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Class & Division	S.E. COMPS A (BATCH B)
Experiment No.	2

**<u>Aim:</u>** Experiment on finding the running time of an algorithm(merge sort and quick sort)

## **Theory:**

#### Merge sort

Merge sort is a sorting algorithm that works by dividing an array into smaller subarrays, sorting each subarray, and then merging the sorted subarrays back together to form the final sorted array. In simple terms, we can say that the process of merge sort is to divide the array into two halves, sort each half, and then merge the sorted halves back together. This process is repeated until the entire array is sorted. One thing that you might wonder is what is the specialty of this algorithm. We already have a number of sorting algorithms then why do we need this algorithm? One of the main advantages of merge sort is that it has a time complexity of O(n log n), which means it can sort large arrays relatively quickly. It is also a stable sort, which means that the order of elements with equal values is preserved during the sort.

#### Quick sort

Like <u>Merge Sort</u>, Quick sort is a <u>Divide and Conquer algorithm</u>. It picks an element as a pivot and partitions the given array around the picked pivot. There are many different versions of quickSort that pick pivot in different ways.

- Always pick the first element as a pivot.
- Always pick the last element as a pivot (implemented below)
- Pick a random element as a pivot.
- Pick median as the pivot.

The key process in quickSort is a partition(). The target of partitions is, given an array and an element x of an array as the pivot, put x at its correct position in a sorted array and put all smaller elements (smaller than x) before x, and put all greater elements (greater than x) after x. All this should be done in linear time.

## **Algorithm:**

### Merge sort:

- 1. If the array "b" has only one element, return the array as it is already sorted.
- 2. Calculate the middle index of the array "b" using "mid = (beg + end) / 2".
- 3. Call the "mergesort" function recursively for the first half of the array "a[beg, mid]"
- 4. Call the "mergesort" function recursively for the second half of the array "a[mid+1, end]"
- 5. Call the "merge" function to merge the two sorted arrays obtained from the previous steps back into the original array "b".
- 6. The "merge" function takes in two arrays, the first half and the second half, and sorts the elements in both arrays and stores them back into the original array "b".
- 7. Repeat the above steps until all elements of the array "b" are sorted in ascending order.

## Quick sort:

- 1. If the array "b" has zero or one element, return the array as it is already sorted.
- 2. Choose the first element of the array "b" as the pivot.
- 3. Initialize two variables "low" and "high" to keep track of the elements to be swapped. Set "low" to the first position and "high" to the last position in the array "b."
- 4. While "low" is less than "high," repeat the following steps: a. Increment "low" while the element at

- "low" is less than or equal to the pivot. b. Decrement "high" while the element at "high" is greater than the pivot. c. If "low" is less than "high", swap the elements at "low" and "high".
- 5. Swap the pivot with the element at "high" to place the pivot in its correct position in the sorted array.
- 6. Call the quick sort algorithm recursively for the two sub-arrays "b[beg, high-1]" and "b[high+1, end]".
- 7. Repeat the above steps until all elements of the array "b" are sorted in ascending order

## Code:

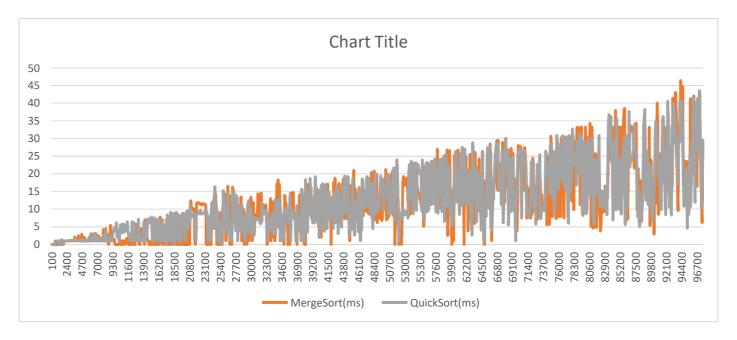
```
#include <bits/stdc++.h>
using namespace std;
void merge(int arr[], int l, int mid, int r)
    int n1=mid-l+1;
    int a[n1],b[n2];
    for(int i=0;i<n1;i++)</pre>
    a[i]=arr[l+i];
    for(int j=0;j<n2;j++)</pre>
    b[j]=arr[mid+1+j];
    int i=0,j=0,ind=1;
    while(i<n1 && j<n2){
        if(a[i]<=b[j])
        arr[ind]=a[i++];
        else
        arr[ind]=b[j++];
    while(i<n1){</pre>
        arr[ind]=a[i++];
    while(j<n2){</pre>
        arr[ind]=b[j++];
void merge_sort(int arr[], int l, int r)
        int mid = (1 + r) / 2;
        merge_sort(arr, 1, mid);
        merge_sort(arr, mid + 1, r);
        merge(arr, 1, mid, r);
void quick(int b[],int beg,int end)
    if(beg>end)
```

```
return;
    int pivot=beg,low=beg+1,high=end;
   while(pivot!=high)
        if(b[low]<=b[pivot])</pre>
            if(b[high]>b[pivot])
            high--;
            else
                if(low<high)</pre>
                swap(b[low],b[high]);
                     swap(b[pivot],b[high]);
                     break;
    quick(b,beg,high-1);
    quick(b,high+1,end);
int main()
    int n=100000;
    for(int i=100;i<=n;i+=100){
        int arr[n],b[n];
        for(int i=0;i<n;i++){</pre>
            arr[i]=rand()%100;
        copy(arr,arr+n,b);
        auto start = chrono::high_resolution_clock::now();
        merge_sort(arr,0,n-1);
        auto end = chrono::high_resolution_clock::now();
        cout<<"\n"<<n<<"\t"<<chrono::duration_cast<chrono::nanoseconds>(end -
start).count()<<"\t";</pre>
        start = chrono::high_resolution_clock::now();
        quick(b,0,n-1);
        end = chrono::high_resolution_clock::now();
        cout<<chrono::duration_cast<chrono::nanoseconds>(end - start).count();
```

# **Observation table:**

100         0         0           200         0         0           300         0         0           400         0         0           500         0         0           600         0         0           700         0         0.985           800         0.441         1           900         0         0.999           1000         0         0.989           1100         0         1.007           1200         0         0.989           1300         1.008         0           1400         1.037         1.018           1500         0         1.034           1600         1.037         0.997           1700         0         1.395           1800         1.037         0.991           1900         1.03         0           2000         0         0.971           2100         1.031         1.042           2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03	n	MergeSort(ms)	QuickSort(ms)
300         0         0           400         0         0           500         0         0           600         0         0           700         0         0.985           800         0.441         1           900         0         0.999           1000         0         0.989           1100         0         1.007           1200         0         0.989           1300         1.008         0           1400         1.037         1.018           1500         0         1.034           1600         1.037         0.997           1700         0         1.395           1800         1.037         0.991           1900         1.03         0           2000         0         0.971           2100         1.031         1.042           2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.043           2600         1.002         1.046           2700 <t< td=""><td>100</td><td>0</td><td>0</td></t<>	100	0	0
400         0         0           500         0         0           600         0         0           700         0         0.985           800         0.441         1           900         0         0.999           1000         0         0.989           1100         0         1.007           1200         0         0.989           1300         1.008         0           1400         1.037         1.018           1500         0         1.034           1600         1.037         0.997           1700         0         1.395           1800         1.037         0.991           1900         1.03         0           2000         0         0.971           2100         1.031         1.042           2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.046           2700         0.995         1.135           2800         1.038         1.032           2900	200	0	0
500         0         0           600         0         0           700         0         0.985           800         0.441         1           900         0         0.999           1000         0         0.989           1100         0         1.007           1200         0         0.989           1300         1.008         0           1400         1.037         1.018           1500         0         1.034           1600         1.037         0.997           1700         0         1.395           1800         1.037         0.991           1900         1.03         0           2000         0         0.971           2100         1.031         1.042           2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.043           2600         1.002         1.046           2700         0.995         1.135           2800         1.038         1.032           29	300	0	0
600         0         0         0.985           800         0.441         1           900         0         0.999           1000         0         0.989           1100         0         0.989           1200         0         0.989           1300         1.008         0           1400         1.037         1.018           1500         0         1.034           1600         1.037         0.997           1700         0         1.395           1800         1.037         0.991           1900         1.03         0           2000         0         0.971           2100         1.031         1.042           2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.043           2600         1.002         1.046           2700         0.995         1.135           2800         1.038         1.032           2900         1.031         1.038           3000         1.038         1.203 </td <td>400</td> <td>0</td> <td>0</td>	400	0	0
700         0         0.985           800         0.441         1           900         0         0.999           1000         0         0.989           1100         0         0.989           1300         1.008         0           1400         1.037         1.018           1500         0         1.034           1600         1.037         0.997           1700         0         1.395           1800         1.037         0.991           1900         1.03         0           2000         0         0.971           2100         1.031         1.042           2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.043           2600         1.002         1.046           2700         0.995         1.135           2800         1.031         1.038           3000         1.002         1.24           3100         1.038         1.203           3200         1.038         1.203	500	0	0
800         0.441         1           900         0         0.999           1000         0         0.989           1100         0         0.989           1300         1.008         0           1400         1.037         1.018           1500         0         1.034           1600         1.037         0.997           1700         0         1.395           1800         1.037         0.991           1900         1.03         0           2000         0         0.971           2100         1.031         1.042           2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.043           2600         1.002         1.046           2700         0.995         1.135           2800         1.031         1.038           3000         1.032         1.24           3100         1.038         1.203           3200         1.038         1.203           3400         1.039         1.203 <td>600</td> <td>0</td> <td>0</td>	600	0	0
900         0         0.999           1000         0         0.989           1100         0         1.007           1200         0         0.989           1300         1.008         0           1400         1.037         1.018           1500         0         1.034           1600         1.037         0.997           1700         0         1.395           1800         1.037         0.991           1900         1.03         0           2000         0         0.971           2100         1.031         1.042           2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.046           2700         0.995         1.135           2800         1.038         1.032           2900         1.031         1.038           3000         1.002         1.24           3100         1.038         1.203           3200         1.038         1.203           3400         1.037         1.157 </td <td>700</td> <td>0</td> <td>0.985</td>	700	0	0.985
1000         0         0.989           1100         0         1.007           1200         0         0.989           1300         1.008         0           1400         1.037         1.018           1500         0         1.034           1600         1.037         0.997           1700         0         1.395           1800         1.037         0.991           1900         1.03         0           2000         0         0.971           2100         1.031         1.042           2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.043           2600         1.002         1.046           2700         0.995         1.135           2800         1.038         1.032           2900         1.031         1.038           3000         1.002         1.24           3100         1.038         1.203           3200         1.038         1.203           3400         1.037         1.157	800	0.441	1
1100         0         1.007           1200         0         0.989           1300         1.008         0           1400         1.037         1.018           1500         0         1.034           1600         1.037         0.997           1700         0         1.395           1800         1.037         0.991           1900         1.03         0           2000         0         0.971           2100         1.031         1.042           2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.043           2600         1.002         1.046           2700         0.995         1.135           2800         1.038         1.032           2900         1.031         1.038           3000         1.038         1.203           3200         1.038         1.203           3400         1.039         1.203           3400         1.037         1.157           3500         1.038         1.206 </td <td>900</td> <td>0</td> <td>0.999</td>	900	0	0.999
1200         0         0.989           1300         1.008         0           1400         1.037         1.018           1500         0         1.034           1600         1.037         0.997           1700         0         1.395           1800         1.037         0.991           1900         1.03         0           2000         0         0.971           2100         1.031         1.042           2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.043           2600         1.002         1.046           2700         0.995         1.135           2800         1.038         1.032           2900         1.031         1.038           3000         1.038         1.203           3200         1.038         1.203           3400         1.039         1.203           3400         1.037         1.157           3500         1.038         1.206 <td>1000</td> <td>0</td> <td>0.989</td>	1000	0	0.989
1300         1.008         0           1400         1.037         1.018           1500         0         1.034           1600         1.037         0.997           1700         0         1.395           1800         1.037         0.991           1900         1.03         0           2000         0         0.971           2100         1.031         1.042           2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.043           2600         1.002         1.046           2700         0.995         1.135           2800         1.031         1.038           3000         1.031         1.038           3000         1.031         1.038           3000         1.038         1.203           3200         1.038         1.203           3400         1.037         1.157           3500         1.038         1.206	1100	0	1.007
1400         1.037         1.018           1500         0         1.034           1600         1.037         0.997           1700         0         1.395           1800         1.037         0.991           1900         1.03         0           2000         0         0.971           2100         1.031         1.042           2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.043           2600         1.002         1.046           2700         0.995         1.135           2800         1.038         1.032           2900         1.031         1.038           3000         1.038         1.203           3200         1.038         1.203           3400         1.039         1.203           3400         1.038         1.206	1200	0	0.989
1500         0         1.034           1600         1.037         0.997           1700         0         1.395           1800         1.037         0.991           1900         1.03         0           2000         0         0.971           2100         1.031         1.042           2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.043           2600         1.002         1.046           2700         0.995         1.135           2800         1.038         1.032           2900         1.031         1.038           3000         1.038         1.203           3200         1.038         1.203           3400         1.039         1.203           3400         1.037         1.157           3500         1.038         1.206	1300	1.008	0
1600         1.037         0.997           1700         0         1.395           1800         1.037         0.991           1900         1.03         0           2000         0         0.971           2100         1.031         1.042           2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.043           2600         1.002         1.046           2700         0.995         1.135           2800         1.038         1.032           2900         1.031         1.038           3000         1.038         1.203           3200         1.038         1.203           3400         1.039         1.203           3400         1.037         1.157           3500         1.038         1.206	1400	1.037	1.018
1700         0         1.395           1800         1.037         0.991           1900         1.03         0           2000         0         0.971           2100         1.031         1.042           2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.043           2600         1.002         1.046           2700         0.995         1.135           2800         1.038         1.032           2900         1.031         1.038           3000         1.038         1.203           3200         1.038         1.203           3400         1.039         1.203           3400         1.037         1.157           3500         1.038         1.206	1500	0	1.034
1800         1.037         0.991           1900         1.03         0           2000         0         0.971           2100         1.031         1.042           2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.043           2600         1.002         1.046           2700         0.995         1.135           2800         1.038         1.032           2900         1.031         1.038           3000         1.032         1.24           3100         1.038         1.203           3200         1.038         1.04           3300         1.039         1.203           3400         1.037         1.157           3500         1.038         1.206	1600	1.037	
1900         1.03         0           2000         0         0.971           2100         1.031         1.042           2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.043           2600         1.002         1.046           2700         0.995         1.135           2800         1.038         1.032           2900         1.031         1.038           3000         1.038         1.203           3200         1.038         1.04           3300         1.039         1.203           3400         1.037         1.157           3500         1.038         1.206	1700	0	1.395
2000         0         0.971           2100         1.031         1.042           2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.043           2600         1.002         1.046           2700         0.995         1.135           2800         1.038         1.032           2900         1.031         1.038           3000         1.002         1.24           3100         1.038         1.203           3200         1.038         1.04           3300         1.039         1.203           3400         1.037         1.157           3500         1.038         1.206	1800	1.037	0.991
2100         1.031         1.042           2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.043           2600         1.002         1.046           2700         0.995         1.135           2800         1.038         1.032           2900         1.031         1.038           3000         1.038         1.203           3200         1.038         1.04           3300         1.039         1.203           3400         1.037         1.157           3500         1.038         1.206	1900	1.03	0
2200         1.037         0.991           2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.043           2600         1.002         1.046           2700         0.995         1.135           2800         1.038         1.032           2900         1.031         1.038           3000         1.002         1.24           3100         1.038         1.203           3200         1.038         1.04           3300         1.039         1.203           3400         1.037         1.157           3500         1.038         1.206	2000	_	0.971
2300         0.996         1.046           2400         1.047         0.983           2500         1.03         1.043           2600         1.002         1.046           2700         0.995         1.135           2800         1.038         1.032           2900         1.031         1.038           3000         1.002         1.24           3100         1.038         1.203           3200         1.038         1.04           3300         1.039         1.203           3400         1.037         1.157           3500         1.038         1.206	2100	1.031	
2400         1.047         0.983           2500         1.03         1.043           2600         1.002         1.046           2700         0.995         1.135           2800         1.038         1.032           2900         1.031         1.038           3000         1.002         1.24           3100         1.038         1.203           3200         1.038         1.04           3300         1.039         1.203           3400         1.037         1.157           3500         1.038         1.206	2200	1.037	0.991
2500         1.03         1.043           2600         1.002         1.046           2700         0.995         1.135           2800         1.038         1.032           2900         1.031         1.038           3000         1.002         1.24           3100         1.038         1.203           3200         1.038         1.04           3300         1.039         1.203           3400         1.037         1.157           3500         1.038         1.206	2300	0.996	1.046
2600       1.002       1.046         2700       0.995       1.135         2800       1.038       1.032         2900       1.031       1.038         3000       1.002       1.24         3100       1.038       1.203         3200       1.038       1.04         3300       1.039       1.203         3400       1.037       1.157         3500       1.038       1.206	2400	1.047	0.983
2700       0.995       1.135         2800       1.038       1.032         2900       1.031       1.038         3000       1.002       1.24         3100       1.038       1.203         3200       1.038       1.04         3300       1.039       1.203         3400       1.037       1.157         3500       1.038       1.206	2500	1.03	1.043
2800         1.038         1.032           2900         1.031         1.038           3000         1.002         1.24           3100         1.038         1.203           3200         1.038         1.04           3300         1.039         1.203           3400         1.037         1.157           3500         1.038         1.206	2600		
2900     1.031     1.038       3000     1.002     1.24       3100     1.038     1.203       3200     1.038     1.04       3300     1.039     1.203       3400     1.037     1.157       3500     1.038     1.206	2700		1.135
3000     1.002     1.24       3100     1.038     1.203       3200     1.038     1.04       3300     1.039     1.203       3400     1.037     1.157       3500     1.038     1.206	2800	1.038	
3100       1.038       1.203         3200       1.038       1.04         3300       1.039       1.203         3400       1.037       1.157         3500       1.038       1.206	2900	1.031	1.038
3200       1.038       1.04         3300       1.039       1.203         3400       1.037       1.157         3500       1.038       1.206	3000	1.002	
3300     1.039     1.203       3400     1.037     1.157       3500     1.038     1.206	3100	1.038	
3400     1.037     1.157       3500     1.038     1.206			
3500 1.038 1.206	3300	1.039	1.203
	3400		
3600 1.038 1.298	3500	1.038	1.206
	3600	1.038	1.298

3700	2.1	1.038
3800	1.042	1.038
3900	1.037	1.689
4000	1.041	1.037
4100	1.04	1.04
4200	1.845	1.042
4300	2.518	1.041
4400	1.038	1.034
4500	1.039	1.035
4600	1	1.234
4700	1.036	1.037
4800	2.95	1.247
4900	1.001	1.027
5000	1.001	1.237
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**Observation:** Quiksort takes less time to sort than merge sort.

**Conclusion:** Successfully wrote a program to implement merge and quick sort. Made relevant observations and found the running time of both sorting methods. We can conclude that quick sort is faster.