

VISVESVARAYA TECHNOLOGICAL UNIVERSITY

“JnanaSangama”, Belgaum -590014, Karnataka.



LAB RECORD

Bio Inspired Systems (23CS5BSBIS)

Submitted by

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in partial fulfillment for the award of the degree of

**BACHELOR OF ENGINEERING
in
COMPUTER SCIENCE AND ENGINEERING**



**B.M.S. COLLEGE OF ENGINEERING
(Autonomous Institution under VTU)
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**B.M.S. College of Engineering,
Bull Temple Road, Bangalore 560019**
(Affiliated To Visvesvaraya Technological University, Belgaum)
Department of Computer Science and Engineering



CERTIFICATE

This is to certify that the Lab work entitled “ Bio Inspired Systems (23CS5BSBIS)” carried out by **Shashank S P (1BM22CS256)**, who is a bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements of the above mentioned subject and the work prescribed for the said degree.

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Github Link:

https://github.com/shashanksp2003/bis_lab

Program 1

Genetic Algorithm for Optimization Problems:

Genetic Algorithms (GA) are inspired by the process of natural selection and genetics, where the fittest individuals are selected for reproduction to produce the next generation. GAs are widely used for solving optimization and search problems. Implement a Genetic Algorithm using Python to solve a basic optimization problem, such as finding the maximum value of a mathematical function.

Implementation Steps:

1. Define the Problem: Create a mathematical function to optimize.
2. Initialize Parameters: Set the population size, mutation rate, crossover rate, and number of generations.
3. Create Initial Population: Generate an initial population of potential solutions.
4. Evaluate Fitness: Evaluate the fitness of each individual in the population.
5. Selection: Select individuals based on their fitness to reproduce.
6. Crossover: Perform crossover between selected individuals to produce offspring.
7. Mutation: Apply mutation to the offspring to maintain genetic diversity.
8. Iteration: Repeat the evaluation, selection, crossover, and mutation processes for a fixed number of generations or until convergence criteria are met.
9. Output the Best Solution: Track and output the best solution found during the generations.

Lab-01

shows Initialization Population

Genetic Algorithm

Initialize population with random solutions
evaluate the fitness of each individual in the population.

while (stopping criteria not met):
 select parents from the population based on fitness

 apply crossover to create offspring

 apply mutation to offspring with a certain probability

 evaluate the fitness of each offspring
 select individuals for the next generation
 from current population and offspring

 update population with new generation

return the best solution found

Initialize population! create an initial set of random solutions.

evaluate fitness; calculate how good each solution is according to a fitness function.

selection: choose parents based on fitness.

Using, roulette wheel selection?.

Crossover: combine parents to create new offspring, inheriting traits from both parents.

mutation: apply small random changes to offspring to maintain diversity.

Fitness evaluation - calculate fitness for each offspring.

Survivor selection: choose individuals for the next generation, often based on fitness.

Repeat: continue until termination condition is met.

Result: the best solution found over generations.

possible
i) Define f

$f(x)$

where x :

\mathbf{x}

\mathbf{x}_i is v

vec

real:

ii) Initial

$n \rightarrow h$

$w \rightarrow \mathbb{R}^n$

$c_1 \rightarrow c$

on

$c_2 \rightarrow s$

iii) Initial

$x \rightarrow \mathbb{R}^n$

$y \rightarrow \mathbb{R}^m$

persons

persons

Code:

```

import random

def fitness(x):
    return x**2

def initialize_population(pop_size, low, high):
    return [random.uniform(low, high) for _ in range(pop_size)]

def selection(population, fitness_values):
    total_fitness = sum(fitness_values)
    selection_probs = [f / total_fitness for f in fitness_values]
    return random.choices(population, weights=selection_probs, k=2)

def crossover(parent1, parent2):
    alpha = random.random()
    offspring1 = alpha * parent1 + (1 - alpha) * parent2
    offspring2 = alpha * parent2 + (1 - alpha) * parent1
    return offspring1, offspring2

def mutate(individual, mutation_rate, low, high):
    if random.random() < mutation_rate:
        return random.uniform(low, high)
    return individual

def genetic_algorithm(pop_size, generations, low, high, mutation_rate, crossover_rate):
    population = initialize_population(pop_size, low, high)
    best_solution = None
    best_fitness = float('-inf')

    for generation in range(generations):
        fitness_values = [fitness(ind) for ind in population]

        max_fitness = max(fitness_values)
        if max_fitness > best_fitness:
            best_fitness = max_fitness
            best_solution = population[fitness_values.index(max_fitness)]

        new_population = []
        while len(new_population) < pop_size:
            parent1, parent2 = selection(population, fitness_values)

            if random.random() < crossover_rate:
                offspring1, offspring2 = crossover(parent1, parent2)
            else:
                offspring1, offspring2 = parent1, parent2

            offspring1 = mutate(offspring1, mutation_rate, low, high)
            offspring2 = mutate(offspring2, mutation_rate, low, high)

            new_population.append(offspring1)
            new_population.append(offspring2)

    return best_solution

```

```
new_population.extend([offspring1, offspring2])

population = new_population[:pop_size]

print(f"Generation {generation+1}: Best fitness = {best_fitness:.4f}, Best solution = {best_solution:.4f}")

print(f"\nBest solution found: x = {best_solution:.4f}, f(x) = {best_fitness:.4f}")

population_size = 100
num_generations = 10
x_range_low = -10
x_range_high = 10
mutation_rate = 0.1
crossover_rate = 0.7

genetic_algorithm(population_size, num_generations, x_range_low, x_range_high, mutation_rate,
crossover_rate)
```

Output:

```
→ Generation 1: Best fitness = 99.5858, Best solution = 9.9793
Generation 2: Best fitness = 99.5858, Best solution = 9.9793
Generation 3: Best fitness = 99.5858, Best solution = 9.9793
Generation 4: Best fitness = 99.5858, Best solution = 9.9793
Generation 5: Best fitness = 99.5858, Best solution = 9.9793
Generation 6: Best fitness = 99.5858, Best solution = 9.9793
Generation 7: Best fitness = 99.5858, Best solution = 9.9793
Generation 8: Best fitness = 99.5858, Best solution = 9.9793
Generation 9: Best fitness = 99.5858, Best solution = 9.9793
Generation 10: Best fitness = 99.5858, Best solution = 9.9793

Best solution found: x = 9.9793, f(x) = 99.5858
```

Program 2

Particle Swarm Optimization for Function Optimization:

Particle Swarm Optimization (PSO) is inspired by the social behavior of birds flocking or fish schooling. PSO is used to find optimal solutions by iteratively improving a candidate solution with regard to a given measure of quality. Implement the PSO algorithm using Python to optimize a mathematical function.

Implementation Steps:

1. Define the Problem: Create a mathematical function to optimize.
2. Initialize Parameters: Set the number of particles, inertia weight, cognitive and social coefficients.
3. Initialize Particles: Generate an initial population of particles with random positions and velocities.
4. Evaluate Fitness: Evaluate the fitness of each particle based on the optimization function.
5. Update Velocities and Positions: Update the velocity and position of each particle based on its own best position and the global best position.
6. Iterate: Repeat the evaluation, updating, and position adjustment for a fixed number of iterations or until convergence criteria are met.
7. Output the Best Solution: Track and output the best solution found during the iterations.

Set of
such solutions
with different
structures,
so some
are better
than others
and some
are worse.
for
fitness
measures
for
different
solutions.

Lab-02

Particle Swarm Optimization (PSO)

i) Define problem

$$f(x) = A \cdot n + \sum_{i=1}^n [x_i^2 - A \cdot \cos(2\pi x_i)]$$

where $A=10$, n = dimensionality of

Input x
 x_i is value of variable in input

vector of $()$ containing all variables

Goal: to minimize the function.

ii) Initialize parameters.

$n \rightarrow$ no. of variables

$w \rightarrow$ initial weight

$c_1 \rightarrow$ cognitive coefficient (controls particle's own best position)

$c_2 \rightarrow$ social coeff (best known position by swarm)

iii) Initialize particles

$x \rightarrow$ position

$y \rightarrow$ velocity

personal best position (p_i^*)

personal best fitness ($f(p_i^*)$)

4) Evaluate fitness

Rostrum function: calculate smooth objective
fitness for current position; score =
 $f(x^i)$

if score < personal-best-score[i];
update personal-best-position[i] +
 x^i .

update personal-best-store[i] to score.

5) Update velocities & positions

generate random values, η_1, η_2 ,

$\eta_1 \in [0, 1]$.

update velocity $(w + v_i[+] + (1 + \eta_1) * (v_i[i] - pos[i]) +$

$(2 + \eta_2) * (global-best-pos - pos[i]))$

update position.

b) Iterate

for each iteration t ($t = 1$ to num-iterations);

for each particle i ($i = 1$ to num-particles);

Calculate fitness score @ new position

($\eta_1 + \eta_2$) weight local learning

~~# output~~

output best solution

after, return global best position & score

Global minimum occurs @ $x_i = 0$. (all $x_i \geq 0$)

$$\text{i.e. } R_n + (0 - R_n) = R_n - R_n = 0$$

(i.e.)

for $x_i \geq 0$

This problem is too simple.

not even one good place

to start with no local minima

but, it's still a good start

not bad

so, (f, g) form two binaries paligato siha

(binaries) so binarotni

Not / not work with for finding with doubles

of bin

(f, g) opti case not

Code:

```

import numpy as np
import random
import matplotlib.pyplot as plt

def rastrigin(x):
    return 10 * len(x) + sum([(xi ** 2 - 10 * np.cos(2 * np.pi * xi)) for xi in x])

class Particle:
    def __init__(self, dim, bounds):
        self.position = np.random.uniform(bounds[0], bounds[1], dim)
        self.velocity = np.random.uniform(-1, 1, dim)
        self.best_position = np.copy(self.position)
        self.best_value = rastrigin(self.position)

    def evaluate(self):
        current_value = rastrigin(self.position)
        if current_value < self.best_value:
            self.best_value = current_value
            self.best_position = np.copy(self.position)

def pso(dim, bounds, num_particles=30, max_iter=100, w=0.5, c1=1.5, c2=1.5):
    particles = [Particle(dim, bounds) for _ in range(num_particles)]

    global_best_position = None
    global_best_value = float('inf')

    best_values_over_iterations = []

    for iter in range(max_iter):
        for particle in particles:
            particle.evaluate()
            if particle.best_value < global_best_value:
                global_best_value = particle.best_value
                global_best_position = np.copy(particle.best_position)

        best_values_over_iterations.append(global_best_value)

        for particle in particles:
            inertia = w * particle.velocity
            cognitive = c1 * np.random.random() * (particle.best_position - particle.position)
            social = c2 * np.random.random() * (global_best_position - particle.position)

            particle.velocity = inertia + cognitive + social
            particle.position = particle.position + particle.velocity

            particle.position = np.clip(particle.position, bounds[0], bounds[1])

        if (iter+1) % 10 == 0:

```

```

print(f"Iteration {iter+1}/{max_iter}, Global Best Value: {global_best_value}")

return global_best_position, global_best_value, particles, best_values_over_iterations

if __name__ == "__main__":
    dim = 2
    bounds = [-5.12, 5.12]

    best_position, best_value, particles, best_values_over_iterations = pso(dim, bounds,
num_particles=30, max_iter=100)

    print("\nFinal Best Position:", best_position)
    print("Final Best Value:", best_value)

fig, ax = plt.subplots(figsize=(8, 6))

final_best_positions = np.array([particle.best_position for particle in particles])

    ax.scatter(final_best_positions[:, 0], final_best_positions[:, 1], color='blue', label="Particle Best
Positions", alpha=0.7)

    ax.scatter(best_position[0], best_position[1], color='red', label="Global Best", s=100, marker='*')

    ax.set_title("Final Particle Positions in PSO")
    ax.set_xlabel("Dimension 1")
    ax.set_ylabel("Dimension 2")
    ax.legend()
    plt.grid(True)
    plt.show()

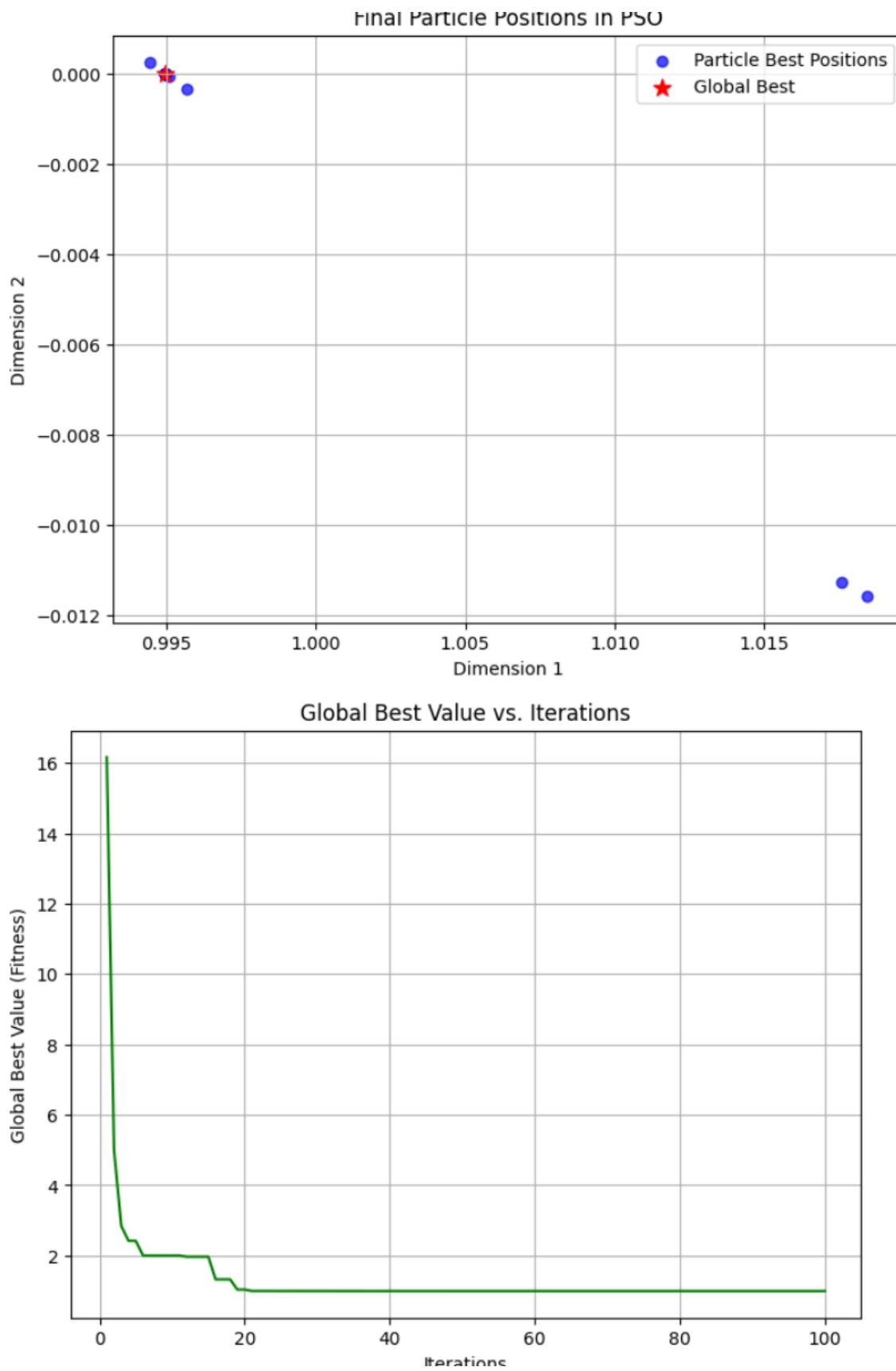
plt.figure(figsize=(8, 6))
plt.plot(range(1, len(best_values_over_iterations) + 1), best_values_over_iterations, color='green')
plt.title("Global Best Value vs. Iterations")
plt.xlabel("Iterations")
plt.ylabel("Global Best Value (Fitness)")
plt.grid(True)
plt.show()

```

Output:

```
→ Iteration 10/100, Global Best Value: 2.003250667292207
Iteration 20/100, Global Best Value: 1.0371970536607833
Iteration 30/100, Global Best Value: 0.9965161455248861
Iteration 40/100, Global Best Value: 0.9949848667711656
Iteration 50/100, Global Best Value: 0.9949610887864182
Iteration 60/100, Global Best Value: 0.994959059938175
Iteration 70/100, Global Best Value: 0.9949590571109823
Iteration 80/100, Global Best Value: 0.9949590570934674
Iteration 90/100, Global Best Value: 0.9949590570932898
Iteration 100/100, Global Best Value: 0.9949590570932898

Final Best Position: [ 9.94958638e-01 -8.70961770e-10]
Final Best Value: 0.9949590570932898
```



Program 3

Ant Colony Optimization for the Traveling Salesman Problem:

The foraging behavior of ants has inspired the development of optimization algorithms that can solve complex problems such as the Traveling Salesman Problem (TSP). Ant Colony Optimization (ACO) simulates the way ants find the shortest path between food sources and their nest. Implement the ACO algorithm using Python to solve the TSP, where the objective is to find the shortest possible route that visits a list of cities and returns to the origin city.

Implementation Steps:

1. Define the Problem: Create a set of cities with their coordinates.
2. Initialize Parameters: Set the number of ants, the importance of pheromone (α), the importance of heuristic information (β), the evaporation rate (ρ), and the initial pheromone value.
3. Construct Solutions: Each ant constructs a solution by probabilistically choosing the next city based on pheromone trails and heuristic information.
4. Update Pheromones: After all ants have constructed their solutions, update the pheromone trails based on the quality of the solutions found.
5. Iterate: Repeat the construction and updating process for a fixed number of iterations or until convergence criteria are met.
6. Output the Best Solution: Keep track of and output the best solution found during the iterations.

lab-03

14/11/24

Ant - colony optimization for the Traveling Salesman problem

Pseudocode:

Initialize pheromone levels on all edges

(Σ_{ij})

for each ant :

Randomly select a starting city.

for each step in the tour;

choose the next city based on the pheromone level and distance heuristic

Add the city to the ant's tour

End for

For

while stopping criteria not met (e.g. max iterations or convergence):

For each ant ;

Evaluate the quality of the solution / tour length)

End for

For each edge (i, j);

update

I-if E

where D

by a

D I-if

else

End if

Apply p

I-if

End while

Return

Initializ

update pheromone on edge (i, j) based
on ant tours:

$$\tau_{ij} \leftarrow (1 - \rho) \tau_{ij} + \Delta \tau_{ij}$$

where $\Delta \tau_{ij}$ is the pheromone deposited
by ant k :

$$\Delta \tau_{ij} = \sum_k \frac{1}{L_k} \text{tours length of ant } k$$

End for.

Apply pheromone evaporation:

$$\tau_{ij} \leftarrow (1 - \rho) \tau_{ij} + \tau_{ij} \text{ for all edges } (i, j)$$

End while.

Return the best sol's found

Initialization

S. Sankar

b)

Code:

```

import numpy as np
import matplotlib.pyplot as plt

# 1. Define the Problem: Create a set of cities with their coordinates
cities = np.array([
    [0, 0], # City 0
    [1, 5], # City 1
    [5, 1], # City 2
    [6, 4], # City 3
    [7, 8], # City 4
])
# Calculate the distance matrix between each pair of cities
def calculate_distances(cities):
    num_cities = len(cities)
    distances = np.zeros((num_cities, num_cities))

    for i in range(num_cities):
        for j in range(num_cities):
            distances[i][j] = np.linalg.norm(cities[i] - cities[j])

    return distances

distances = calculate_distances(cities)

# 2. Initialize Parameters
num_ants = 10
num_cities = len(cities)
alpha = 1.0 # Influence of pheromone
beta = 5.0 # Influence of heuristic (inverse distance)
rho = 0.5 # Evaporation rate
num_iterations = 10
initial_pheromone = 1.0

# Pheromone matrix initialization
pheromone = np.ones((num_cities, num_cities)) * initial_pheromone

# 3. Heuristic information (Inverse of distance)
def heuristic(distances):
    with np.errstate(divide='ignore'): # Ignore division by zero
        return 1 / distances

eta = heuristic(distances)

# 4. Choose next city probabilistically based on pheromone and heuristic info
def choose_next_city(pheromone, eta, visited):
    probs = []
    for j in range(num_cities):

```

```

if j not in visited:
    pheromone_ij = pheromone[visited[-1], j] ** alpha
    heuristic_ij = eta[visited[-1], j] ** beta
    probs.append(pheromone_ij * heuristic_ij)
else:
    probs.append(0)
probs = np.array(probs)
return np.random.choice(range(num_cities), p=probs / probs.sum())

# Construct solution for a single ant
def construct_solution(pheromone, eta):
    tour = [np.random.randint(0, num_cities)]
    while len(tour) < num_cities:
        next_city = choose_next_city(pheromone, eta, tour)
        tour.append(next_city)
    return tour

# 5. Update pheromones after all ants have constructed their tours
def update_pheromones(pheromone, all_tours, distances, best_tour):
    pheromone *= (1 - rho) # Evaporate pheromones

    # Add pheromones for each ant's tour
    for tour in all_tours:
        tour_length = sum([distances[tour[i], tour[i + 1]] for i in range(-1, num_cities - 1)])
        for i in range(-1, num_cities - 1):
            pheromone[tour[i], tour[i + 1]] += 1.0 / tour_length

    # Increase pheromones on the best tour
    best_length = sum([distances[best_tour[i], best_tour[i + 1]] for i in range(-1, num_cities - 1)])
    for i in range(-1, num_cities - 1):
        pheromone[best_tour[i], best_tour[i + 1]] += 1.0 / best_length

# 6. Main ACO Loop: Iterate over multiple iterations to find the best solution
def run_aco(distances, num_iterations):
    pheromone = np.ones((num_cities, num_cities)) * initial_pheromone
    best_tour = None
    best_length = float('inf')

    for iteration in range(num_iterations):
        all_tours = [construct_solution(pheromone, eta) for _ in range(num_ants)]
        all_lengths = [sum([distances[tour[i], tour[i + 1]] for i in range(-1, num_cities - 1)]) for tour in all_tours]

        current_best_length = min(all_lengths)
        current_best_tour = all_tours[all_lengths.index(current_best_length)]

        if current_best_length < best_length:
            best_length = current_best_length
            best_tour = current_best_tour

```

```

update_pheromones(pheromone, all_tours, distances, best_tour)

print(f"Iteration {iteration + 1}, Best Length: {best_length}")

return best_tour, best_length

# Run the ACO algorithm
best_tour, best_length = run_aco(distances, num_iterations)

# 7. Output the Best Solution
print(f"Best Tour: {best_tour}")
print(f"Best Tour Length: {best_length}")

# 8. Plot the Best Route
def plot_route(cities, best_tour):
    plt.figure(figsize=(8, 6))
    for i in range(len(cities)):
        plt.scatter(cities[i][0], cities[i][1], color='red')
        plt.text(cities[i][0], cities[i][1], f"City {i}", fontsize=12)

    # Plot the tour as lines connecting the cities
    tour_cities = np.array([cities[i] for i in best_tour] + [cities[best_tour[0]]]) # Complete the loop by
    returning to the start
    plt.plot(tour_cities[:, 0], tour_cities[:, 1], linestyle='-', marker='o', color='blue')

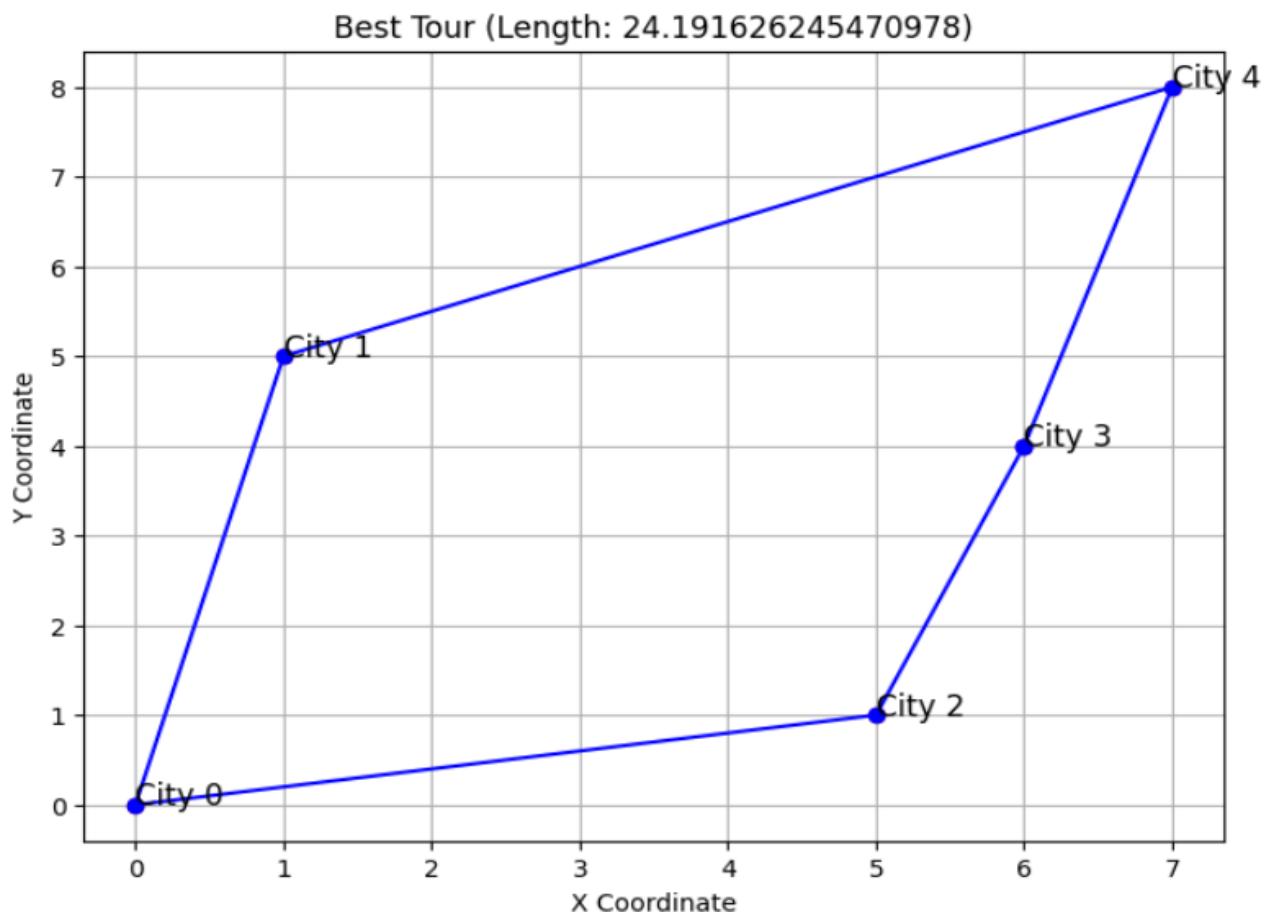
    plt.title(f"Best Tour (Length: {best_length})")
    plt.xlabel("X Coordinate")
    plt.ylabel("Y Coordinate")
    plt.grid(True)
    plt.show()

# Call the plot function
plot_route(cities, best_tour)

```

Output:

```
Iteration 1, Best Length: 24.191626245470978
Iteration 2, Best Length: 24.191626245470978
Iteration 3, Best Length: 24.191626245470978
Iteration 4, Best Length: 24.191626245470978
Iteration 5, Best Length: 24.191626245470978
Iteration 6, Best Length: 24.191626245470978
Iteration 7, Best Length: 24.191626245470978
Iteration 8, Best Length: 24.191626245470978
Iteration 9, Best Length: 24.191626245470978
Iteration 10, Best Length: 24.191626245470978
Best Tour: [3, 4, 1, 0, 2]
Best Tour Length: 24.191626245470978
```



Program 4

Cuckoo Search (CS):

Cuckoo Search (CS) is a nature-inspired optimization algorithm based on the brood parasitism of some cuckoo species. This behavior involves laying eggs in the nests of other birds, leading to the optimization of survival strategies. CS uses Lévy flights to generate new solutions, promoting global search capabilities and avoiding local minima. The algorithm is widely used for solving continuous optimization problems and has applications in various domains, including engineering design, machine learning, and data mining.

Implementation Steps:

1. Define the Problem: Create a mathematical function to optimize.
2. Initialize Parameters: Set the number of nests, the probability of discovery, and the number of iterations.
3. Initialize Population: Generate an initial population of nests with random positions.
4. Evaluate Fitness: Evaluate the fitness of each nest based on the optimization function.
5. Generate New Solutions: Create new solutions via Lévy flights.
6. Abandon Worst Nests: Abandon a fraction of the worst nests and replace them with new random positions.
7. Iterate: Repeat the evaluation, updating, and replacement process for a fixed number of iterations or until convergence criteria are met.
8. Output the Best Solution: Track and output the best solution found during the iterations.

21/ May

LAB-04

Cuckoo Search

1. Initialization

- * Set parameters n , p_a and max. Iter
- * Randomly initialize a population of n nests (solutions)
- * x_i for $i = 1, 2, \dots, n$
- * Evaluate the fitness $f(x_i)$ for each nest using the objective function.

2. Generate new Solutions

- * for each nest, generate a new solution x_{new} using levy flights, $x_{\text{new}} = x_{\text{current}} + d \cdot \text{levy}(\lambda)$ where d is a step size scaling factor, and $\text{levy}(\lambda)$ is the step drawn from a Levy distribution.
- * Evaluate $f(x_{\text{new}})$.
- * Replace x_i with x_{new} if $f(x_{\text{new}})$ is better.

3. Discovery of alien eggs.

- * Randomly choose a fraction p_a of the worst nests (based on fitness)

- * Replace these nests with new random solutions

1. update

+ Track

5. iterate

+ Repeat iterations

Convergence

6. output

+ Return

Pseudo

Input:

n , p_a

Output

1. Init

2. Eval

3. while

a. or

fe

if

24

1. update Best solution (solution is initialized)

+ Track the best solution x^* with the highest fitness

2. iterate

+ Repeat steps 2-4 until the max no. of iterations max_iter is reached or a convergence criterion is satisfied.

3. output the best solution.

+ Return x^* the sol'n with best fitness.

Pseudo code

Input: objective function $f(x)$, parameters n, pa, max_iter

Output: Best solution x^*

1. Initialize a nest x_i randomly

2. Evaluate fitness $f(x_i)$ for each nest

3. while $t < \text{max_iter}$ do:

a. generate new solutions using Levy flights

for each nest i :

$$x_{\text{new}} = x_{\text{current}} + \lambda * \text{levy}(X)$$

if $f(x_{\text{new}}) > f(x_i)$:

$$x_i = x_{\text{new}}$$

b. Replace a fraction per of the worst nests
with new random solutions and sort them.

c. Keep track of the best sol'n x^*

4. End while

5. Return x^*

Solved
Date: 21/11/24

" Grey "

Step

Algorithm

Step-01 in

• Define the

D. O.

• Set the pop
maximum ,
ant brizi

Step-02 in

• Randomly
in The

• Assign in
and delta (evalution)

Step-03 upd

• For each t
D from d .

D -

• update the
weighted inf

$x = \underline{?}$

(X) few + to + known - x = worse

: (i-x) + v (worse-x) + ?

worse-x > 1-x

Code:

```

import numpy as np
import random
import math
import matplotlib.pyplot as plt

# Define a sample function to optimize (Sphere function in this case)
def objective_function(x):
    return np.sum(x ** 2)

# Lévy flight function
def levy_flight(Lambda):
    sigma_u = (math.gamma(1 + Lambda) * np.sin(np.pi * Lambda / 2) /
               (math.gamma((1 + Lambda) / 2) * Lambda * 2 ** ((Lambda - 1) / 2))) ** (1 / Lambda)
    sigma_v = 1
    u = np.random.normal(0, sigma_u, size=1)
    v = np.random.normal(0, sigma_v, size=1)
    step = u / (abs(v) ** (1 / Lambda))
    return step

# Cuckoo Search algorithm
def cuckoo_search(num_nests=25, num_iterations=100, discovery_rate=0.25, dim=5,
                  lower_bound=-10, upper_bound=10):
    # Initialize nests
    nests = np.random.uniform(lower_bound, upper_bound, (num_nests, dim))
    fitness = np.array([objective_function(nest) for nest in nests])

    # Get the current best nest
    best_nest_idx = np.argmin(fitness)
    best_nest = nests[best_nest_idx].copy()
    best_fitness = fitness[best_nest_idx]

    Lambda = 1.5 # Parameter for Lévy flights
    fitness_history = [] # To track fitness at each iteration

    for iteration in range(num_iterations):
        # Generate new solutions via Lévy flight
        for i in range(num_nests):
            step_size = levy_flight(Lambda)
            new_solution = nests[i] + step_size * (nests[i] - best_nest)
            new_solution = np.clip(new_solution, lower_bound, upper_bound)
            new_fitness = objective_function(new_solution)

            # Replace nest if new solution is better
            if new_fitness < fitness[i]:
                nests[i] = new_solution
                fitness[i] = new_fitness

        # Discover some nests with probability 'discovery_rate'
        for i in range(int(discovery_rate * num_nests)):
            nest_idx = random.randint(0, num_nests - 1)
            new_nest = levy_flight(Lambda)
            new_fitness = objective_function(new_nest)
            if new_fitness < fitness[nest_idx]:
                nests[nest_idx] = new_nest
                fitness[nest_idx] = new_fitness

```

```

random_nests = np.random.choice(num_nests, int(discovery_rate * num_nests), replace=False)
for nest_idx in random_nests:
    nests[nest_idx] = np.random.uniform(lower_bound, upper_bound, dim)
    fitness[nest_idx] = objective_function(nests[nest_idx])

# Update the best nest
current_best_idx = np.argmin(fitness)
if fitness[current_best_idx] < best_fitness:
    best_fitness = fitness[current_best_idx]
    best_nest = nests[current_best_idx].copy()

# Store fitness for plotting
fitness_history.append(best_fitness)

# Print the best solution at each iteration (optional)
print(f"Iteration {iteration+1}/{num_iterations}, Best Fitness: {best_fitness}")

# Plot fitness convergence graph
plt.plot(fitness_history)
plt.title('Fitness Convergence Over Iterations')
plt.xlabel('Iteration')
plt.ylabel('Best Fitness')
plt.show()

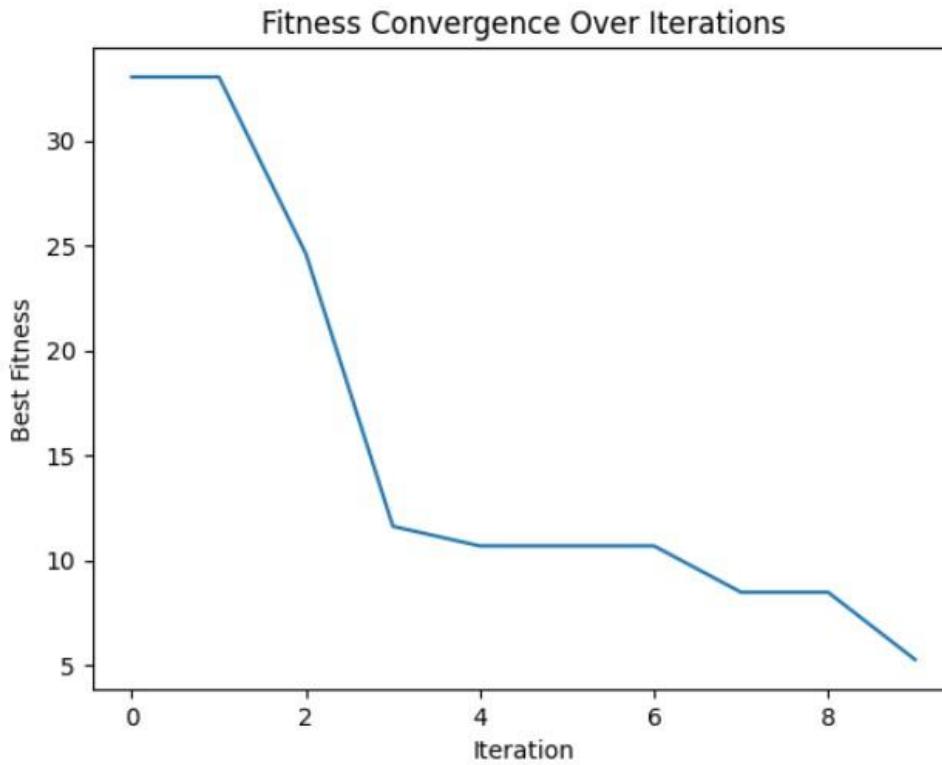
# Return the best solution found
return best_nest, best_fitness

# Example usage
best_nest, best_fitness = cuckoo_search(num_nests=30, num_iterations=10, dim=10,
lower_bound=-5, upper_bound=5)
print("Best Solution:", best_nest)
print("Best Fitness:", best_fitness)

```

Output:

```
Iteration 1/10, Best Fitness: 33.041281203083585  
Iteration 2/10, Best Fitness: 33.041281203083585  
Iteration 3/10, Best Fitness: 24.61474034339304  
Iteration 4/10, Best Fitness: 11.62274110008269  
Iteration 5/10, Best Fitness: 10.689701522637932  
Iteration 6/10, Best Fitness: 10.689701522637932  
Iteration 7/10, Best Fitness: 10.689701522637932  
Iteration 8/10, Best Fitness: 8.483040606104721  
Iteration 9/10, Best Fitness: 8.483040606104721  
Iteration 10/10, Best Fitness: 5.27254818921324
```



```
Best Solution: [-0.44074699  0.44475909 -0.40497755 -1.1444419  -0.79762137  0.46740521  
-0.91064972 -1.00122337  0.38893795 -0.7543568 ]  
Best Fitness: 5.27254818921324
```

Program 5

Grey Wolf Optimizer (GWO):

The Grey Wolf Optimizer (GWO) algorithm is a swarm intelligence algorithm inspired by the social hierarchy and hunting behavior of grey wolves. It mimics the leadership structure of alpha, beta, delta, and omega wolves and their collaborative hunting strategies. The GWO algorithm uses these social hierarchies to model the optimization process, where the alpha wolves guide the search process while beta and delta wolves assist in refining the search direction. This algorithm is effective for continuous optimization problems and has applications in engineering, data analysis, and machine learning.

Implementation Steps:

1. Define the Problem: Create a mathematical function to optimize.
2. Initialize Parameters: Set the number of wolves and the number of iterations.
3. Initialize Population: Generate an initial population of wolves with random positions.
4. Evaluate Fitness: Evaluate the fitness of each wolf based on the optimization function.
5. Update Positions: Update the positions of the wolves based on the positions of alpha, beta, and delta wolves.
6. Iterate: Repeat the evaluation and position updating process for a fixed number of iterations or until convergence criteria are met.
7. Output the Best Solution: Track and output the best solution found during the iterations.

Lab-05

23/11/24

"Grey wolf optimizer"Step"Algorithm"Step-01 initialize the problem

- Define the optimization problem (objective function $f(x)$)

- Set the population size n (number of wolves) and maximum number of iterations T .

Step-02, initialize the parameters

- Randomly initialize the position of wolf in the search space

- Assign initial positions to alpha (α), beta (β) and delta (γ) wolves based on fitness evaluation.

Step-03, update the positions

- For each wolf in the pack calculate its distance from α , β and γ wolves using

$$D = |C - X_{best} - X|$$

- update the position of each wolf based on the weighted influence of α , β and γ

$$x = \frac{x_1 + x_2 + x_3}{3}$$

where, x_1, x_2, x_3 are updated positions using
1, β , & 8 wolves.

Step-04: Adjust exploration and exploitation.

- update the coefficient vectors A & C

$$A = 2\alpha \cdot r_1 - \alpha, C = 2 \cdot r_2$$

where

- α decreases linearly from 2 to 0 over iterations to control exploration/exploitation.

r_1, r_2 are random numbers in $[0, 1]$.

Step-05: Evaluate fitness.

- Evaluate the fitness of each wolf using the objective function $f(x)$.

- update α, β, γ & 8 wolves if better solutions are found.

Step-06:

- if the maximum number of iterations T is reached or the solution has converged, return the alpha wolf (α) as the best solution.

- otherwise go back to step 3.

pseudo-

1. initial
random

2. Evalu

Alpha

Beta

Delta w

while($t <$

a. for e

b. calcu

and

D-alpha

D-beta

D-delt

ii). updat

x_new

b) upda

A = 20

C = 2

pseudo-code

1. initialize the population (positions of wolf)
randomly within the search space.

2. Evaluate the fitness of each wolf & identify:
Alpha wolf (best sol'n so far).

Beta wolf (second best sol'n)

Delta wolf (third - best sol'n).

while($t < 1$):

a. for each wolf in the population

i. calculate the distance D from alpha,beta,
and delta.

$$D_{\text{alpha}} = |C_{\text{alpha}}^T \cdot x_{\text{alpha}} - x|$$

$$D_{\text{beta}} = |C_{\text{beta}}^T \cdot x_{\text{beta}} - x|$$

$$D_{\text{delta}} = |C_{\text{delta}}^T \cdot x_{\text{delta}} - x|$$

ii. update the position of the wolf:

$$x_{\text{new}} = (x_{\text{alpha}} - A_{\text{alpha}} * D_{\text{alpha}} * x_{\text{alpha}} +$$

$$x_{\text{beta}} - A_{\text{beta}} * D_{\text{beta}} * x_{\text{beta}} +$$

~~$$x_{\text{delta}} - A_{\text{delta}} * D_{\text{delta}} * x_{\text{delta}}) / 3$$~~

b) update the values of coefficient vectors A & C;

$$A = 2\alpha * \gamma_1 - \alpha$$

$$C = \gamma_1 + \gamma_2$$

(where ' α ' decreases linearly from 2 to 0,
and α_1 and α_2 are random on $[0, 1]$)

C. Evaluate the fitness of all wolves

D. Update alpha, beta, & delta wolves

E. Based on fitness, select best solution

F. Increment t by 1

G. Output the alpha wolf as the best soln.

~~for task~~

b) Parse

function

return

function

neight

for di

for

if :

ni =

nj =

neigh

return

function

for e

new si

l - .pn

return n

function

initial

initial

Code:

```

import numpy as np
import matplotlib.pyplot as plt

# Step 1: Define the Problem (a mathematical function to optimize)
def objective_function(x):
    return np.sum(x**2) # Example: Sphere function (minimize sum of squares)

# Step 2: Initialize Parameters
num_wolves = 5 # Number of wolves in the pack
num_dimensions = 2 # Number of dimensions (for the optimization problem)
num_iterations = 10 # Number of iterations
lb = -10 # Lower bound of search space
ub = 10 # Upper bound of search space

# Step 3: Initialize Population (Generate initial positions randomly)
wolves = np.random.uniform(lb, ub, (num_wolves, num_dimensions))

# Initialize alpha, beta, delta wolves
alpha_pos = np.zeros(num_dimensions)
beta_pos = np.zeros(num_dimensions)
delta_pos = np.zeros(num_dimensions)

alpha_score = float('inf') # Best (alpha) score
beta_score = float('inf') # Second best (beta) score
delta_score = float('inf') # Third best (delta) score

# To store the alpha score over iterations for graphing
alpha_score_history = []

# Step 4: Evaluate Fitness and assign Alpha, Beta, Delta wolves
def evaluate_fitness():
    global alpha_pos, beta_pos, delta_pos, alpha_score, beta_score, delta_score

    for wolf in wolves:
        fitness = objective_function(wolf)

        # Update Alpha, Beta, Delta wolves based on fitness
        if fitness < alpha_score:
            delta_score = beta_score
            delta_pos = beta_pos.copy()

            beta_score = alpha_score
            beta_pos = alpha_pos.copy()

            alpha_score = fitness
            alpha_pos = wolf.copy()
        elif fitness < beta_score:
            delta_score = beta_score

```

```

delta_pos = beta_pos.copy()

beta_score = fitness
beta_pos = wolf.copy()
elif fitness < delta_score:
    delta_score = fitness
    delta_pos = wolf.copy()

# Step 5: Update Positions
def update_positions(iteration):
    a = 2 - iteration * (2 / num_iterations) # a decreases linearly from 2 to 0

    for i in range(num_wolves):
        for j in range(num_dimensions):
            r1 = np.random.random()
            r2 = np.random.random()

            # Position update based on alpha
            A1 = 2 * a * r1 - a
            C1 = 2 * r2
            D_alpha = abs(C1 * alpha_pos[j] - wolves[i, j])
            X1 = alpha_pos[j] - A1 * D_alpha

            # Position update based on beta
            r1 = np.random.random()
            r2 = np.random.random()
            A2 = 2 * a * r1 - a
            C2 = 2 * r2
            D_beta = abs(C2 * beta_pos[j] - wolves[i, j])
            X2 = beta_pos[j] - A2 * D_beta

            # Position update based on delta
            r1 = np.random.random()
            r2 = np.random.random()
            A3 = 2 * a * r1 - a
            C3 = 2 * r2
            D_delta = abs(C3 * delta_pos[j] - wolves[i, j])
            X3 = delta_pos[j] - A3 * D_delta

            # Update wolf position
            wolves[i, j] = (X1 + X2 + X3) / 3

            # Apply boundary constraints
            wolves[i, j] = np.clip(wolves[i, j], lb, ub)

# Step 6: Iterate (repeat evaluation and position updating)
for iteration in range(num_iterations):
    evaluate_fitness() # Evaluate fitness of each wolf
    update_positions(iteration) # Update positions based on alpha, beta, delta

```

```
# Record the alpha score for this iteration
alpha_score_history.append(alpha_score)

# Optional: Print current best score
print(f"Iteration {iteration+1}/{num_iterations}, Alpha Score: {alpha_score}")

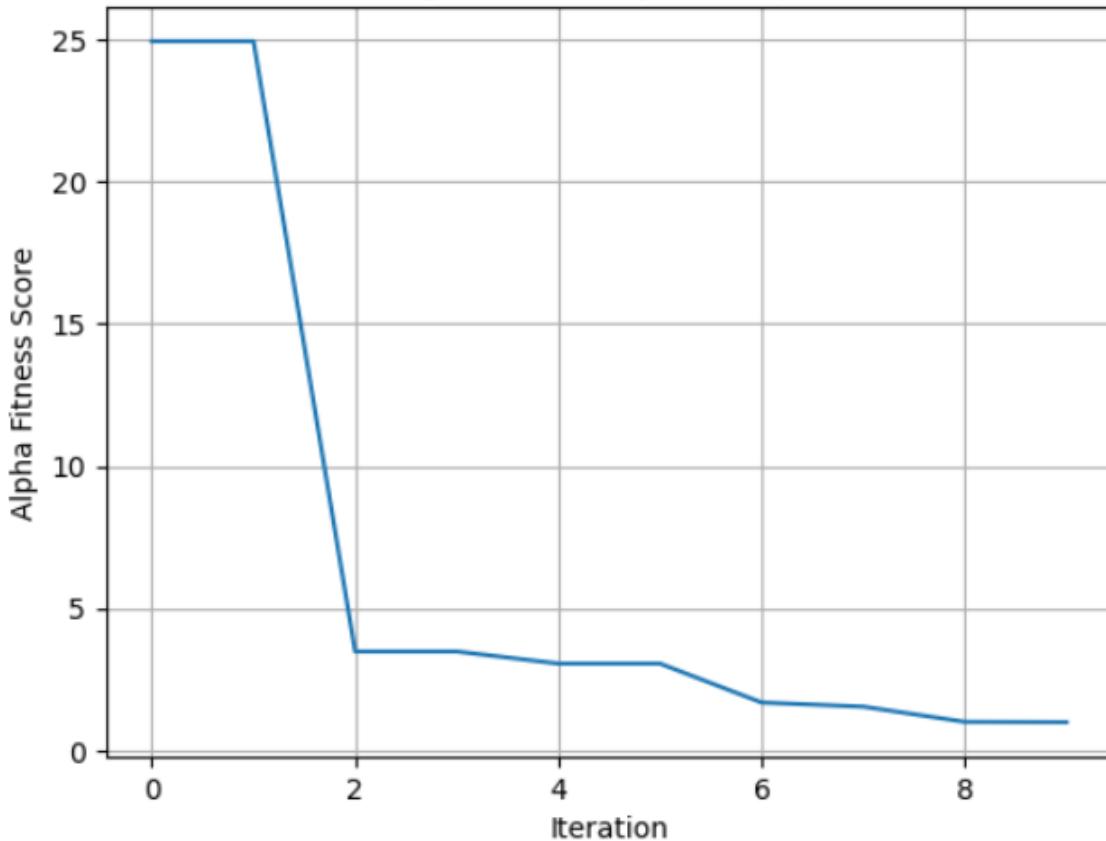
# Step 7: Output the Best Solution
print("Best Solution:", alpha_pos)
print("Best Solution Fitness:", alpha_score)

# Plotting the convergence graph
plt.plot(alpha_score_history)
plt.title('Convergence of Grey Wolf Optimizer')
plt.xlabel('Iteration')
plt.ylabel('Alpha Fitness Score')
plt.grid(True)
plt.show()
```

Output:

```
Iteration 1/10, Alpha Score: 24.938603997415413
Iteration 2/10, Alpha Score: 24.938603997415413
Iteration 3/10, Alpha Score: 3.478306502607043
Iteration 4/10, Alpha Score: 3.478306502607043
Iteration 5/10, Alpha Score: 3.0526022091841627
Iteration 6/10, Alpha Score: 3.0526022091841627
Iteration 7/10, Alpha Score: 1.6838080429555806
Iteration 8/10, Alpha Score: 1.5380015669091764
Iteration 9/10, Alpha Score: 1.0036157784249133
Iteration 10/10, Alpha Score: 0.9922915488635977
Best Solution: [ 0.82264201 -0.56173987]
Best Solution Fitness: 0.9922915488635977
```

Convergence of Grey Wolf Optimizer



Program 6

Parallel Cellular Algorithms and Programs:

Parallel Cellular Algorithms are inspired by the functioning of biological cells that operate in a highly parallel and distributed manner. These algorithms leverage the principles of cellular automata and parallel computing to solve complex optimization problems efficiently. Each cell represents a potential solution and interacts with its neighbors to update its state based on predefined rules. This interaction models the diffusion of information across the cellular grid, enabling the algorithm to explore the search space effectively. Parallel Cellular Algorithms are particularly suitable for large-scale optimization problems and can be implemented on parallel computing architectures for enhanced performance.

Implementation Steps:

1. Define the Problem: Create a mathematical function to optimize.
2. Initialize Parameters: Set the number of cells, grid size, neighborhood structure, and number of iterations.
3. Initialize Population: Generate an initial population of cells with random positions in the solution space.
4. Evaluate Fitness: Evaluate the fitness of each cell based on the optimization function.
5. Update States: Update the state of each cell based on the states of its neighboring cells and predefined update rules.
6. Iterate: Repeat the evaluation and state updating process for a fixed number of iterations or until convergence criteria are met.
7. Output the Best Solution: Track and output the best solution found during the iterations.

6) Parallel cellular Algorithm and program

Function objective . Function(x):
return sum ($[x_i^2 \text{ for } x_i \text{ in } x]$)

Function get neighbors (grid, i , j , grid-size):

$\text{neighbors}[j, i]$ coordinate - top second position
for $di \in [-1, 0, 1]$

for $dj \in [-1, 0, 1]$ position - right - left

if $|di| > 0$ or $|dj| > 0$ - right-left

$ni = (i + di) \bmod \text{grid-size}$ (fitness) new top

$nj = (j + dj) \bmod \text{grid-size}$ (new) new right

neighbors.append ([ni, nj]) - weighted

return neighbors

Function update state (current, neighbors - 201 x 1000)

for each dimension d in solution

new solution [d] = neighbor-101 [d] + RANDOM

(- perturbation range, perturbation range)

return new - solution.

function parallel - cellular algorithm (grid-size,

max-iter, solution)

initialize grid with random value in [0, 1000]
cells using objective function

initialize fitness, values, cells using objective function

set global best - val = none

set global best - fitness = infinity

set global best - fitness = infinity - best - 1000

```

    for t=1 to max_iter
        create an empty new-grid for updated grid
        for i=0 to grid_size-1
            for j=0 to grid_size-1
                neighbors = get_neighbors(grid, i, j, grid)
                best_neighborhood = grid[i][j]
                best_fitness = fitness[i][j]
                for each n in neighbors
                    if fitness[n] > best_fitness
                        best_fitness = fitness[n]
                        best_neighborhood = n
                new_sol = update_rate(grid[i][j], best_neighborhood)
                return mutation_range = 0.1
                new_fit = objective_function(new_sol)
                if new_fit < fitness[i][j]
                    new_grid[i][j] = new_sol
                    fitness[i][j] = new_fit
                else
                    new_grid[i][j] = grid[i][j]
                if fitness[i][j] < global_best_fitness
                    global_best_sol = grid[i][j]
                    global_best_fitness = fitness[i][j]

```

return global

Applications

- simulation of river flow
- weather simulation
- forest fire model
- road traffic management

$x_{bi} = b_i$

(Training) in

(Testing) &



Retrieves

the global

global

return gridz new-grid
return global-best-sol, global-best-fitness

Applications
simulation of natural phenomena

weather generation

forest fire modelling

road traffic modelling

Extraction of birds

$x_{bi} - \text{birds}$ ($i + 1$), $[1, n_{\text{birds}}]$

$x_{bi} - \text{birds}$ ($i + 1$), $[1, n_{\text{birds}}]$

Extraction of birds

$x_{bi} - \text{birds}$ ($i + 1$), $[1, n_{\text{birds}}]$

Extraction of birds

$x_{bi} - \text{birds}$ ($i + 1$), $[1, n_{\text{birds}}]$

Extraction of birds

$x_{bi} - \text{birds}$ ($i + 1$), $[1, n_{\text{birds}}]$

$x_{bi} - \text{birds}$ ($i + 1$), $[1, n_{\text{birds}}]$

$x_{bi} - \text{birds}$ ($i + 1$), $[1, n_{\text{birds}}]$

$x_{bi} - \text{birds}$ ($i + 1$), $[1, n_{\text{birds}}]$

$x_{bi} - \text{birds}$ ($i + 1$), $[1, n_{\text{birds}}]$

$x_{bi} - \text{birds}$ ($i + 1$), $[1, n_{\text{birds}}]$

Code:

```

import numpy as np

def sphere_function(position):
    """
    Objective function to minimize.
    Sphere Function: f(x) = sum(x_i^2)
    """
    return np.sum(position**2)

def initialize_population(grid_size, solution_dim, lower_bound, upper_bound):
    """
    Initialize the cellular grid with random positions in the solution space.
    Each cell is assigned a random position (vector).
    """
    grid = np.random.uniform(lower_bound, upper_bound, size=(grid_size, grid_size, solution_dim))
    return grid

def evaluate_fitness(grid):
    """
    Evaluate the fitness of each cell in the grid based on the optimization function.
    """
    fitness = np.apply_along_axis(sphere_function, 2, grid)
    return fitness

def get_neighbors(grid, i, j):
    """
    Get the neighboring cells of cell (i, j) in the grid.
    Wraps around the grid edges (toroidal topology).
    """
    neighbors = []
    grid_size = len(grid)
    for di in [-1, 0, 1]:
        for dj in [-1, 0, 1]:
            if di != 0 or dj != 0: # Exclude the cell itself
                ni, nj = (i + di) % grid_size, (j + dj) % grid_size
                neighbors.append(grid[ni, nj])
    return np.array(neighbors)

def update_states(grid, fitness, learning_rate):
    """
    Update the state (position) of each cell based on the neighbors and predefined rules.
    Each cell moves towards the best position in its neighborhood.
    """
    grid_size, _, solution_dim = grid.shape
    new_grid = np.copy(grid)
    for i in range(grid_size):
        for j in range(grid_size):
            neighbors = get_neighbors(grid, i, j)

```

```

neighbor_fitness = np.array([sphere_function(n) for n in neighbors])
best_neighbor = neighbors[np.argmin(neighbor_fitness)]
# Move cell slightly towards the best neighbor's position
new_grid[i, j] += learning_rate * (best_neighbor - grid[i, j])
return new_grid
def parallel_cellular_algorithm(
    grid_size=10, solution_dim=2, lower_bound=-5.0, upper_bound=5.0,
    iterations=100, learning_rate=0.1):
    """
    Main function to execute the Parallel Cellular Algorithm.
    """

    # Step 1: Initialize population
    grid = initialize_population(grid_size, solution_dim, lower_bound, upper_bound)
    best_solution = None
    best_fitness = float('inf')

    for iteration in range(iterations):
        # Step 2: Evaluate fitness
        fitness = evaluate_fitness(grid)

        # Track the best solution
        min_idx = np.unravel_index(np.argmin(fitness), fitness.shape)
        current_best = grid[min_idx]
        current_fitness = fitness[min_idx]
        if current_fitness < best_fitness:
            best_solution = current_best
            best_fitness = current_fitness

        # Step 3: Update states
        grid = update_states(grid, fitness, learning_rate)

        # Print iteration progress
        print(f"Iteration {iteration+1}/{iterations}: Best Fitness = {best_fitness:.5f}")

    # Step 4: Output the best solution
    print("\nOptimization Complete.")
    print(f"Best Solution: {best_solution}")
    print(f"Best Fitness: {best_fitness:.5f}")

# Run the algorithm
if __name__ == "__main__":
    parallel_cellular_algorithm(grid_size=10, solution_dim=2, iterations=10, learning_rate=0.2)

```

Output:

```
⤵ Iteration 1/10: Best Fitness = 0.34823
Iteration 2/10: Best Fitness = 0.19787
Iteration 3/10: Best Fitness = 0.04693
Iteration 4/10: Best Fitness = 0.01438
Iteration 5/10: Best Fitness = 0.01100
Iteration 6/10: Best Fitness = 0.00318
Iteration 7/10: Best Fitness = 0.00318
Iteration 8/10: Best Fitness = 0.00318
Iteration 9/10: Best Fitness = 0.00318
Iteration 10/10: Best Fitness = 0.00318

Optimization Complete.
Best Solution: [-0.05362323  0.01746463]
Best Fitness: 0.00318
```

Program 7

Optimization via Gene Expression Algorithms:

Gene Expression Algorithms (GEA) are inspired by the biological process of gene expression in living organisms. This process involves the translation of genetic information encoded in DNA into functional proteins. In GEA, solutions to optimization problems are encoded in a manner similar to genetic sequences. The algorithm evolves these solutions through selection, crossover, mutation, and gene expression to find optimal or near-optimal solutions. GEA is effective for solving complex optimization problems in various domains, including engineering, data analysis, and machine learning.

Implementation Steps:

1. Define the Problem: Create a mathematical function to optimize.
2. Initialize Parameters: Set the population size, number of genes, mutation rate, crossover rate, and number of generations.
3. Initialize Population: Generate an initial population of random genetic sequences.
4. Evaluate Fitness: Evaluate the fitness of each genetic sequence based on the optimization function.
5. Selection: Select genetic sequences based on their fitness for reproduction.
6. Crossover: Perform crossover between selected sequences to produce offspring.
7. Mutation: Apply mutation to the offspring to introduce variability.
8. Gene Expression: Translate genetic sequences into functional solutions.
9. Iterate: Repeat the selection, crossover, mutation, and gene expression processes for a fixed number of generations or until convergence criteria are met.
10. Output the Best Solution: Track and output the best solution found during the iterations.

2) Optimization via Gene Expression Algorithm

function objective function (sol)

return sum (x^2 for x in sol)

function gene-exp (gene-seq):

return gene-seq # direct mapping

function selection (population, fitness, selection-size)

- selecting -size):

sorted -idx = sorted (range len(fitness))

key = random k fitness

return population [i] for i in sorted -idx
[i:selection -size]

function crossover (parent1, parent2,

crossover -rate):

if random.random() < crossover -rate:

point ← random.randint (1, len (parent1) - 1)

child1 ← parent1 [point :] + parent2 [point :]

child2 ← parent2 [point :] + parent1 [point :]

else

child1, child2 = parent1, parent2

return child1, child2

```

function mutation (individual, mutation_rate, population)
    for i in range (len (population)) = for
        if random () < mutation_rate:
            individual[i] = random.uniform (-1, 1)
    return individual

function gene_exp (edge (population) else,
    gene, len,
    mutation_rate, population)
    population [random.uniform (-1, 1)] = population
    for i in range (gene):
        for j in range (population_size):
            fitness = objective - function (gene, edge)
            if fitness > best_fit:
                best_fit = fitness
                selected_popl = selection (population, fitness)
    for gen in range (1, max_gen + 1):
        for gen in range (1, max_gen + 1):
            for gen in range (1, max_gen + 1):

```

offspring = [] , len(offspring) = len(selected_population)

for i in range(0, len(selected_population)):

parent 1 = selected_population[i]

parent 2 = selected_population[cut_index : len(selected_population)]

child1, child2 = crossover(parent1, parent2, crossover_rate)

offspring.append(child1)

offspring.append(child2)

for i in range(len(offspring)):

offspring[i] = mutation(offspring[i], mutation_rate)

population = selected_population + offspring

Fitness = []

for int i in population:

for i in range(len(population)):

if fitness[i] < best_fitness:

best_fitness = population[i]

best_fitness = fitness[i]

return best_fitness, best_fitness


```

# Step 1: Initialize Population
population = initialize_population(pop_size, num_genes, lower_bound, upper_bound)

# Step 2: Iterate for a fixed number of generations
best_solution = None
best_fitness = float('inf')

for generation in range(num_generations):
    # Step 3: Evaluate fitness
    fitness = evaluate_fitness(population)

    # Step 4: Track the best solution
    min_fitness_idx = np.argmin(fitness)
    if fitness[min_fitness_idx] < best_fitness:
        best_fitness = fitness[min_fitness_idx]
        best_solution = population[min_fitness_idx]

    # Step 5: Selection
    selected_population = tournament_selection(population, fitness)

    # Step 6: Crossover and Mutation
    new_population = []
    for i in range(0, pop_size, 2):
        parent1 = selected_population[i]
        parent2 = selected_population[i+1] if i+1 < pop_size else selected_population[0] # Ensuring even number of parents

        # Perform crossover
        if np.random.rand() < crossover_rate:
            child1, child2 = crossover(parent1, parent2)
        else:
            child1, child2 = parent1, parent2 # No crossover, just pass parents

        # Apply mutation
        child1 = mutate(child1, mutation_rate, lower_bound, upper_bound)
        child2 = mutate(child2, mutation_rate, lower_bound, upper_bound)

        # Add the children to the new population
        new_population.extend([child1, child2])

    # Update population with new generation
    population = np.array(new_population[:pop_size]) # Ensure population size remains constant

return best_solution, best_fitness

# Set parameters
pop_size = 100          # Population size
num_genes = 10           # Number of genes (dimensions of the problem)
lower_bound = -5.12      # Lower bound of the search space

```

```
upper_bound = 5.12          # Upper bound of the search space
mutation_rate = 0.1         # Mutation rate
crossover_rate = 0.8        # Crossover rate
num_generations = 500       # Number of generations

# Run the Gene Expression Algorithm
best_solution, best_fitness = gene_expression_algorithm(pop_size, num_genes, lower_bound,
upper_bound, mutation_rate, crossover_rate, num_generations)

# Output the results
print("Best Solution:", best_solution)
print("Best Fitness:", best_fitness)
```

Output:

```
→ Best Solution: [ 0.01956405  0.00271381 -0.00243719  0.00141388 -0.02586832  0.00105932
  0.01769152 -1.03340239 -0.02943199 -0.04696745]
Best Fitness: 2.166804134722355
```