### **BASIC ALGEBRA FORMULAS**

### **Arithmetic Operations**

$$a(b+c) = ab + ac, \qquad \frac{a}{b} \cdot \frac{c}{d} = \frac{ac}{bd}$$
$$\frac{a}{b} + \frac{c}{d} = \frac{ad + bc}{bd}, \qquad \frac{a/b}{c/d} = \frac{a}{b} \cdot \frac{d}{c}$$

## **Laws of Signs**

$$-(-a) = a, \qquad \frac{-a}{b} = -\frac{a}{b} = \frac{a}{-b}$$

**Zero** Division by zero is not defined.

If 
$$a \neq 0$$
:  $\frac{0}{a} = 0$ ,  $a^0 = 1$ ,  $0^a = 0$   
For any number  $a$ :  $a \cdot 0 = 0 \cdot a = 0$ 

# **Laws of Exponents**

$$a^{m}a^{n} = a^{m+n},$$
  $(ab)^{m} = a^{m}b^{m},$   $(a^{m})^{n} = a^{mn},$   $a^{m/n} = \sqrt[n]{a^{m}} = \left(\sqrt[n]{a}\right)^{m}$   
If  $a \neq 0$ ,  
 $\frac{a^{m}}{a^{n}} = a^{m-n},$   $a^{0} = 1,$   $a^{-m} = \frac{1}{a^{m}}.$ 

The Binomial Theorem For any positive integer n,

$$(a+b)^{n} = a^{n} + na^{n-1}b + \frac{n(n-1)}{1 \cdot 2}a^{n-2}b^{2} + \frac{n(n-1)(n-2)}{1 \cdot 2 \cdot 3}a^{n-3}b^{3} + \dots + nab^{n-1} + b^{n}.$$

For instance,

$$(a + b)^2 = a^2 + 2ab + b^2,$$
  $(a - b)^2 = a^2 - 2ab + b^2$   
 $(a + b)^3 = a^3 + 3a^2b + 3ab^2 + b^3,$   $(a - b)^3 = a^3 - 3a^2b + 3ab^2 - b^3.$ 

### Factoring the Difference of Like Integer Powers, n > 1

$$a^{n} - b^{n} = (a - b)(a^{n-1} + a^{n-2}b + a^{n-3}b^{2} + \cdots + ab^{n-2} + b^{n-1})$$

For instance,

$$a^{2} - b^{2} = (a - b)(a + b),$$
  

$$a^{3} - b^{3} = (a - b)(a^{2} + ab + b^{2}),$$
  

$$a^{4} - b^{4} = (a - b)(a^{3} + a^{2}b + ab^{2} + b^{3}).$$

Completing the Square If  $a \neq 0$ ,

$$ax^2 + bx + c = au^2 + C$$
  $\left(u = x + (b/2a), C = c - \frac{b^2}{4a}\right)$ 

The Quadratic Formula If  $a \neq 0$  and  $ax^2 + bx + c = 0$ , then

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}.$$