

MAE 158 Drag Calculator

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Profile Drag Coeff

Setup

```
hp_aircraft = 1;
T = 400;
%P = 1; % via Table A.2
R = 1716;
rho = 0.0008754;
speedSound = sqrt(1.4*R*T);
V = [230:1:880]; %765;
M = V/speedSound; % Mach Number
Sref = 1000;

%% Characteristic Lengths
MACexpW = 0;
MACexpH = 0;
MACexpV = 0;
%Lc = [MACexpW, MACexpH, MACexpV, 16.2, 16.8];
Lc = []; %Characteristic Lengths

%% Ratios
Lf = 119;
Df = 11;
ratios = [0.12, 0.09, 0.09, 0.06, Lf/Df, 5] % Thickness and Fineness
```

```
ratios = 1x6
    0.1200    0.0900    0.0900    0.0600   10.8182    5.0000
```

```
sigma = [0.2, 0.35, 0.8, 1]; % Taper
%% Sexp
Sexpw = 0; % Defined Later on
Sexp = [Sexpw, 261, 161];
%% Swet
Swet = [0, 0, 0, 117, 0, 455];
```

Component 1 Wing

```
bW = 93.2; % Span
tcW = 0.18;
sweepangleW = 28; % Sweep Angle
sigmaW = 0.2; % Taper Ratio: cT/cR
CRW = 17.8; % Root Chord
Coverage_wing = .17; % Percent Covered
Rfuse = 11/2;

% Getting Swet %
SexpW = (1-Coverage_wing)*Sref;
```

```

SwetW = SWET(SexpW);

% Getting Skin Friction Coefficient %
CTW = sigmaW * CRW;
CRexp_wing = CREXP(CRW, CTW, Rfuse, bW);
MACexpW = MAC(CRexp_wing,CTW);
Lc = [Lc, MACexpW];

RNw = ReynoldsNumber(V, MACexpW);
Cf_w = CF(RNw);

% Getting Form Factor %
Kwing = Kairfoil(tcW, M, sweepangleW);

% Calculating f and adding to array %
fwing = F(Kwing, Cf_w, SwetW);

```

Horizontal Tail

```

SexpH = 261;
tcH = 0.09;
sweepangleH = 31.6;           % Sweep Angle
sigmaH = 0.35;               % Wing Taper Ratio
CRH = 11.1;                  % Root Chord

% Getting Swet %
SwetH = SWET(SexpH);

% Getting Skin Friction Coefficient %
CTH = sigmaH * CRH;
MACexpH = MAC(CRH,CTH);
Lc = [Lc, MACexpH];

RNh = ReynoldsNumber(V, MACexpH);
Cf_h = CF(RNh);

% Getting Form Factor %
Khoriztail = Kairfoil(tcH, M, sweepangleH);

% Calculating f and adding to array %
fhoriztail = F(Khoriztail, Cf_h, SwetH);

```

Vertical Tail

```

SexpV = 161;
tcV = 0.09;
sweepangleV = 43.5;          % Sweep Angle
sigmaV = 0.8;                % Wing Taper Ratio
CRV = 15.5;                  % Root Chord

% Getting Swet %
SwetV = SWET(SexpV);

```

```

% Getting Skin Friction Coefficient %
CTV = sigmaV * CRV;
MACexpV = MAC(CRV,CTV);
Lc = [Lc, MACexpV];

RNv = ReynoldsNumber(V, MACexpV);
Cf_v = CF(RNv);

% Getting Form Factor %
Kverttail = Kairfoil(tcV, M, sweepangleV);

% Calculating f and adding to array %
fverttail = F(Kverttail, Cf_v, SwetV);

```

Pylons

```

SwetP = 117; % Wetted Area
tcP = 0.06;
sweepangleP = 0; % Sweep Angle
sigmaP = 1; % Taper Ratio: cT/cR
chordP = 16.2; % Chord

% Getting Skin Friction Coefficient %
Lc = [Lc, chordP];
RNp = ReynoldsNumber(V, chordP);
Cf_p = CF(RNp);

% Getting Form Factor %
Kpylon = Kairfoil(tcP, M, sweepangleP);

% Calculating f and adding to array %
fpylon = F(Kpylon, Cf_p, SwetP);

```

Component 2: Fuselage

```

Lf = 105;
Df = 11;

% Calculating Swet %
SwetF = 0.8 * pi * Df * Lf;

% Getting Skin Friction Coefficient %
RNf = ReynoldsNumber(V, Lf);
Lc = [Lc, Lf];
Cf_f = CF(RNf);

% Getting Form Factor %
ratioF = Lf/Df;
Kfuse = KFR(ratioF); % Via Digitized Figure 11.4

% Calculating f and adding to array %
ffuselage = F(Kfuse, Cf_f, SwetF);

```

Nacelles

```
% Swet %  
SwetN = 455;  
  
% Getting Skin Friction Coefficient %  
Ln = 16.8;  
Lc = [Lc, Ln];  
RNn = ReynoldsNumber(V, 16.8);  
Cf_n = CF(RNn);  
  
% Getting Form Factor %  
ratioN = 5;  
Knacelle = KFR(ratioN); % Via Digitized Figure 11.4  
  
% Calculating f and adding to array %  
fnacelle = F(Knacelle, Cf_n, SwetN);
```

Profile Drag Coeff Calculation

```
ftotal = fwing + fhoriztail + fverttail + fpylon + ffuselage + fnacelle;  
CDP_total = 1.10 * ftotal./Sref;
```

Induced Drag Coeff

```
% Getting CL %  
W = 98000; % Aircraft Weight  
q = 0.5 * rho * (V.^2); % Dynamic Pressure  
CL = W ./ (q * Sref); % Coeff of Lift  
% Getting Aspect Ratio %  
ARw = (bW^2)/Sref;  
% Getting CDi %  
efactor = oswaldEff(ARw, CDP_total); % Oswald Efficiency Factor  
e = 1; % Ignore  
CDi = (CL.^2) ./ ((pi * ARw) .* efactor); % Coeff of Induced Drag
```

Total Drag & Lift/Drag Ratio

```
ProfileDrag = CDP_total .* q .* Sref;  
InducedDrag = CDi .* q .* Sref;  
CDtotal = CDP_total + CDi;  
TotalDrag = CDtotal .* q .* Sref;  
L = W;  
LiftToDrag = L ./ TotalDrag;  
[LiftToDragMax, index] = max(LiftToDrag)
```

```
LiftToDragMax = 16.9434  
index = 370
```

```
max(LiftToDrag)
```

```
ans = 16.9434
```

```
Voptimum = V(index)
```

V = 765 ft/s Information

This section is used to verify the software to the hand calculations

```

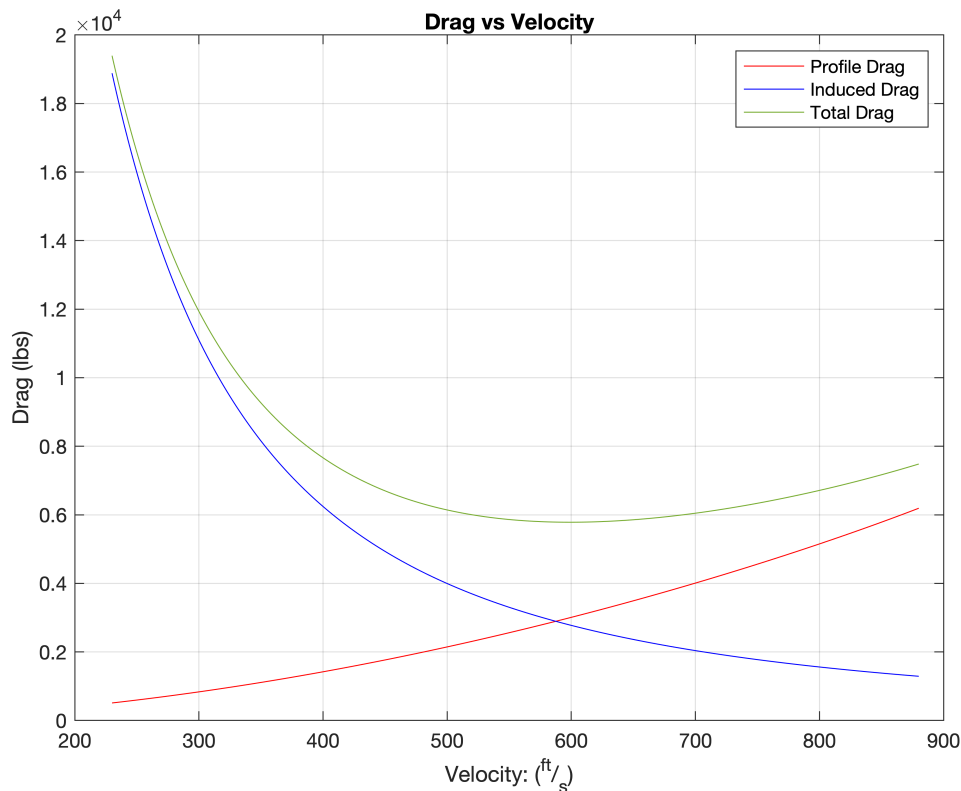
indexV765 = find(V==765);
%{
M765 = M(indexV765);
%   Profile Calculation__
%   Wing Data
ChordVals = [CRW, CTW, CRexp_wing, MACexpW];
RNw(indexV765);
Cf_w(indexV765);
%   Horizontal Tail Data
ChordVals = [CRH, CTH, MACexpH];
RNh(indexV765);
%   Vertical Tail Data
ChordVals = [CRV, CTV, MACexpV];
RNv(indexV765);
%   Pylons
RNp(indexV765);
%   Nacelles
RNn(indexV765);
%   Fuselage
RNf(indexV765);
SwetF;
%   Profile Total
CDP_total(indexV765);
ProfileDrag(indexV765);
%   Induced Calculation__
%   CL
q(indexV765);
CL(indexV765);
ARw;
efactor(indexV765);
CDi(indexV765);
%   Total Calculations__
CDtotal(indexV765);
TotalDrag(indexV765);
LiftToDrag(indexV765);
%}
%   Table Info
ComponentName = ["#", "Component", "Leff", "Re", "Cf", "K", "Swet", "CDP"];
WingValues = ["Wing", MACexpW, RNw(indexV765), Cf_w(indexV765), Kwing(indexV765), SwetF];
FuselageValues = ["Fuselage", Lf, RNf(indexV765), Cf_f(indexV765), Kfuse, SwetF, ffuse];
HTailValues = ["H. Tail", MACexpH, RNh(indexV765), Cf_h(indexV765), Khoriztail(indexV765), SwetH];
VTailValues = ["V. Tail", MACexpV, RNv(indexV765), Cf_v(indexV765), Kverttail(indexV765), SwetV];
PylonValues = ["Pylon", chordP, RNp(indexV765), Cf_p(indexV765), Kpylon(indexV765), SwetP];
NacelleValues = ["Nacelles", Ln, RNn(indexV765), Cf_n(indexV765), Knacelle, SwetN, fna];
testTable = [WingValues; FuselageValues; HTailValues; VTailValues; PylonValues; NacelleValues];
FinalTable = array2table(testTable);
FinalTable.Properties.VariableNames(1:7) = {'Component', 'Leff', 'Re', 'Cf', 'K', 'Swet', 'CDP'};

```

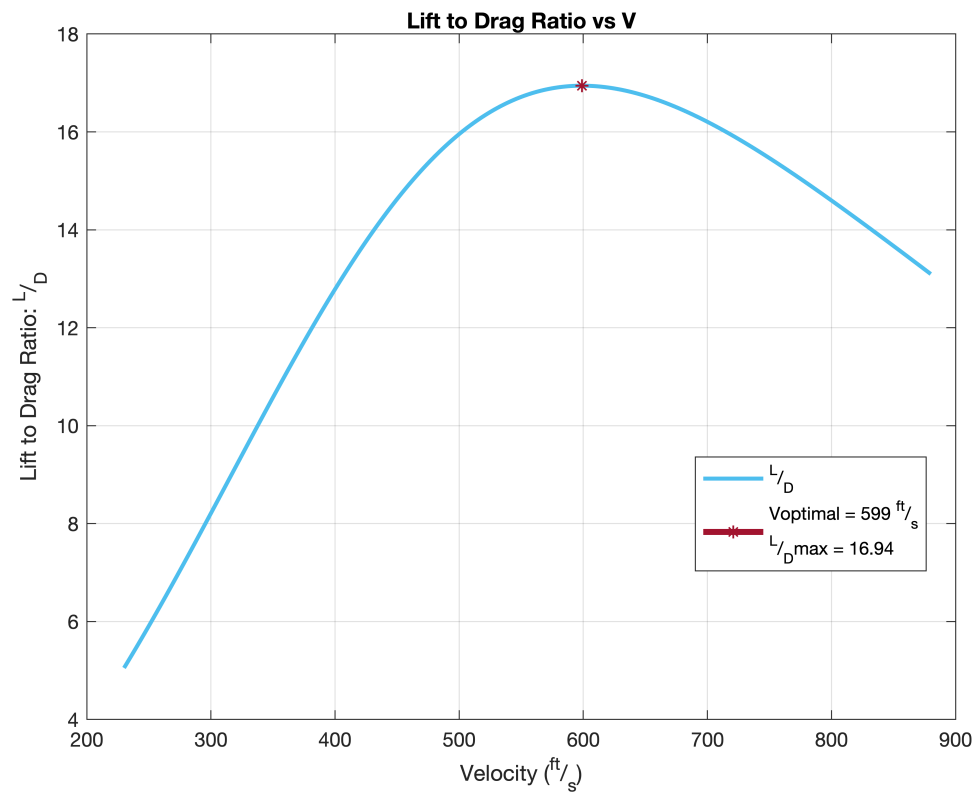
```
writetable(FinalTable, 'FinalTable.csv'); % Generate CSV Table
```

Plots

```
plot(V, ProfileDrag, 'r', V, InducedDrag, 'b')
hold on;
plot(V, TotalDrag, Color=[0.4660 0.6740 0.1880])
grid on
title("Drag vs Velocity")
ylabel("Drag (lbs)")
xlabel("Velocity: (^{ft}/_{s})")
legend("Profile Drag", "Induced Drag", "Total Drag")
hold off
```



```
plot(V, LiftToDrag, Color=[0.3010 0.7450 0.9330], LineWidth=2)
hold on
%plot(Voptimum, LiftToDragMax, 'Color', 'r', 'Marker', 'o', 'LineWidth', 1)
plot(Voptimum, LiftToDragMax, Color=[0.6350 0.0780 0.1840], Marker="*", LineWidth=3);
grid on
title("Lift to Drag Ratio vs V")
ylabel("Lift to Drag Ratio: ^{L}/_{D}")
xlabel("Velocity (^{ft}/_{s})")
legend("^{L}/_{D}", "Voptimal = 599 ^{ft}/_{s}" + newline + " ^{L}/_{D}max = 16.94", Location='best')
hold off;
```



Functions

Reynolds Number Function

```
function RN = ReynoldsNumber(Velocity, characteristicLength)
    mu = 3.025E-7;
    rho = 0.0008754;
    V = Velocity;
    Lc = characteristicLength;
    RN = (rho * V * Lc)/mu;
end
```

Swet Function

```
function Swet = SWET(Sexp)
    Swet = 2 * 1.02 * Sexp;
end
```

MAC Function

```
function cbar = MAC(cR, cT)
    cbar = (2/3) * (cR + cT - ((cR*cT)/(cR+cT)));
end
```

CR Exposed Function

```
function crexp = CREXP(cR, cT, y, b)
    crexp = cR - ((cR - cT)*(2*(y/b)));
```

```
end
```

Skin Friction Coefficient

```
function Cf = CF(RN)
    Cf = 0.455 ./ ((log10(RN)).^2.58);
end
```

Form Factor for Airfoils

```
function K = Kairfoil(tc, Mo, sweepAngle)
    numTerm = (2-Mo.^2) * cosd(sweepAngle);
    denTerm = sqrt(1-((Mo.^2)*cosd(sweepAngle)));
    Z = numTerm./denTerm;
    K = 1 + (Z .* tc) + (100*tc^4);
end
```

Form Factor via Fineness Ratio

```
function K = KFR(LbyD)
    K = 1.991*LbyD^-1.024+0.9084;
    % General model Power2:
    % Coefficients (with 95% confidence bounds):
    %   a =      1.991  (1.882, 2.101)
    %   b =     -1.024  (-1.091, -0.9582)
    %   c =      0.9084 (0.8888, 0.9279)
end
```

F Function

```
function f = F(K, Cf, Swet)
    f = K .* Cf * Swet;
end
```

Oswald Efficiency Function

```
function e = oswaldEff(ARW, CDP)
    e = [];
    for N = 1:length(CDP)
        CDProunded = round(CDP(N),2); % Skips Interpolation
        switch CDProunded
            case .01
                e = [e, .000114*ARW^2 - .01085*ARW + .9659]; %
            case .015
                e = [e, (2.5e-05)*ARW^3 - .0002244*ARW^2 - .01422*ARW + .9649]; %
            case .02
                e = [e, .000364*ARW^2 - .02149*ARW + .9641]; %
            case .025
                e = [e, (-6.849e-06)*ARW^3 + .0006443*ARW^2 - .0269*ARW + .9614]; %
        end
    end
end

%% Digitized Curved Results for Oswald Efficiency Factor %%
%{
```



```

CDP = .01
f(x) = p1*x^2 + p2*x + p3
Coefficients (with 95% confidence bounds):
    p1 =    0.000114  (0.000103, 0.0001251)
    p2 =   -0.01085  (-0.01099, -0.01071)
    p3 =    0.9659   (0.9655, 0.9663)
%}
%{

CDP = .015
f(x) = p1*x^3 + p2*x^2 + p3*x + p4
Coefficients (with 95% confidence bounds):
    p1 =    2.5e-05  (1.971e-05, 3.03e-05)
    p2 =  -0.0002244 (-0.0003207, -0.0001281)
    p3 =   -0.01422  (-0.01471, -0.01373)
    p4 =    0.9649   (0.9642, 0.9655)
%}
%{

CDP = .02
f(x) = p1*x^2 + p2*x + p3
Coefficients (with 95% confidence bounds):
    p1 =    0.000364  (0.0003456, 0.0003824)
    p2 =   -0.02149  (-0.02171, -0.02126)
    p3 =    0.9641   (0.9635, 0.9647)
%}
%{

CDP = .025
f(x) = p1*x^3 + p2*x^2 + p3*x + p4
Coefficients (with 95% confidence bounds):
    p1 =  -6.849e-06  (-1.049e-05, -3.207e-06)
    p2 =    0.0006443 (0.0005786, 0.0007101)
    p3 =   -0.0269   (-0.02723, -0.02656)
    p4 =    0.9614   (0.961, 0.9619)
%}

```