTSA uses a large neighborhood of size O(n3), where n is the number of teams. Some of the moves defining the neighborhood are rather complex and affect the schedule in significant ways. Others can be regarded as a form of ejection chains.
- 3. TTSA includes a strategic oscillation strategy to balance the time spent in the feasible and infeasible regions.
- 4. TTSA incorporates the concept of "reheats" to escape from local minima with very low temperatures.

Functions

To start with, a backtrack search method is used to create an initial random schedule.

Hard Constraint: Should follow a double round-robin method.

Soft Constraint: 1. No more than three consecutive home/away games.

2. A game of Ti at Tj's home cannot be followed by a game of Tj at Ti's home.

There are five different functions performed on this schedule S. The neighborhood of a schedule S is the set of the (possibly infeasible) schedules which can be obtained by applying one of five types of moves.

SwapHomes: (Ti, Tj)
 This function swaps home/away roles of Ti and Tj in the schedule.

2. SwapRounds: (r1, r2)

This function swaps round r1 and r2.

3. SwapTeams: (Ti, Tj):

This function swaps two teams' schedules.

4. PartialSwapRounds:(r1,r2,t)

This function swaps round r1 and r2 for team t.

5. PartialTeamSwap: (t1,t2,r)

This function swaps values of team t1 and t2 for round r.

TTSA uses a reheating method to avoid the local minima of temperature.

The parameters defined to perform this method are maxP, maxC, maxR, temperature T, w, beta b

<u>Outcome</u>

1. Number of Teams = 4

Initial input parameters: Number of Teams: 4 Number of Rounds: 6

maxP: 10 maxR: 10 maxC: 10 w:6000.0

Temperature: 400

Time Required: 29 ms bestFeasible: 8559.0 bestInfeasible: Infinity bestTemperature: 400

```
Initial input parameters:
Number of Teams: 4
Number of Rounds: 6
maxP: 10
maxR: 10
maxC: 10
w:6000.0
Temperature: 400
Initial Schedule:
                 3
                               6
Rounds
        1
            2
Teams
           -3
                -2
        -4
                      4 3
1
2
        3
                 1
            -4
                     -3
        -2
             1
                             -4
3
                 4
                -3
4
        1
            2
Cost of the schedule: 9736
Distance Matrix:
[0, 745, 665, 929]
[745, 0, 80, 337]
[665, 80, 0, 380]
[929, 337, 380, 0]
Rounds
        1 2 3 4 5
                                6
Teams
        4
                 -3
                     2
1
                         3
2
        3
                             -3
3
        -2
                 1
                             2
             4
                     -4
             -3
        -1
                -2
                      3
Time Required: 29 ms
bestFeasible: 8559.0
bestInfeasible: Infinity
bestTemperature: 400
Best feasible schedule
Rounds-> 1
            2
                 3
                      4
                           5
                                6
Teams
                          4
1
        3
            -2
                 -4
                     -3
                 3
2
             1
                 -2
3
             4
                     1
                         2
                             -4
        2
            -3
                 1
                    -2
                         -1
                              3
The Cost for feasible is: 8559
Best infeasible schedule
Rounds-> 1
             2
                  3
                           5
                                6
Teams
                         -3
                            3
        2
1
                 -2
                     4
                     3
2
        -1
                1
                         4
                             -4
             2
3
        -4
                 4
                     -2
                         1
                             -1
        3
            1
                -3
                              2
                     -1
                         -2
The Cost for infeasible is: 15763
```

2. Number of Teams: 6

Initial input parameters:

Number of Teams: 6 Number of Rounds: 10

maxP: 10 maxR: 10 maxC: 10 w:6000.

Temperature: 400

Time Required: 40 ms bestFeasible: 26964.0 bestInfeasible: 27486.0 bestTemperature: 396

```
Initial input parameters:
Number of Teams: 6
Number of Rounds: 10
maxP: 10
maxR: 10
maxC: 10
w:6000.0
Initial Schedule:
Rounds
           1
                 2
                       3
                             4
                                   5
                                         6
                                               7
                                                     8
                                                           9
                                                                 10
Teams
                                          4
5
-6
-1
-2
                 -4
                       -6
                             5
1
                                    -1
-4
3
-6
5
                                                             6
2
3
4
5
6
                                                           -4
5
2
-3
           2
           -6
                1
                      -2
                            6
                                               6
-5
           1
                2
                -3
                                 2
                                          3
                     1
                          -4
                                                     -2
                                                           -1
           4
Cost of the schedule: 28950
Distance Matrix:
[0, 745, 665, 929, 605, 521]
[745, 0, 80, 337, 1090, 315]
[665, 80, 0, 380, 1020, 257]
[929, 337, 380, 0, 1380, 408]
[605, 1090, 1020, 1380, 0, 1010]
[521, 315, 257, 408, 1010, 0]
                 2
                                   5
                                         6
                                               7
                                                     8
Rounds
           1
                       3
                             4
                                                           9
                                                                 10
Teams
                            5
1
                                                            -2
1
-5
6
3
                                -1
5
-6
                            4
2
3
4
5
6
                                                      2
-1
-6
                                      -4
3
                                          5
-4
-2
                 2
                          -2
                     1
                         -1
-3
                                -3
4
               1
3
           2
                    -5
                                                       5
                                                           -4
Time Required: 40 ms
26964.0 27486.0 396
best feasible table
Rounds-> 1
                 2
                             4
                                   5
                                         6
                                               7
                                                     8
                                                           9
                                                                 10
Teams
                -6
                                                  3
                                                       5
           2
                      -5
                            6
                                 4
                                      -3
                                            -2
                                                           -4
1
2
3
4
                     3
-2
                                       6
                                                 -6
                 -4
                            4
                 5
                                                        2
           3
                    -6
                                                        6
                          -2
                                 -1
                                       5
                                            -3
                                                             1
                2
5
                -3
                                                            -2
           6
                     1
                          3
                                           -6
                               2
                                                4
                                                     -1
                                 3
                 1
                     4
           -5
                          -1
                                      -2
The Cost for feasible is: 26964
best infeasible table
                 2
                                   5
                                         6
                                               7
                                                     8
                                                           9
Rounds-> 1
                       3
                                                                  10
Teams
                                      3
5
-1
                       -6
                                  2
                                                -5
                 -3
                             6
                                                      -2
                                                             5
1
2
3
4
           -4
                -5
                                                 6
                                                           -6
           3
                                 -1
                                                       1
                      4
                     5
           -2
                                 6
                                           2
                 1
                          -5
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               6
2
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                                                             3
           1
                                           -1
5
                                     -2
4
                     -3
                           3
                                 4
                                           6
           -6
                                                      -4
                                                            -1
           5
                -4
                     1
                          -1
The Cost for infeasible is: 40206
```

3. Number of Teams: 10

Initial input parameters: Number of Teams: 10 Number of Rounds: 18

maxP: 10 maxR: 10 maxC: 10 w:6000.0

Temperature: 400

Time Required: 331 ms bestFeasible: 66932.0

bestInfeasible: 67098.25546619005

bestTemperature: 760

```
Initial input parameters:
Number of Teams: 10
Number of Rounds: 18
maxR: 10
maxR: 10
maxR: 10
w 16000.0
Temperature: 400

Initial Schedule:
Rounds 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18

Teams
1 6 -9 3 10 7 -3 -5 -7 -10 -8 -2 8 -4 9 5 2 -6 4
2 -7 4 6 3 -8 -4 9 5 -9 -6 1 -5 -10 8 -3 -1 7 10
3 -4 8 -1 -2 -9 1 -10 9 7 -5 -7 4 5 6 2 -8 10 -6
4 3 -2 -5 6 -10 2 8 10 -6 -7 -9 -3 1 7 -8 5 9 -1
5 9 7 4 -7 -6 -10 1 -2 -8 3 6 2 -3 10 1 -4 8 -9
6 -1 10 -2 -4 5 5 -8 -7 8 4 2 -5 -9 7 -3 9 -10 1 3
7 2 -5 8 5 -1 9 6 1 -3 4 3 10 -6 -4 -10 -9 -2 -8
8 -10 -3 -7 -9 2 6 -4 -6 5 1 10 -1 9 -2 4 3 -5 7
9 -5 1 -10 8 3 -7 -2 -3 2 10 4 6 -8 -1 -6 7 -4 5

Distance Matrix:
[0, 745, 665, 929, 685, 521, 370, 587, 467, 670]
[745, 0, 80, 337, 1090, 315, 567, 712, 871, 741]
[665, 80, 0, 300, 1020, 257, 501, 664, 806, 697]
[929, 337, 380, 0, 1380, 0, 1380, 622, 646, 878, 732]
[605, 180, 120, 1380, 0, 110, 957, 119, 1100, 1060, 1270]
[521, 315, 257, 408, 1010, 0, 253, 410, 557, 451]
[370, 567, 501, 662, 957, 253, 0, 250, 311, 325]
[587, 712, 664, 646, 1190, 410, 250, 0, 260, 86]
[467, 871, 808, 878, 1060, 557, 311, 260, 0, 328]
[670, 741, 607, 732, 1270, 451, 325, 86, 328, 0]
```

```
Time Required: 331 ms
bestFeasible: 66932.0
bestInfeasible: 67098.25546619005
bestTemperature: 760
 Best infeasible schedule Rounds-> 1 2 3 4
                                                                                                                             11
                                                                                                                                         12
                                                                                                                                                                                                                    18
 10 -2 6 5 9 -4 -3 4 -7
The Cost for infeasible is : 67268.55571478521
 Best feasible schedule
Rounds-> 1 2 3
                                                                                            8
                                                                                                      9
                                                                                                                 10
                                                                                                                             11
                                                                                                                                         12
                                                                                                                                                      13
                                                                                                                                                                  14
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                                                                                                                                                                                                                    18
 Teams
6 -4 8 -9 2 9 -5

7 8 5 3 -8 2 1 -

8 -7 -6 -4 7 1 -9

9 2 -1 6 -10 -6 8

10 -5 2 5 9 -4 -3

The Cost for feasible is: 66932.0
```

4. Number of Teams: 12

Initial input parameters: Number of Teams: 12 Number of Rounds: 22

maxP: 10 maxR: 10 maxC: 10 w:6000.0

Temperature: 400

Time Required: 660 ms bestFeasible: 133138.0

bestInfeasible: 130916.12777334794

bestTemperature: 1497

```
Time Required: 660 ms
bestFeasible: 133138.0
bestInfeasible: 130916.12777334794
bestTemperature: 1497
Hest infeasible schedule
Rounds-> 1 2 3 4 5 6
Teams
Teams 2 3 4 5 6 7 8 1 2 -4 -1 8 6 5 -10 7 9 11 3 9 -8 -10 8 12 5 -1 7 -1 4 2 -11 -5 -1 6 1 11 -10 5 -11 -12 4 12 -2 -3 -10 1 6 1 7 9 -2 -4 12 8 11 -7 7 -8 -6 -12 9 1 11 -2 -3 8 7 3 -2 -3 10 -9 -6 12 -1 10 -12 -9 3 11 -8 2 5 4 -5 11 5 4 -1 -10 9 -7 -4 -6 -1 10 5 7 -5 -3 -6 9 -8 3 The Cost for infeasible is: 131054.1262821146 Hounds 1 2 3 4 5 6 7 8 12 -7 -9 -12 Teams 1 -7 -9 -13
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9 -11
-12 -8
11 -6
1 -7 10
1 8 9
10 3 -
4 12
2 -10
-1 -5
-4 8
7 6
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-12 9
-9 -12
4 11
-3 -7
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8 -10
10 4
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6 -3 1
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-3
-8
-2
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-4
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-12
11
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12
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7
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8
-4
-6
-10
9
-3
-2
                                                                                                                                                              1 4 10 8 -7 11 2 -6
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11
12
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-7
6
-10
-5
8
-2
-3
2
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12
The
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-10
-11
5
12
9 6
8 7
                                                                                                                                                                             9
-12
-7
11
-10
8
                                                                                                                                                                                                -1
11
10
-9
-8
                                                                                                                                                                                                                                                                                                                     2 - 4 - 3 - 12 1 10
                                                                                                                                                 -3
1
6
-2
5
-4
                                                                                                                                                                     -6
-9
3
```

5. n= 14

Initial input parameters: Number of Teams: 14 Number of Rounds: 26

maxP: 10 maxR: 10 maxC: 10 w:6000.0

Cost of the schedule: 149709

Time Required: 302 ms bestFeasible: 252564.0 bestInfeasible: 30455.9466 Best Temperature: 798

```
Distance Matrix:

[0, 745, 665, 929, 605, 521, 370, 587, 467, 670, 700, 1210, 2130, 1890]

[745, 0, 80, 337, 1090, 315, 567, 712, 871, 741, 1420, 1630, 2560, 2430]

[665, 80, 0, 380, 1020, 257, 501, 664, 808, 697, 1340, 1570, 2520, 2370]

[929, 337, 380, 0, 1380, 408, 622, 646, 878, 732, 1520, 1530, 2430, 2360]

[605, 1090, 1020, 1380, 0, 1010, 957, 1190, 1060, 1270, 966, 1720, 2590, 2270]

[521, 315, 257, 408, 1010, 0, 253, 410, 557, 451, 1140, 1320, 2260, 2110]

[370, 567, 501, 622, 957, 253, 0, 250, 311, 325, 897, 1090, 2040, 1870]

[587, 712, 664, 646, 1190, 410, 250, 0, 260, 86, 939, 916, 1850, 1730]

[467, 871, 808, 878, 1060, 557, 311, 260, 0, 328, 679, 794, 1740, 1560]

[670, 741, 697, 732, 1270, 451, 325, 86, 328, 0, 1005, 905, 1846, 1731]

[700, 1420, 1340, 1520, 966, 1140, 897, 939, 679, 1005, 0, 878, 1640, 1300]

[1210, 1630, 1570, 1530, 1720, 1320, 1090, 916, 794, 905, 878, 0, 947, 832]

[2130, 2560, 2520, 2430, 2590, 2260, 2040, 1850, 1740, 1846, 1640, 947, 0, 458]

[1890, 2430, 2370, 2360, 2270, 2110, 1870, 1730, 1560, 1731, 1300, 832, 458, 0]
```

```
Time Required: 3291 ms
bestFeasible: 264950.0
bestInfeasible: 364950.0
```

Problems Faced

- 1. With an increasing number of teams, my solution was taking forever to converge. So I modified my backtracking function and included soft constraints while creating the first random schedule.
- 2. Making the above modification sometimes gave me a best infeasible value of zero/infinity.
- 3. The new algorithm for creating the first schedule is not very optimized. So, it still takes more time to converge for values above 10.

Run-time and Quality of Results Trade-offs

- 1. By varying parameters, affects the algorithm converging time. Increasing the value of maxP, maxC, maxR and Temperature increases the time as per obtained observations.
- 2. For values (number of teams) greater than 10, increasing w and making beta parameters 0.998 helped the program to converge faster.
- 3. Following is the observation table of various outcomes taken by changing given parameters:

				Best Feasible as per	Initial	Final	
n	maxC	maxP	maxR	the CMU website	Feasible	Feasible	Time(ms)
	10	10	10		9736	<mark>8559</mark>	29
	100	10	10		9107	5708	221
4	10	100	10	8276	10095	5708	97
	10	10	10		28950	26964	40
	100	10	10		29853	<mark>2166</mark> 3	540
					25522.55		
6	10	100	10	22969	9	22012	280
	10	10	10		89101	67268	331
					85623.36		
10	100	10	10	56506	9	<mark>66107</mark>	1777
	10	10	10		155404	133138	634
					167038.9		
12	100	10	10	107483	325	<mark>132257</mark>	4651
14	10	10	10	182797	305217.8	264950	1885

			501		
			296233.1		
100	10	10	108	<mark>257200</mark>	5989

The highlighted cells in the table show optimized feasible output for a given number of teams.

4. \The graph below shows the relation between number of teams and average time required to get the final schedule.

Time vs. Number of Teams

