

Advanced Digital Signal Processing (ADSP) Lab - Python

Lab Manual

Course Code: EEE G613

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▼ Experiment No. - 4

1. Signal Modeling using Pade' approximation

Design a linear lowpass filter having cutoff frequency of $\pi/2$. The frequency response of the *ideal lowpass filter* is given below

$$I(e^{j\omega}) = \begin{cases} e^{-jn_d\omega} & ; |\omega| < \frac{\pi}{2} \\ 0 & ; otherwise \end{cases}$$

where n_d is the filter delay. Take $n_d = 5$.

- a) find $i(n)$. Mathematically obtain the expression for $i(n)$ in your observation book.
- b) Design a filter with $p=0$ and $q=10$ to match $i(n)$ exactly. Plot the impulse response.
- c) Calculate the error between $i(n)$ and the filter's impulse response for a signal range of 20 samples.
- d) Consider another filter design with $p=5$ and $q=5$ to match $i(n)$. Plot the filter response.
- e) Calculate the error between $i(n)$ and ARMA filter impulse response for a signal range of 20 samples
- f) compare the filter coefficients you have calculated for b) and d) using 'pade' function given below.

▼ Python Code- Part (a),(b) & (c):

```

#import libraries
import numpy as np
from scipy.signal import lfilter
import matplotlib.pyplot as plt
from scipy import signal

#for p=0 and q=10
q = 10
n = range(20)
nd = 5
temp = 0
x = np.zeros(len(n))
for temp in n:
    x[temp] = (np.sin(((temp + 1) - nd) * np.pi / 2)) / ((temp + 1) - nd)

x[4] = 0.5

#plotting
plt.subplot(3, 1, 1)
plt.title('I(n)')
plt.stem(n, x)
x = x[:, np.newaxis]
b = x[0:11]
print("\nNumerator coefficients: \n")
print(b)
a = np.zeros(len(b))
a[0] = 1
print("\nDenominator Coefficients: \n")
print(a)
# Transferring the obtained coefficients to a transfer function
system = signal.TransferFunction(b, 1, dt=0.1)
# Printing the system representation
print("Transfer function: \n")
print(system)
system1 = signal.dlti(b, a)
# Computing the impulse response
t, h = signal.dimpulse(system)
h = h[0].flatten()
h = h[0:100]
# Plotting the impulse response
plt.subplot(3, 1, 2)
plt.title('Impulse response')
plt.plot(t, h)
# Calculating the error
e = x.flatten() - h[0:20]
# Displaying the error
print("\nError:\n")
print(e)
# Plotting the error
plt.subplot(3, 1, 3)
plt.title('Error response')
plt.stem(n, e)
plt.show()

```


▼ *Python Code- Part (d),(e) & (f):*

```

#for p=5 and q=5
p = 5
q = 5
n = range(20)
nd = 5
temp = 0
x = np.zeros(len(n))
for temp in n:
    x[temp] = (np.sin(((temp + 1) - nd) * np.pi / 2)) / ((temp + 1) - nd

x[4] = 0.5
plt.subplot(3, 1, 1)
plt.title('I(n)')
plt.stem(n, x)
x = x[:, np.newaxis]
if p + q >= len(x):
    raise ValueError("Model order too large")

X = []
N = len(x) + 2 * p - 1
xpad = np.concatenate((np.zeros((p, 1)), x, np.zeros((p, 1))))
for i in range(1, p + 2):
    X.append(xpad[p - i + 1 : N - i + 1])

X = np.column_stack(X)
Xq = X[q + 1 : q + p + 1, 1:p + 1]
Xqq = X[q + 1 : p + q + 1, 0]
Xqq = np.reshape(Xqq, (len(Xqq), 1))
a = np.matmul(np.linalg.pinv(Xqq), Xq)
a = np.array(a)
a = np.append(1, a)
print("\nDenominator Coeffecients\n")
print(a)
b = np.matmul(X[0:q + 1, 0:p + 1], a)
b = np.append(0, b)
print("\nNumerator Coeffecients\n")
print(b)

# Transferring the obtained coefficients to a transfer function
system = signal.TransferFunction(b, a, dt=0.1)
# Printing the system representation
print("\nTransfer function\n")
print(system)
system1 = signal.dlti(b, a)
# Computing the impulse response
t, h = signal.dimpulse(system)
h = h[0].flatten()
# Plotting the impulse response
plt.subplot(3, 1, 2)
plt.title('Impulse response')
plt.plot(t, h)
print(h[1:20])
# Calculating the error
e = x.flatten() - h[0:20]
# Displaying the error

```

```
print("\nError:\n")
print(e)
# Plotting the error
plt.subplot(3, 1, 3)
plt.title('Error response')
plt.stem(n, e)
```
<ipython-input-19-c4119a8e0444>:9: RuntimeWarning: invalid value encountered in
x[temp] = (np.sin(((temp + 1) - nd) * np.pi / 2)) / ((temp + 1) - nd)

Denominator Coeffecients

[1.00000000e+00 5.71205034e-16 -2.64705882e+00 -1.10294118e+00
 -8.82352941e-01 6.61764706e-01]

Numerator Coeffecients

[0.00000000e+00 -6.12323400e-17 -3.33333333e-01 3.29162678e-17
 1.88235294e+00 8.67647059e-01 -1.35294118e+00]

Transfer function

TransferFunctionDiscrete(
array([-3.3333333e-01, 3.29162678e-17, 1.88235294e+00, 8.67647059e-01,
 -1.35294118e+00]),
array([1.00000000e+00, 5.71205034e-16, -2.64705882e+00, -1.10294118e+00,
 -8.82352941e-01, 6.61764706e-01]),
```