

B.Tech 2nd Semester Mid-Term Examination 2021

Subject Name: Engineering Mathematics – II

Subject Code: UAD12B10, DTPH12B12

Full Marks: 20

Answer Script To Be Submitted Through Email: nita.ma.btech.j1@gmail.com

Time: 1 Hour

Symbols Used Here Have Their Usual Meanings

Choose the correct option from the following:

[10 × 2 = 20 Marks]

1. If $B(n, 2) = \frac{1}{6}$ and n is a positive integer, then the value of n is

- [illegible]

- a) $0, \frac{9}{2}$ b) $0, \frac{7}{2}$
c) $0, -\frac{9}{2}$ d) None of these

2. If A is the region bounded by the parabolas $y^2 = 4x$, $x^2 = 4y$ then $\iint_A y \, dx \, dy$ is equal to

- a) $\frac{48}{5}$ b) $\frac{36}{5}$
c) $\frac{32}{5}$ d) None of these

- 7.** Let $A = \begin{pmatrix} 1 & 2 & 3 \\ 1 & 0 & 1 \\ 3 & -1 & 5 \end{pmatrix}$, $B = \begin{pmatrix} 1 & 0 & 1 \\ 1 & 1 & 2 \\ 0 & -1 & 3 \end{pmatrix}$ and rank of A is 3. Then rank of AB is
- a) 0 b) 1
c) 2 d) 3

3. The value of $\int_0^\infty \int_x^\infty \frac{e^{-y}}{y} dx dy$ changing the order of integration is

- a) 0 b) $\frac{3}{4}$
c) 1 d) None of these

8. The value of $X = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$, when $\begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 3 & 1 & 2 \end{bmatrix} X = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$ is

- a) $X = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$ b) $X = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$
c) $X = \begin{bmatrix} 1 \\ 0 \\ -1 \end{bmatrix}$ d) $X = \begin{bmatrix} 2 \\ -1 \\ 1 \end{bmatrix}$

4. The value of the integral $\iint r^3 dr d\theta$ over the area included between the circles $r = 2\sin\theta$ and $r = 4\sin\theta$, is

- a) $\frac{28}{9}\pi$ b) $\frac{45}{2}\pi$
c) $\frac{22}{7}\pi$ d) π

5. The definite integral $\int_a^b f(x)dx$ is said to be improper integral of 2nd kind if

- a) $[a,b]$ is of finite length but $f(x)$ has one or more points of infinite discontinuity
- b) The interval of integration $[a,b]$ is unbounded or $f(x)$ is not bounded on $[a,b]$
- c) $[a,b]$ is of finite length and $f(x)$ is bounded in the interval $[a,b]$
- d) None of these

9. For which of the following value of x, the rank of the matrix $\begin{bmatrix} 2 & 1 & 4 \\ 1 & x & 2 \\ 4 & 0 & x+2 \end{bmatrix}$ will be 2?
- a) $x = 6$ b) $x \neq 6$
- c) $x = 2$ d) None of these

10. The system of equations $2x + 3y + 5z = 9$, $7x + 3y - 2z = 8$, $2x + 3y + \lambda z = \mu$ has infinite number of solution for

- a) $\lambda = 9$
c) $\lambda = 5, \mu = \text{any value}$
- b) $\lambda = 5, \mu = 9$
d) None of these

6. The value of k for which the system of equations $x + ky + 3z = 0, 4x + 3y + kz = 0, 2x + y + 2z = 0$ is consistent is/are

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