

# Project 3: Planning Search

## Uninformed Searches

### Problem 1

The optimal path length of the solution is 6 steps as discovered by breadth first and uniform cost searches. Uniform cost however does seem to take longer and goes through more nodes to find the optimal solution.

Depth search is extremely fast but does not find the most optimal solution. In the world of air cargo, that may be very bad as distances between airports are not small. As an example, the optimal solution discovered by both breadth first and uniform cost say to load Cargo1 on Plane1 and load Cargo2 on Plane2 and fly each plane to their appropriate location once (SFO->JFK for P1 and JFK->SFO for P2); however, depth first search has multiple flies between SFO and JFK for the same plane which is very expensive (time, fuel, etc.).

Optimal sequence:

Load(C1, P1, SFO)

Load(C2, P2, JFK)

Fly(P1, SFO, JFK)

Fly(P2, JFK, SFO)

Unload(C1, P1, JFK)

Unload(C2, P2, SFO)

Search	Expansions	Goal Tests	New Nodes	Time (s)	Path Length
Breadth First	43	56	180	.02	6
Depth First	21	22	84	.01	20
Uniform Cost	55	57	224	.03	6

### Problem 2

Problem 2 is consistent with results from Problem 1. The optimal length is 9 as discovered by Breadth First and Uniform Cost (more expensive) and depth first is extremely fast but takes 8.5x as many steps.

Optimal Sequence:

Load(C2, P2, JFK)  
Fly(P2, JFK, ATL)  
Load(C3, P2, ATL)  
Fly(P2, ATL, SFO)  
Unload(C3, P2, SFO)  
Unload(C2, P2, SFO)  
Load(C1, P1, SFO)  
Fly(P1, SFO, JFK)  
Unload(C1, P1, JFK)

Search	Expansions	Goal Tests	New Nodes	Time (s)	Path Length
Breadth First	3063	4274	25442	4.86	9
Depth First	82	83	511	.11	77
Uniform Cost	4444	4446	36366	6.90	9

### Problem 3

Problem 3 is consistent with results from Problem 1 and Problem 2. The optimal length is 12 as discovered by Breadth First and Uniform Cost (more expensive) and depth first is extremely fast but takes 32x as many steps.

Optimal Sequence:

Load(C2, P2, JFK)  
Fly(P2, JFK, ORD)  
Load(C4, P2, ORD)  
Fly(P2, ORD, SFO)  
Load(C1, P1, SFO)  
Fly(P1, SFO, ATL)  
Load(C3, P1, ATL)  
Fly(P1, ATL, JFK)  
Unload(C4, P2, SFO)  
Unload(C3, P1, JFK)  
Unload(C2, P2, SFO)  
Unload(C1, P1, JFK)

Search	Expansions	Goal Tests	New Nodes	Time (s)	Path Length
Breadth First	14663	18098	129631	29.45	12
Depth First	408	409	3364	1.26	392
Uniform Cost	18223	18225	159618	35.67	12

## Heuristic Searches

### Problem 1

Each of the heuristic searches finds the optimal solution of 6 steps; however,  $h_{pg\_levelsum}$  takes significantly longer (15x). Even though  $h_{pg\_levelsum}$  is clearly a good heuristic as the algorithm is taking far fewer steps to get to the goal, the computation cost at each step is too high.  $h_1$  is nearly the same as uninformed Uniform Cost search and  $h_{ignore\_preconditions}$  goes through fewer nodes to reach the same solution in the same time.

Search	Expansions	Goal Tests	New Nodes	Time (s)	Path Length
A* w/ $h_1$	55	57	224	.03	6
A* w/ $h_{ignore\_preconditions}$	41	43	170	.03	6
A* w/ $h_{pg\_levelsum}$	11	13	50	.46	6

## Problem 2

Each of the heuristic searches finds the optimal solution of 9 steps; however, `h_pg_levelsum` takes significantly longer (11-26x). Even though `h_pg_levelsum` is clearly a good heuristic as the algorithm is taking far fewer steps to get to the goal, the computation cost at each step is too high. `h_1` is nearly the same as uninformed Uniform Cost search. Contrary to Problem 1, `h_ignore_preconditions` is both faster and goes through fewer nodes to reach the same solution.

Search	Expansions	Goal Tests	New Nodes	Time (s)	Path Length
A* w/ <code>h_1</code>	4444	4446	36366	6.84	9
A* w/ <code>h_ignore_preconditions</code>	1526	1528	12725	2.94	9
A* w/ <code>h_pg_levelsum</code>	293	295	2407	76.76	9

## Problem 3

Each of the heuristic searches finds the optimal solution of 12 steps; however, `h_pg_levelsum` takes significantly longer (6-17x). Even though `h_pg_levelsum` is clearly a good heuristic as the algorithm is taking far fewer steps to get to the goal, the computation cost at each step is too high. `h_1` is nearly the same as uninformed Uniform Cost search. Contrary to Problem 1, `h_ignore_preconditions` is both faster and goes through fewer nodes to reach the same solution.

Search	Expansions	Goal Tests	New Nodes	Time (s)	Path Length
A* w/ <code>h_1</code>	18223	18225	159618	36.04	12
A* w/ <code>h_ignore_preconditions</code>	5040	5042	44944	11.77	12
A* w/ <code>h_pg_levelsum</code>	331	333	3054	203.98	12

## Conclusion

Out of all the searches that return the optimal solution, A\* w/ h\_ignore\_preconditions performed the best (exception was Problem 1 where it took split seconds longer that is likely just a measuring precision issue and Problem 1 is too small to be a real world problem). Hence, heuristic based searches are the way to go.

I believe h\_ignore\_preconditions does so well because it is not only a good heuristic on its own but its computation cost is very low. This is especially compared to h\_pg\_levelsum where the algorithm clearly explores the graph in a better path to the solution but the computation cost of the heuristic is very large. This is mentioned in section 11.4 page 398 “It [level sum heuristic] is much more accurate than number-of-unsatisfied-goals heuristic from Section 11.2” [1]. As the course has continuously suggested however, it is better to start with a simple solution and apply intelligence only as needed. Hence, if the only advantage of using h\_pg\_levelsum is to use less memory but modern hardware infrastructures invalidate that advantage, then the better solution is h\_ignore\_preconditions as it's easier to implement and low on computation cost.

I did notice however the slowness factor when comparing time between h\_pg\_levelsum vs. h\_ignore\_preconditions got lower as the problem got larger. It's hard to say whether that is a true trend because there are only 3 problems, but if it does hold true than h\_pg\_levelsum would be a much better heuristic as real world problems are likely to be large and an optimal exploration path would be better for memory costs.<sup>1</sup>

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<sup>1</sup> Russell, S. J., Norvig, P. (2002). *Artificial Intelligence: A Modern Approach (2nd Edition)*. Prentice Hall. ISBN: 0137903952