

# DATSAW: Dynamically Adjusting Tool Selection with Federated Average Weighing

## Introduction

DATSAW optimizes tool selection based on image quality using a federated averaging approach. This document details the mathematical steps involved and the relationships between different variables.

## Step 1: Calculate Image Quality

For each image, the image quality, represented as Epsilon ( $\epsilon$ ), is calculated:

$$\epsilon = \text{Image Quality Metric}$$

## Step 2: Define Tools

We define a bag of  $k$  tools, denoted as  $T = \{t_1, t_2, \dots, t_k\}$ , arranged in ascending order based on a factor  $\alpha$ :

$$\alpha = \text{cost} \times \text{performance}$$

The tools are sorted such that:

$$t_1 < t_2 < \dots < t_k \quad (\text{where } \alpha(t_i) \text{ is increasing})$$

## Step 3: Calculate Window Parameters

Two additional factors,  $\gamma$  and  $\delta$ , are calculated as:

$$\gamma, \delta = \left\lfloor \frac{1}{\epsilon} \right\rfloor$$

These factors represent the start and end indices of the selection window.

## Step 4: Define Beta

Let  $\beta$  represent the subset of tools selected between  $\alpha$  and  $\gamma$ , defined as:

$$\beta = \{t_i \mid \alpha < i < \gamma\}$$

where  $t_i$  are the tools within the specified range.

## Step 5: Relationship Between Beta and Epsilon

The relationship between  $\beta$  and  $\epsilon$  is significant because  $\epsilon$  influences the selection window:

- A higher value of  $\epsilon$  results in a smaller  $\gamma$  and  $\delta$ , thus reducing the range of selected tools, which may limit the elements in  $\beta$ .
- Conversely, a lower value of  $\epsilon$  expands the selection window, potentially increasing the size of  $\beta$ .

This relationship emphasizes how image quality affects the diversity of tools available for federated averaging.

## Step 6: Assign Priorities for Federated Averaging

The tools in the selected window are assigned priorities:

- First tool ( $t_\gamma$ ): Priority = 0.2
- Last tool ( $t_\delta$ ): Priority = 0.2
- Middle tools ( $t_i$  for  $\gamma < i < \delta$ ): Priority = 0.4

## Step 7: Federated Averaging

The final output  $z$  is computed using federated averaging:

$$z = \frac{\sum_{i=\gamma}^{\delta} p_i \cdot t_i}{\sum_{i=\gamma}^{\delta} p_i}$$

where  $p_i$  is the priority assigned to tool  $t_i$ .

## Conclusion

The output  $z$  is returned to the user after applying the federated averaging method, balancing contributions from different tools based on their assigned priorities and the influence of image quality through  $\epsilon$ .