

**Deterministic Select** (vector  $\mathbf{A}$  of size  $n$ , integer  $k \leq n$ )

- 1: **if**  $n == 5$  **then**
- 2:     Sort  $\mathbf{A}$  and return the element in  $k$ -th position.
- 3: **end if**
- 4: Partition  $\mathbf{A}$  into vectors  $\{\mathbf{B}_i\}_{i=0}^{(n/5)-1}$ , where each vector  $\mathbf{B}_i$  has 5 elements.
- 5: **for**  $0 \leq i < n/5$  **do**
- 6:      $\mathbf{C}[i] = \text{Deterministic Select}(\mathbf{B}_i, 3)$
- 7: **end for**  
    { /\*  $\mathbf{C}$  is a  $(n/5)$ -long vector, where the  $i$ -th entry is the median of  $\mathbf{B}_i$  \*/.}
- 8: (*median-of-medians*)  $p = \text{Deterministic Select}(\mathbf{C}, (n/10))$
- 9: Partition  $\mathbf{A}$  into three sub-vectors  $\mathbf{A}_{<p}$ ,  $\mathbf{A}_{=p}$ , and  $\mathbf{A}_{>p}$ .  
    { /\*  $\mathbf{A}_{<p}$  has all elements of  $\mathbf{A}$  that are less than  $p$ . \*/ }  
    { /\*  $\mathbf{A}_{=p}$  has all elements of  $\mathbf{A}$  that are equal to  $p$ . \*/ }  
    { /\*  $\mathbf{A}_{>p}$  has all elements of  $\mathbf{A}$  that are greater than  $p$ . \*/ }
- 10: **if**  $k \leq \text{length}(\mathbf{A}_{<p})$  **then**
- 11:     **return**  $\text{Deterministic Select}(\mathbf{A}_{<p}, k)$
- 12: **else**
- 13:     **if**  $k > \text{length}(\mathbf{A}_{<p}) + \text{length}(\mathbf{A}_{=p})$  **then**
- 14:         **return**  $\text{Deterministic Select}(\mathbf{A}_{>p}, k - \text{length}(\mathbf{A}_{<p}) - \text{length}(\mathbf{A}_{=p}))$
- 15:     **end if**
- 16: **else**
- 17:     **return**  $p$
- 18: **end if**