

## Model Description

The model consists of the state of the vehicle. The state is comprised of the following:

- X position (x)
- Y position (y)
- Orientation (psi)
- Velocity (v)
- Cross track error (cte)
- Orientation error (epsi)

The actuator controls are modeled using the following two parameters

- Steering angle (del)
- Acceleration (a) -> Braking is modeled using negative values of acceleration.

Given the state at any time (t), the state at time (t+1) can be calculated using the equations

- $x_{t+1} = x_t + v_t * \cos(\psi_t) * dt$
- $y_{t+1} = y_t + v_t * \sin(\psi_t) * dt$
- $\psi_{t+1} = \psi_t + v_t / L_f * \delta_t * dt$
- $v_{t+1} = v_t + a_t * dt$
- $cte_{t+1} = cte_t + v_t * \sin(\epsilon_t) * dt$  //  $cte_t = f(x) - y$
- $\epsilon_{t+1} = \epsilon_t + v_t / L_f * \delta_t * dt$

## Time Step length and elapsed duration

A default value of  $N = 25$  and  $dt = 0.05$  was initially chosen. The selected value led to large run times. The  $dt$  was increased to 0.1 and no degradation on accuracy was observed. The run time was still high and as such the value of  $N$  was subsequently decreased from 25 to 15 and then to 10. At  $N = 10$  and  $dt=0.1$ , the project goals were met with fast execution speed.

## MPC Preprocessing

The preprocessing includes converting from the map's coordinate system to the car's coordinate system using the equations below

- $ptsx_v[i] = (ptsx[i] - px) * \cos(\psi) + (psy[i] - py) * \sin(\psi)$ ; //  $px \rightarrow$  x position of car,  $py \rightarrow$  y position of car,  $\psi \rightarrow$  orientation of car

- $\text{ptsy\_v}[i] = (\text{ptsy}[i] - \text{py}) * \cos(\text{psi}) - (\text{ptsx}[i] - \text{px}) * \sin(\text{psi});$

## Handling Latency

Latency is handled by adding a state prediction using a time step of 100 ms.

The vehicle models are used to update the state before invoking `MPC.Solve()`. The equations below are used.

- $\text{px} = \text{px} + \text{v} * \cos(\text{psi}) * \text{latency\_in\_sec};$
- $\text{py} = \text{py} + \text{v} * \sin(\text{psi}) * \text{latency\_in\_sec};$
- $\text{psi} = \text{psi} - \text{v} * \text{delta/Lf} * \text{latency\_in\_sec};$
- $\text{v} = \text{v} + \text{acc} * \text{latency\_in\_sec};$