

Assignment 3

Due Tuesday, November 7th, before class.

Prof. Dr. Sven Behnke Friedrich-Hirzebruch-Allee 8

- 3.1) Let a robot be equipped with wheel encoders and on-board software that transforms the physical measuring data into time-discrete odometry measurements $\langle \hat{\delta}_{rot1}, \hat{\delta}_{trans}, \hat{\delta}_{rot2} \rangle$.

Let the robot start at pose $\langle x, y, \theta \rangle = \langle 3m, -2m, -30^\circ \rangle$ and obtain the following subsequent odometry measurements:

| Motion 1 | Motion 2 |
|-------------------------------------|-------------------------------------|
| $\hat{\delta}_{rot1}^1 = -20^\circ$ | $\hat{\delta}_{rot1}^2 = 20^\circ$ |
| $\hat{\delta}_{trans}^1 = 10m$ | $\hat{\delta}_{trans}^2 = 3m$ |
| $\hat{\delta}_{rot2}^1 = 10^\circ$ | $\hat{\delta}_{rot2}^2 = -30^\circ$ |

Calculate the resulting pose of the robot, assuming exact measurements!

5 points

- 3.2) How would your pose estimate for the Motion 1 look like under the following simple error model?

$$\begin{aligned}\hat{\delta}_{rot1} &= \delta_{rot1} \pm \varepsilon_{rot1}, & \varepsilon_{rot1} &= 10^\circ \\ \hat{\delta}_{trans} &= \delta_{trans} \pm \varepsilon_{trans}, & \varepsilon_{trans} &= 0.5m \\ \hat{\delta}_{rot2} &= \delta_{rot2} \pm \varepsilon_{rot2}, & \varepsilon_{rot2} &= 5^\circ\end{aligned}$$

Please draw the movements for noise $+\varepsilon_{movement}$ and $-\varepsilon_{movement}$ and the resulting eight pose estimates into one diagram!

5 points

- 3.3) Visualize the likelihood of positions (x, y) after
- Motion 1,
 - Motion 1 followed by Motion 2,
 - Motion 1 followed by Motion 2, followed by Motion 1
- with the error model from 3.2) by computing the likelihoods on a grid (x, y, θ) and marginalizing out the heading direction θ !

5 points

- 3.4) Initialize 100 samples at $\langle x, y, \theta \rangle = \langle 3m, 2m, -30^\circ \rangle$.

Show the (x, y) positions of the samples after

- Motion 1,
 - Motion 1 followed by Motion 2,
 - Motion 1 followed by Motion 2, followed by Motion 1
- by applying a sampling-based motion model with parameters from 3.2)! Compare your results to 3.3)!

5 points