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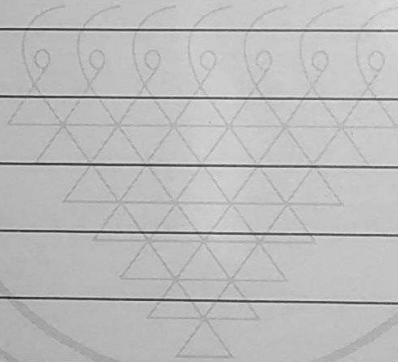
Class :- B.E IT

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॥ ज्ञानदीपेन भास्वताः ॥



Consider following instance of 8 puzzle problem

8 7 6  
2 1 5  
3 4 -

8 7  
2 1 6  
3 4 5

initial

final configuration

Consider heuristic function defined below

- $h_1$ : Misplaced tiles count excepts space
- $h_2$ : Correctly placed tiles count except space
- $h_3$ : Sum of Manhattan distance between current and correct position of all tiles except space

Answer the following question

- a) In 8 puzzle problem we are concerned with getting to goal configuration within least number of step. All moves are thus equally costly. Define  $g(n)$  in your own words. What will be the cost of 6 Step Solution to some arbitrary 8 puzzle instance?

→ The lowest path cost  $g(n)$  can be the cost to reach the goal configuration in least steps.



In our case, we can reach the final configuration in atleast 4 moves. OP, UP LEFT, LEFT.

Since all the moves are equally costly we compute  $g(n)$  as.

$$g(n) = 1 + 1 + 1 + 1 + 1$$

$$g(n) = 4$$

Consider the following arbitrary 8-puzzle instance which gives solution in 6 steps:

$$\begin{array}{ccc} 8 & 7 & 6 \\ 2 & 1 & 5 \\ - & 3 & 4 \end{array}$$

The solution can be represented as :

$$\begin{aligned} & \{ \{8, 7, 6\}, \{2, 1, 5\}, \{-, 3, -\} \} \rightarrow \{ \{8, 7, 6\}, \{2, 1, 5\}, \{3, -, -\} \} \rightarrow \\ & \{ \{8, 7, 6\}, \{2, 1, 5\}, \{3, 4, -\} \} \rightarrow \{ \{8, 7, 6\}, \{2, 1, -\}, \{3, 4, 5\} \} \rightarrow \\ & \{ \{8, 7, -\}, \{2, 1, 6\}, \{3, 4, 5\} \} \rightarrow \{ \{8, -, 7\}, \{2, 1, 6\}, \{3, 4, 5\} \} \rightarrow \\ & \{ \{-, 8, 7\}, \{2, 1, 6\}, \{3, 4, 5\} \} \end{aligned}$$

Since all the moves are equally costly, the cost would be

$$g(n) = 6$$

Draw exhaustive state space tree of depth limited to 4 for instance of 8 puzzle

problem in question

Q Compute  $h_i(n)$  where  $i = 1, 2, 3$  and  $n$   
= initial state final state from question

for  $i = 1$ ,  $n = \text{initial state}$

$h_1(\text{initial}) = \text{misplaced tiles count except space}$

$$h_1(\text{initial}) = 4$$

$n = \text{goal state}$

$$h_1(\text{goal}) = 0$$

for  $i = 2$ ,  $n = \text{initial state}$

$h_2(\text{initial}) = \text{correctly placed tiles except space}$

$$h_2(\text{initial}) = 4$$

for  $n = \text{goal state}$

$$h_2(\text{goal}) = 8$$

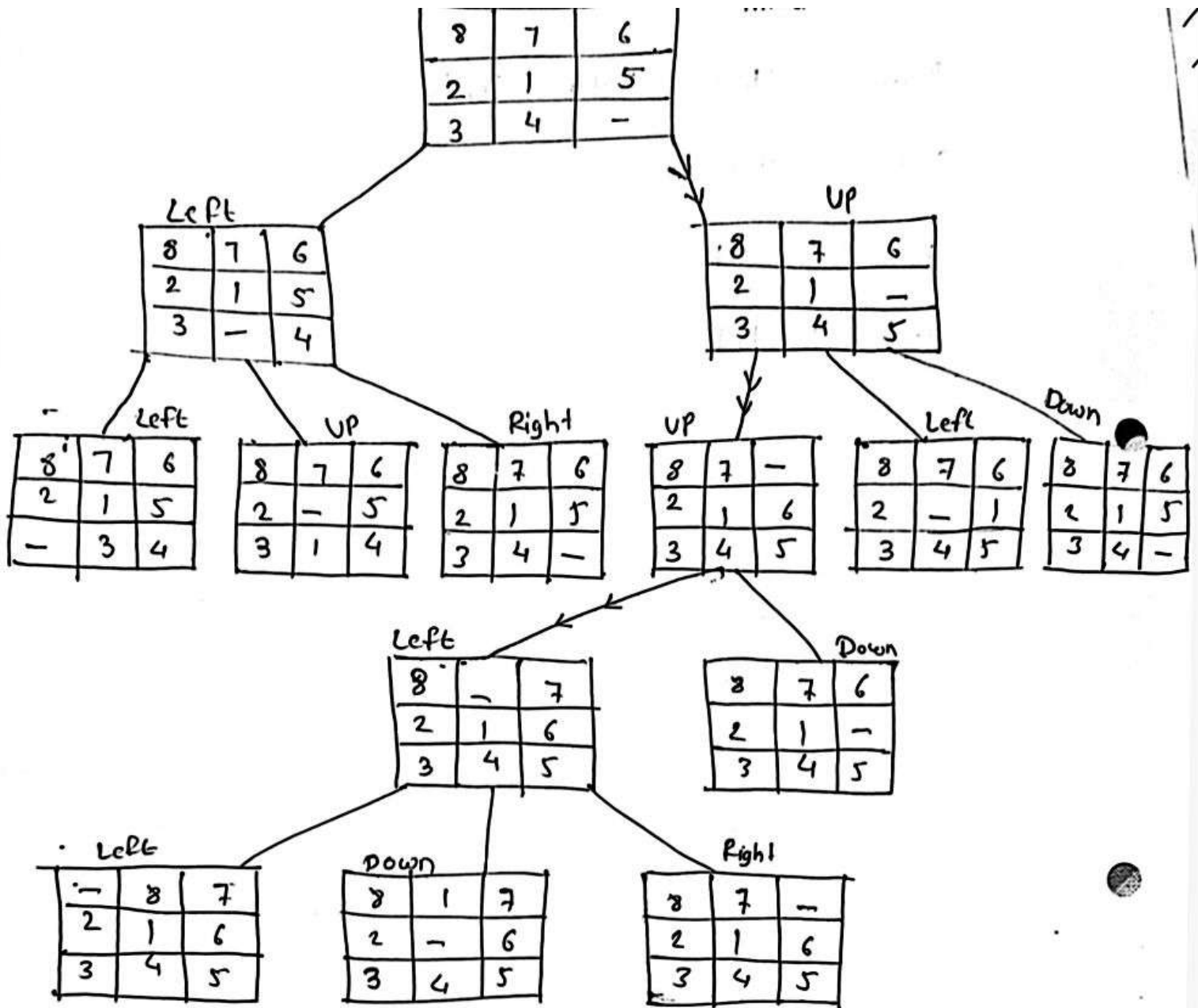
for  $i = 3$ ,  $n = \text{initial state}$

$h_3(\text{initial}) = \text{Sum of manhattan distance between current \& current position of all tiles except space.}$

$$h_3(\text{initial}) = 0 + 0 + 0 + 0 + 1 + 1 + 1 + 1 = 4$$

for  $n = \text{goal state}$

$$h_3(\text{goal}) = 0$$



Final  
configuration.