

Ques 1:

Minimum Spanning Tree (M.S.T) is a non-cyclic part of a graph this has can have V (vertices of graph) node and $E-1$ edges (E is edges in graph). It is designed in a way is traversal in it is minimum.

Application

- (1) It provide us various way we can move from one node to another - efficiently.
- (2) It can be used in ~~network~~ circuit creation and Network - designing.

Ques 2:

Prim's Algorithm = $O(V^2)$ when used adjacency matrix

If we use adjacency list complexity can be reduced to $O(E \log V)$.

Space complexity: $O(V+E)$.

Kruskal algorithm: Time Complexity = $O(E \log V)$.

Space Complexity = $O(\log E)$.

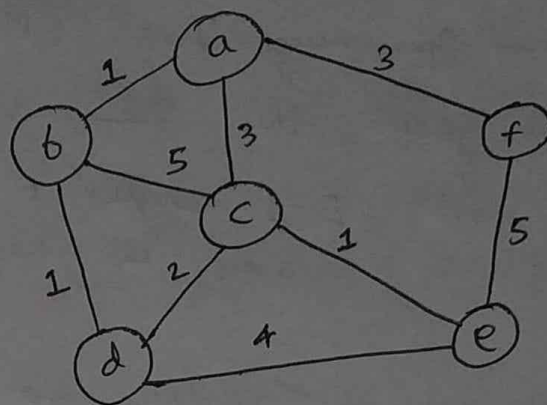
Dijkstra algorithm: Time complexity = $(E+V) \log V$.

Space Complexity = $O(V^2)$.

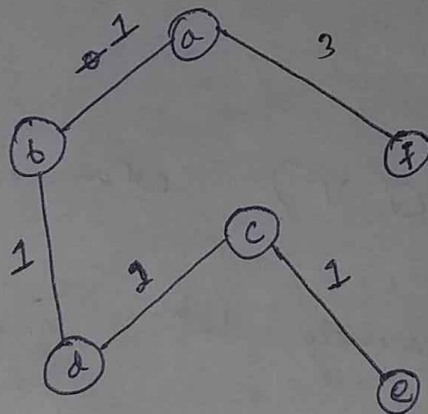
Bellman - Ford algorithm: Time Complexity = $O(V \cdot E)$.

Space - Complexity = $O(NE)$.

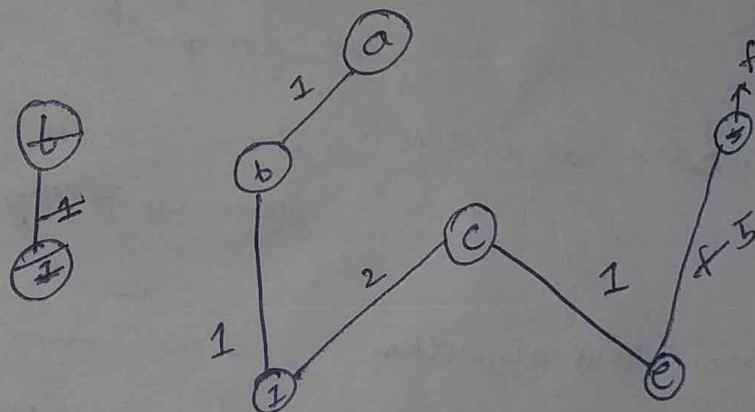
Q3



Kruskal algorithm



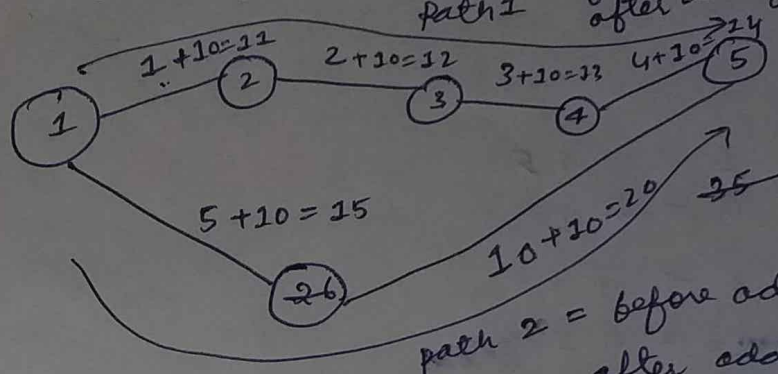
Prim algorithm



Q4:

(5)

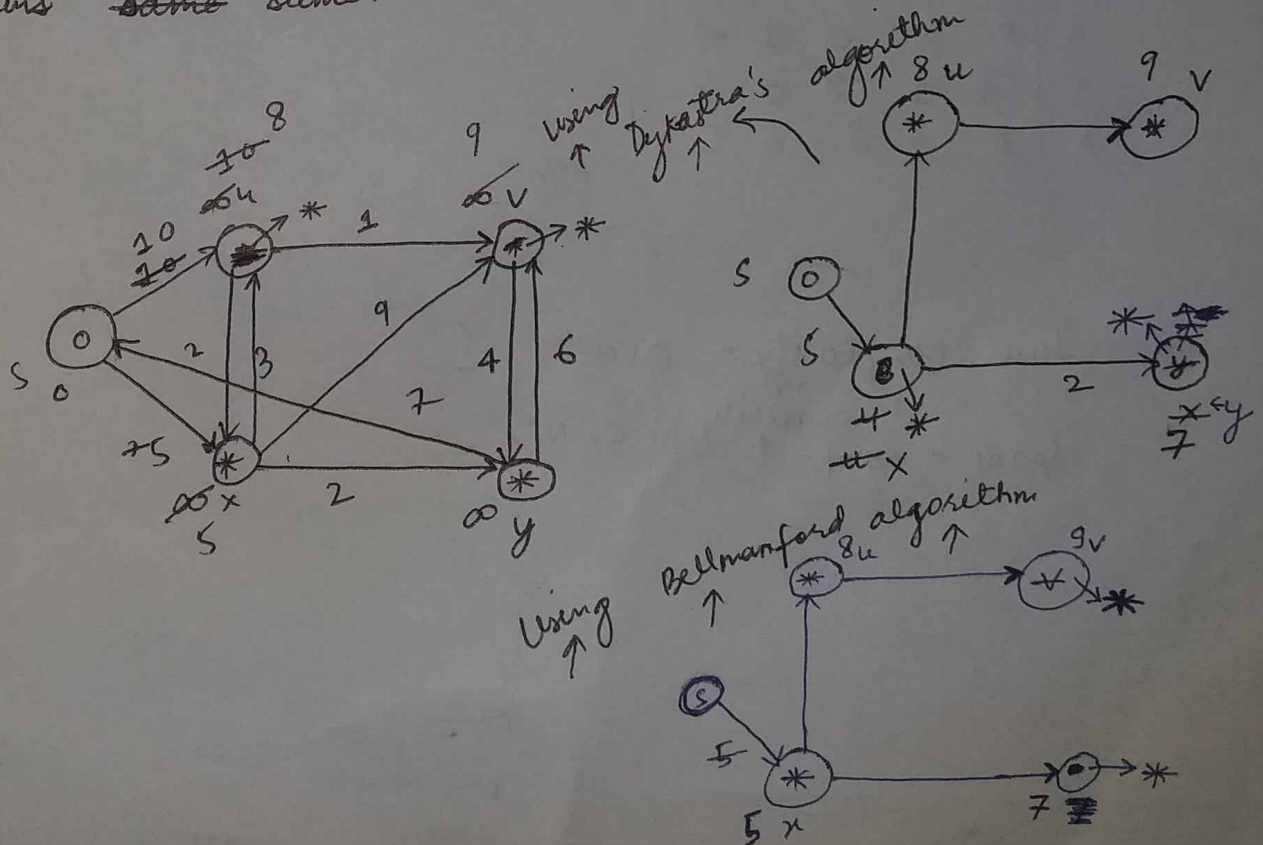
(a) Shortest path will change in the ~~same~~ case when every pair is added with 10 as for example in graph given below



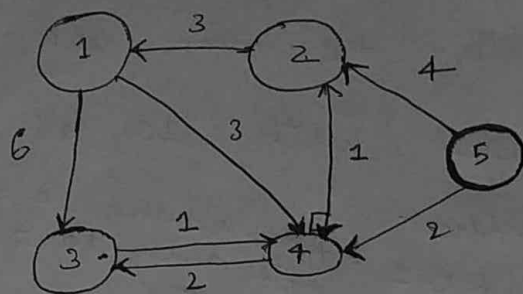
Previously, the shortest path was path 1 after adding 10 path is path 2.

(b) When each weight in graph is multiplied by 10 the shortest path remains same.

Q5:



Q6



$A =$

	1	2	3	4	5
1	0	∞	6 3	∞	∞
2	3	0	∞	∞	∞
3	6 ∞	∞	0	1	∞
4	∞	1	2	0	∞
5	∞	4	∞	2	0

$A^1 =$

	1	2	3	4	5
1	0	4	5	3	∞
2	3	0	7	6	∞
3	5	2	0	1	∞
4	5 4	1	2	0	∞
5	6	3	3	2	0

Ans →

Time-complexity = $O(N^3)$

Space-complexity = $O(N^2)$