

DOCUMENTATION FOR ARTIFIAL INTELLIGENCE
ASSIGNMENT-2

Question-1 Hill climbing informed searching algorithm.

INPUT-

Start state- 2 8 3
 1 6 4
 7 0 5

Goal state- 1 2 3
 8 0 4
 7 6 5

OUTPUT-

2 8 3
1 6 4
7 0 5
Node: 0
Depth: 0
Moves: []

1.sum of Manhattan distance of each tile from the goal position
2.number of tiles displaced from their destined position

1
[18]
2 8 3
1 0 4
7 6 5
Node: 1
Depth: 1
Moves: ['up']

2 8 3
1 6 4
0 7 5
Node: 2
Depth: 1
Moves: ['left']

2 8 3
1 6 4
7 5 0
Node: 3
Depth: 1
Moves: ['right']

[16, 16, 20]
2 0 3
1 8 4
7 6 5
Node: 4
Depth: 2
Moves: ['up', 'up']

```
-----  
2 8 3  
0 1 4  
7 6 5  
Node: 5  
Depth: 2  
Moves: ['up', 'left']  
-----
```

```
2 8 3  
1 4 0  
7 6 5  
Node: 6  
Depth: 2  
Moves: ['up', 'right']  
-----
```

```
[14, 14, 16]  
0 2 3  
1 8 4  
7 6 5  
Node: 7  
Depth: 3  
Moves: ['up', 'up', 'left']  
-----
```

```
2 3 0  
1 8 4  
7 6 5  
Node: 8  
Depth: 3  
Moves: ['up', 'up', 'right']  
-----
```

```
[12, 14]  
1 2 3  
0 8 4  
7 6 5  
Node: 9  
Depth: 4  
Moves: ['up', 'up', 'left', 'down']  
-----
```

```
[12]  
1 2 3  
7 8 4  
0 6 5  
Node: 10  
Depth: 5  
Moves: ['up', 'up', 'left', 'down', 'down']  
-----
```

```
1 2 3  
8 0 4  
7 6 5  
Node: 11  
Depth: 5  
Moves: ['up', 'up', 'left', 'down', 'right']  
-----
```

```
Success  
Time: 0.014479875564575195  
-----
```

HILL CLIMBING -

Hill climbing is a inform search algorithm and it based on Greedy Local Search.

- > Local search: use single current state and move to neighboring states.
- > Are also useful for pure optimization problems. Find best state according to

- some objective function.
- > State space landscape.
 - Location (defined by state).
- > Elevation.
 - Defined by the value of the heuristic function or objective function.
- > Elevation corresponds to cost.
 - Global minimum (aim is to find the lowest valley).
- > Elevation corresponds to an objective function.
 - Global maximum (aim is to find the highest peak).
- > Complete algorithm always finds a goal if one exists.
- > Optimal algorithm always finds global minimum/maximum.

HILL CLIMBING SEARCH

- > "is a loop that continuously moves in the direction of increasing value".
- > It terminates when a peak is reached.
- > No neighbor has higher value.
- > does not maintain any search tree.
- > Current node data structure records state and objective function value.
- > does not look ahead beyond the immediate neighbors of the current state.
- > chooses randomly among the set of best successors, if there is more than one.
- > Hill-climbing a.k.a. greedy local search.
- > Grabs a good neighbor state without thinking ahead about where to go next.
- > Makes very rapid progress towards a solution.
- > Quite easy to improve a bad state.
- > Some problem spaces are great for hill climbing and others are terrible.

ALGORITHM

```

function HILL-CLIMBING(problem) return a state that is a
    (global) maximum
    input: problem, a problem
    local variables: current, a node.
                     neighbor, a node.
    Current <-- MAKE-NODE(INITIAL-STATE[problem])
    loop do
        neighbor <-- a highest valued successor of current
        if VALUE[neighbor] ≤ VALUE[current] then return
        STATE[current]
        current <-- neighbor
  
```

ADVANTAGE

1. Uses very little memory.
2. Finds often reasonable solutions in large or infinite state spaces.

DRAWBACKS

1. Local Maxima
 - (A) peaks that aren't the highest point in the space (below global maxima).

- (B) higher than each of its neighboring states.
- 2. Plateau: region where evaluation function is flat.
 - (A) Flat local maximum: no uphill exit exists.
 - (B) Shoulder: possible to make progress.
 - (C) Could give the search algorithm no direction (random walk) for local maximum.
- 3. Ridges:
 - (A) flat like a plateau, but with drop-offs to the sides; steps to the North, East, South and West may go down, but a combination of two steps (e.g. N, W) may go up.
 - (B) results in a sequence of local maximum not connected to each other.

Question-2 Simulated Annealing informed search.

INPUT-

Start state- 2 8 3
 1 6 4
 7 0 5

Goal state- 1 2 3
 8 0 4
 7 6 5

OUTPUT-

Started running simulated annealing:

goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[2, 8, 3, 1, 6, 4, 7, 0, 5]

Choosing random movement:E
state after move:[2, 8, 3, 1, 6, 4, 7, 5, 0]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[2, 8, 3, 1, 6, 4, 7, 5, 0]

Choosing random movement:W
state after move:[2, 8, 3, 1, 6, 4, 7, 0, 5]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[2, 8, 3, 1, 6, 4, 7, 0, 5]

Choosing random movement:N
state after move:[2, 8, 3, 1, 0, 4, 7, 6, 5]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[2, 8, 3, 1, 0, 4, 7, 6, 5]

Choosing random movement:S
state after move:[2, 8, 3, 1, 6, 4, 7, 0, 5]

goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[2, 8, 3, 1, 6, 4, 7, 0, 5]

Choosing random movement:N
state after move:[2, 8, 3, 1, 0, 4, 7, 6, 5]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[2, 8, 3, 1, 0, 4, 7, 6, 5]

Choosing random movement:S
state after move:[2, 8, 3, 1, 6, 4, 7, 0, 5]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[2, 8, 3, 1, 6, 4, 7, 0, 5]

Choosing random movement:W
state after move:[2, 8, 3, 1, 6, 4, 0, 7, 5]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[2, 8, 3, 1, 6, 4, 0, 7, 5]

Choosing random movement:E
state after move:[2, 8, 3, 1, 6, 4, 7, 0, 5]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[2, 8, 3, 1, 6, 4, 7, 0, 5]

Choosing random movement:W
state after move:[2, 8, 3, 1, 6, 4, 0, 7, 5]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[2, 8, 3, 1, 6, 4, 0, 7, 5]

Choosing random movement:N
state after move:[2, 8, 3, 0, 6, 4, 1, 7, 5]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[2, 8, 3, 0, 6, 4, 1, 7, 5]

Choosing random movement:N
state after move:[0, 8, 3, 2, 6, 4, 1, 7, 5]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[0, 8, 3, 2, 6, 4, 1, 7, 5]

Choosing random movement:E
state after move:[8, 0, 3, 2, 6, 4, 1, 7, 5]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[8, 0, 3, 2, 6, 4, 1, 7, 5]

Choosing random movement:W

state after move:[0, 8, 3, 2, 6, 4, 1, 7, 5]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[0, 8, 3, 2, 6, 4, 1, 7, 5]

Choosing random movement:E
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goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
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Choosing random movement:E
state after move:[8, 3, 0, 2, 6, 4, 1, 7, 5]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[8, 3, 0, 2, 6, 4, 1, 7, 5]

Choosing random movement:S
state after move:[8, 3, 4, 2, 6, 0, 1, 7, 5]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[8, 3, 4, 2, 6, 0, 1, 7, 5]

Choosing random movement:N
state after move:[8, 3, 0, 2, 6, 4, 1, 7, 5]
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state:[8, 3, 0, 2, 6, 4, 1, 7, 5]

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state after move:[8, 0, 3, 2, 6, 4, 1, 7, 5]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
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goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
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goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[0, 8, 3, 2, 6, 4, 1, 7, 5]

Choosing random movement:E
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goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[8, 0, 3, 2, 6, 4, 1, 7, 5]

Choosing random movement:S
state after move:[8, 6, 3, 2, 0, 4, 1, 7, 5]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
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state after move:[8, 6, 3, 2, 7, 4, 1, 0, 5]
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state after move:[8, 6, 3, 2, 7, 4, 0, 1, 5]
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state after move:[8, 6, 3, 2, 7, 4, 1, 0, 5]
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Choosing random movement:E
state after move:[8, 6, 3, 2, 7, 4, 1, 5, 0]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[8, 6, 3, 2, 7, 4, 1, 5, 0]

Choosing random movement:N
state after move:[8, 6, 3, 2, 7, 0, 1, 5, 4]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[8, 6, 3, 2, 7, 0, 1, 5, 4]

Choosing random movement:N
state after move:[8, 6, 0, 2, 7, 3, 1, 5, 4]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[8, 6, 0, 2, 7, 3, 1, 5, 4]

Choosing random movement:W
state after move:[8, 0, 6, 2, 7, 3, 1, 5, 4]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[8, 0, 6, 2, 7, 3, 1, 5, 4]

Choosing random movement:S
state after move:[8, 7, 6, 2, 0, 3, 1, 5, 4]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[8, 7, 6, 2, 0, 3, 1, 5, 4]

Choosing random movement:N
state after move:[8, 0, 6, 2, 7, 3, 1, 5, 4]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[8, 0, 6, 2, 7, 3, 1, 5, 4]

Choosing random movement:E
state after move:[8, 6, 0, 2, 7, 3, 1, 5, 4]
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state:[8, 6, 0, 2, 7, 3, 1, 5, 4]

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state after move:[8, 6, 3, 2, 7, 0, 1, 5, 4]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
state:[8, 6, 3, 2, 7, 0, 1, 5, 4]

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state:[8, 6, 3, 0, 2, 7, 1, 5, 4]

Choosing random movement:S
state after move:[8, 6, 3, 1, 2, 7, 0, 5, 4]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
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goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
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goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
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Choosing random movement:N
state after move:[8, 6, 0, 2, 7, 3, 1, 5, 4]
goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
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Choosing random movement:S
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goal:[1, 2, 3, 8, 0, 4, 7, 6, 5]
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 state:[8, 6, 3, 2, 7, 4, 1, 0, 5]

Simulated Annealing-

- > Hill climbing that does not make downhill move is incomplete.
- > Pure random walk: choosing successor from a list is complete but inefficient.
- > Solution: hill climbing + random walk =simulated annealing to ensure both efficiency and completeness.

Use a more complex Evaluation Function:

- > Do sometimes accept candidates with higher cost to escape from local optimum.
 - Idea: but gradually decrease their size and frequency.
- > Adapt the parameters of this evaluation function during execution.
- > Based upon the analogy with the simulation of the annealing of solids.

Others Names-

1. Monte Carlo Annealing
2. Statistical Cooling
3. Probabilistic Hill Climbing
4. Stochastic Relaxation
5. Probabilistic Exchange Algorithm

Analogy-

- >Slowly cool down a heated solid, so that all particles arrange in the ground energy state.
- > At each temperature wait until the solid reaches its thermal equilibrium.
- > Probability of being in a state with energy E :

$$Pr \{ E = E \} = 1/Z(T) \cdot \exp (-E / k B .T)$$

E Energy
 T Temperature
 kB Boltzmann constant
 $Z(T)$ Normalization factor (temperature dependent)

- At a fixed temperature T :

- Perturb (randomly) the current state to a new state
- ΔE is the difference in energy between new and current state.
- If $\Delta E < 0$ (new state is lower), accept new state as current state.
- If $\Delta E \geq 0$, accept new state with probability
 $Pr (accepted) = \exp (- \Delta E / k B .T).$
- Eventually the systems evolves into thermal equilibrium

- at temperature T .
- When equilibrium is reached, temperature T can be lowered and the process can be repeated.

Difference between Hill Climbing and Simulated Annealing

- > Unlike hill climbing, it does not always pick the best move.
- > SA picks the move randomly.
- > If situation improves then accept the move.
- > Otherwise, accept the move with some probability.
- > Probability decreases as the temperature goes down.
- > Probability decreases exponentially with the badness of the move.
- > Bad moves are more likely to be allowed at the start when temperature is high, and they are unlikely when temperature decreases.