

System Modeling, (Given):

- $\dot{x}_1(t) = v(t) \cos(\theta(t))$
- $\dot{y}_1(t) = v(t) \sin(\theta(t))$
- $\dot{\theta}(t) = \frac{v(t)}{B} \tan(\gamma(t))$
- B uncertain to $\pm 10\%$, r uncertain to $\pm 5\%$
- Modeling process noise as additive, and using a state vector of length 5, after discretizing using Forward Euler method our equations are,

$$S_k = \begin{bmatrix} x_k \\ y_k \\ \theta_k \\ B_k \\ r_k \end{bmatrix} = \begin{bmatrix} x_{k-1} + v_{k-1} \cos(\theta_{k-1}) \Delta t \\ y_{k-1} + v_{k-1} \sin(\theta_{k-1}) \Delta t \\ \theta_{k-1} + v_{k-1} \tan(\gamma_{k-1}) \Delta t \\ B_{k-1} \\ r_{k-1} \end{bmatrix} + \begin{bmatrix} v_1 \\ v_2 \\ v_3 \\ v_4 \\ v_5 \end{bmatrix}_{k-1}$$

Where numeric values for process noise vector v are described in the report.

- For measurement modeling, $w(\cdot)$ was considered additive and used with the given discrete measurement model.

$$\therefore Z(k) = \begin{bmatrix} x(t_k) + \frac{1}{2} B \cos(\theta(t_k)) \\ y(t_k) + \frac{1}{2} B \sin(\theta(t_k)) \end{bmatrix} + \begin{bmatrix} w_1 \\ w_2 \end{bmatrix}_k$$