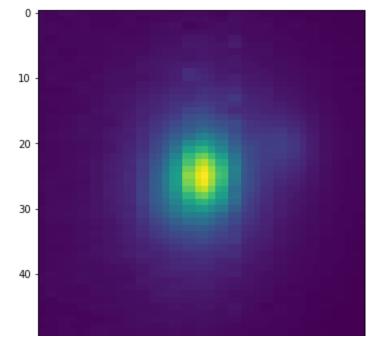
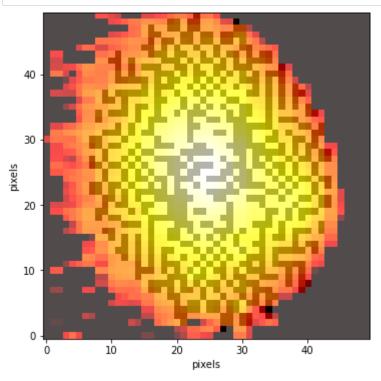
```
In [90]:
         # 04/05/2022 - Trying out Gaussian MGE on J0037 by modifying fit ngc4342 from
         # from mge fit examples
         # import libraries
         import numpy as np
         np.set printoptions(threshold=10000)
         import matplotlib.pyplot as plt
         import warnings
         warnings.filterwarnings( "ignore", module = "matplotlib\..*" )
         warnings.filterwarnings( "ignore", module = "plotbin\..*" )
         from astropy.io import fits
         from os import path
         import mgefit
         from mgefit.find galaxy import find galaxy
         from mgefit.mge fit 1d import mge fit 1d
         from mgefit.sectors photometry import sectors photometry
         from mgefit.mge fit sectors import mge fit sectors
         from mgefit.mge print contours import mge print contours
         from mgefit.mge fit sectors twist import mge fit sectors twist
         from mgefit.sectors photometry twist import sectors photometry twist
         from mgefit.mge print contours twist import mge print contours twist
         plt.rcParams["figure.figsize"] = (8, 6)
         In [2]:
         file dir = '/data/raw data/KECK KCWI SLACS kinematics shawn/CF mosaics/SDSSJ0
         obj name = '/SDSSJ0037-0942'
In [3]:
         # import image, center, and crop
         file = file dir + "/KCWI J0037 icubes mosaic 0.1457 2Dintegrated.fits"
         hdu = fits.open(file)
         img = hdu[0].data
         header = hdu[0].header
         # crop the image to ~ 50 pixels
         central pix = np.unravel index(np.argmax(img, axis=None), img.shape)
         central pix x = central pix[1]
         central pix y = central pix[0]
         crop width = 50
         half width = int(crop width/2)
         img = img[central_pix_y - half width:central pix y + half width, central pix
         plt.clf()
         plt.imshow(img)
        <matplotlib.image.AxesImage at 0x7ff85d675d90>
Out[3]:
```



```
In [4]:
        # check differences for different psf
        # sky and psf?
        scale = 0.147 # arcsec/pixel
         #minlevel?
        minlevel = 1 # counts/pixel
         # exposure time
         exp time = 1.5 * 3600 # seconds
         ngauss = 12
         # Keck is typically 0.7-0.8
         seeing fwhm = 0.75 \# arcsec
         sigmapsf = seeing fwhm / scale / 2.355 # pixels, 2.355 is fwhm/sigma
         #print(sigma psf)
         # Here we use FIND GALAXY directly inside the procedure. Usually you may want
         # to experiment with different values of the FRACTION keyword, before adopting
        # given values of Eps, Ang, Xc, Yc.
         # take different values of pixel fractions
        lower, upper, steps = (0.06, 0.12, 7)
         fractions = np.linspace(lower, upper, steps)
         eps list = []
         theta list = []
         #cen y list = [] # don't need these, already centered it
         \#cen \ x \ list = []
         for frac in fractions:
            #print(f'Calculating fraction {frac}')
            frac = np.around(frac, 2)
            mid = np.around((upper+lower)/2, 2)
            plt.clf()
            if (frac==lower) | (frac==mid) | (frac==upper):
                plot = 1
            else:
                plot = 0
            #plt.clf()
             f = find galaxy(img, fraction=frac, plot=0, quiet=True)
            eps = f.eps
            theta = f.theta
            \#cen\ y = f.ypeak
            \#cen \ x = f.xpeak
            # assign to lists
            eps list.append(eps)
            theta list.append(theta)
            #cen y list.append(cen y)
            #cen_x_list.append(cen x)
            #if plot == 1:
                 plt.title(f'{frac}')
                 plt.pause(1) # Allow plot to appear on the screen
         eps mean = np.mean(eps list)
         theta mean = np.mean(theta list)
         #cen y med = np.median(cen y list)
```

```
\#cen \ x \ med = np.median(cen \ x \ list)
# Perform galaxy photometry
plt.clf()
s = sectors photometry(img, eps mean, theta mean, f.xpeak, f.ypeak,
                      minlevel=minlevel, plot=1)
plt.pause(1) # Allow plot to appear on the screen
# Do the actual MGE fit
# For the final publication-quality MGE fit one should include the line
# "from mge fit sectors regularized import mge fit sectors regularized"
# at the top of this file, rename mge fit sectors() into
# mge fit sectors regularized() and re-run the procedure.
# See the documentation of mge fit sectors regularized for details.
plt.clf()
m = mge fit sectors(s.radius, s.angle, s.counts, eps_mean,
                   ngauss=ngauss, sigmapsf=sigmapsf, #normpsf=normpsf,
                   scale=scale, plot=1, bulge disk=0, linear=0)
plt.pause(1) # Allow plot to appear on the screen
# take the outputs
total counts = m.sol[0]
sigma pix = m.sol[1]
q = m.sol[2]
absdev = m.absdev
# calculate peak surface brightness of each gaussian
peak surf br = total counts/(2*np.pi*q*sigma pix**2)
# convert to johnson i band
# Here 20.840 is the photometric zeropint, 0.1 is a correction for infinite a
# for surface brightness measurements, and AI is the extinction in the I-band
# dust extinction ~ 0.05 from https://irsa.ipac.caltech.edu/workspace/TMP lFD
AI = 0.05
iband surf br = 20.840 + 0.1 + 5 * np.log10(scale) + 2.5 * np.log10(exp time)
# convert to surface density (L sol I pc-2)
M sol I = 4.08
surf density = (64800/np.pi)**2 * 10**( 0.4 * (M sol I - iband surf br))
# convert sigma from pixels to arcsec
sigma = sigma pix * scale
# Show contour plots of the results
plt.clf()
plt.subplot(121)
mge print contours(img.clip(minlevel), theta mean, f.xpeak, f.ypeak, m.sol, s
                  binning=7, sigmapsf=sigmapsf, #normpsf=normpsf,
                  magrange=9)
# Extract the central part of the image to plot at high resolution.
# The MGE is centered to fractional pixel accuracy to ease visual comparson.
n = int(np.around(2/scale))
img cen = img[f.xpeak-n:f.xpeak+n, f.ypeak-n:f.ypeak+n]
xc, yc = n - f.xpeak + f.xmed, n - f.ypeak + f.ymed
plt.subplot(122)
mge print contours(img_cen, theta_mean, xc, yc, m.sol,
```

sigmapsf=sigmapsf, #normpsf=normpsf,
scale=scale)
plt.pause(1) # Allow plot to appear on the screen



```
Iteration:1 chi2: 2.747 Nonzero: 5/12
Iteration:11 chi2: 2.440 Nonzero: 4/12
Iteration:21 chi2: 2.436 Nonzero: 4/12
```

Nonzero Gaussians: 4/12

Eliminating not useful Gaussians...

Starting nonlinear fit...

Iteration:1 chi2: 2.428 Nonzero: 4/4

Nonzero Gaussians: 4/4

Eliminating not useful Gaussians...

All Gaussians are needed!

Computation time: 0.41 seconds

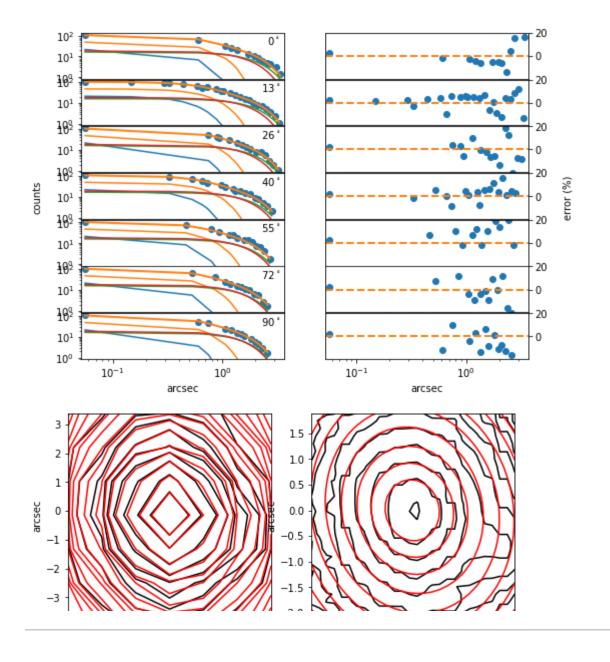
Total Iterations: 25 Nonzero Gaussians: 4 Unused Gaussians: 8

Sectors used in the fit: 19

Total number of points fitted: 287

Chi2: 2.427 STDEV: 0.09157 MEANABSDEV: 0.07049

Total_Counts	sigma_Pixels	q_obs
############	##############	##############
8.050909e+02	1.62485	0.816537
3.858726e+03	3.17038	0.786227
6.682631e+03	7.92397	0.846848
7.276328e+03	9.19698	0.780134



# Try out JAM model step with the model that has psf 0.75

```
In [5]:

V = np.genfromtxt(file_dir + obj_name + '_V_2d.txt', delimiter=',')

dV = np.genfromtxt(file_dir + obj_name + '_dV_2d.txt', delimiter=',')

VD = np.genfromtxt(file_dir + obj_name + '_VD_2d.txt', delimiter=',')

dVD = np.genfromtxt(file_dir + obj_name + '_dVD_2d.txt', delimiter=',')

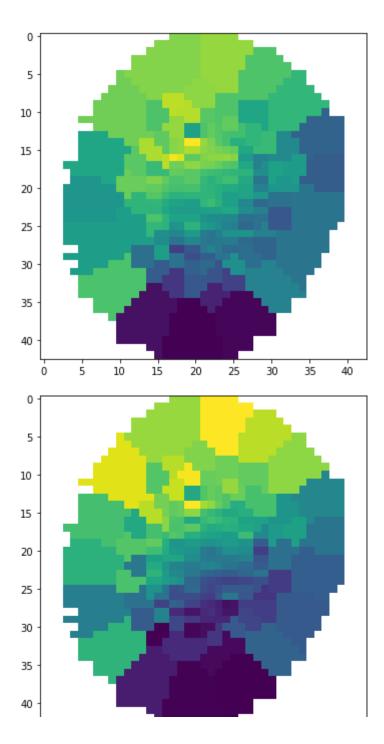
Vrms = np.sqrt(V**2 + VD**2)

plt.imshow(Vrms)

plt.figure()

plt.imshow(V)
```

Out[5]: <matplotlib.image.AxesImage at 0x7ff859f479d0>



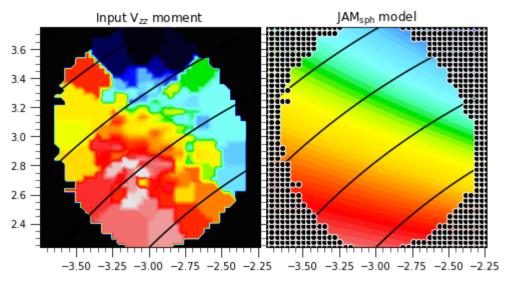
```
In [93]:
          0.00
              Copyright (C) 2019-2021, Michele Cappellari
              E-mail: michele.cappellari at physics.ox.ac.uk
              Updated versions of the software are available from my web page
              http://purl.org/cappellari/software
          CHANGELOG
          _ _ _ _ _ _ _ _
          V1.1.0: MC, Oxford, 16 July 2020
              - Compute both Vrms and LOS velocity.
          V1.0.1: MC, Oxford, 21 April 2020
              - Made a separate file
          V1.0.0: Michele Cappellari, Oxford, 08 November 2019
              - Written and tested
          import numpy as np
          import matplotlib.pyplot as plt
          from jampy.jam axi proj import jam axi proj
          from jampy.jam_axi proj import rotate points
          from plotbin.plot velfield import plot velfield
          #np.random.seed(123)
          \#xbin, ybin = np.random.uniform(low=[-55, -40], high=[55, 40], size=[1000, 2]
          What do I do for inclination?
          inclinations = np.arange(40,100,10) # Assumed galaxy inclination
          \#r = np.sqrt(xbin^{**}2 + (ybin/np.cos(np.radians(inc)))^{**}2) \# Radius in the pla
          \#a = 40
                                                                     # Scale length in a
          \#vr = 2000*np.sqrt(r)/(r + a)
                                                                     # Assumed velocity
          #vel = vr * np.sin(np.radians(inc))*xbin/r
                                                                    # Projected velocit
          \#sig = 8700/(r + a)
                                                                     # Assumed velocity
                                                                     # Vrms field in km/
          \#rms = np.sqrt(vel^{**}2 + sig^{**}2)
          # Until here I computed some fake input kinematics to fit with JAM.
          # Ina real application, instead of the above lines one will read the
          # measured stellar kinematics, e.g. from integral-field spectroscopy
          Open kinematics maps
          V = np.genfromtxt(file_dir + obj_name + '_V_2d.txt', delimiter=',')
dV = np.genfromtxt(file_dir + obj_name + '_dV_2d.txt', delimiter=',')
          VD = np.genfromtxt(file dir + obj name + ' VD 2d.txt', delimiter=',')
          dVD = np.genfromtxt(file dir + obj name + ' dVD 2d.txt', delimiter=',')
          # compute rms velocity
          Vrms = np.sqrt(V**2 + VD**2)
          dVrms = np.sqrt((dV*V)**2 + (dVD*VD)**2)/Vrms
```

```
x and y bins (pixels)
# write the grid of xbins and ybins with (0,0) at the center and the x-axis c
\# set x and y bins so that center is (0, 0)
size = V.shape[0]
xbin arcsec = np.linspace(-np.floor(size/2), np.floor(size/2), size) * scale
ybin arcsec = np.linspace(-np.floor(size/2), np.floor(size/2), size) * scale
# set PA from mean photometry fitting
PA = theta mean
# set new arrays with the rotated coordinates
xbin rot = np.zeros(size)
ybin rot = np.zeros(size)
# rotate the coordinates and append to array
for i in range(len(xbin arcsec)):
    for j in range(len(ybin arcsec)):
        x new, y new = rotate points(xbin arcsec[i], ybin arcsec[j], PA)
        xbin rot[i] = x new
        ybin rot[j] = y new
xbin, ybin = np.meshgrid(xbin rot, ybin rot)
flatten data and bins
V = V.flatten()
dV = dV.flatten()
VD = VD.flatten()
dVD = dVD.flatten()
Vrms = Vrms.flatten()
dVrms = dVrms.flatten()
xbin = xbin.flatten()
ybin = ybin.flatten()
surface density
# take the surface density, etc from mge
surf = surf density # surf dens list[2] <- this was with psf 0.75</pre>
sigma = sigma #sigma list[2]
q0bs = q #q list[2]
from astropy.cosmology import Planck18 as cosmo # Planck 2018
# redshift, convert to angular diameter dist in Mpc
z = 0.195
distance = cosmo.angular diameter distance(z).value
mbh = 1e8 # Black hole mass in solar masses
# try different beta # TBD
\#beta\ list = [0.1, 0.2, 0.3, 0.4, 0.5]
beta = np.full like(surf, 0.2)
# Below I assume mass follows light, but in a real application one
# will generally include a dark halo in surf pot, sigma pot, qobs pot.
# See e.g. Cappellari (2013) for an example
```

```
# https://ui.adsabs.harvard.edu/abs/2013MNRAS.432.1709C
surf lum = surf pot = surf
sigma lum = sigma pot = sigma
qobs lum = qobs_pot = q0bs
sigmapsf = 0.75
sigmapsf = np.atleast 1d(sigmapsf)
sigmaX2 = sigma lum**2 + sigmapsf[:, None]**2
sigmaY2 = (sigma lum*qobs lum)**2 + sigmapsf[:, None]**2
\#normpsf = [0.7, 0.3]
pixsize = scale #0.8
goodbins = np.isfinite(Vrms) # take finite data
1.1.1
run JAM
# I use a loop below, just to higlight the fact that all parameters
# remain the same for the two JAM calls, except for 'moment' and 'data'
plt.figure(1)
reduced chi squared = np.zeros((len(inclinations)))
i=0
for inc in inclinations:
    print('#################")
    print(f'Inclination of {inc} degrees')
    #for moment, data, errors in zip(['zz', 'z'], [Vrms, V], [dVrms, dV]):
         print()
         print(f'Moment {moment}')
    moment = 'zz'
    data = Vrms
    errors = dVrms
    # The model is by design similar but not identical to the adopted kinemat
    m = jam_axi_proj(surf_lum, sigma_lum, qobs_lum, surf_pot, sigma_pot, qobs
                    inc, mbh, distance, xbin, ybin, plot=True, data=data, er
                    sigmapsf=sigmapsf, #normpsf=normpsf,
                    beta=beta, pixsize=pixsize,
                    moment=moment, goodbins=goodbins,
                    align='sph', ml=None, nodots=True)
    plt.pause(3)
    plt.figure(2)
    surf_pot *= m.ml # Scale the density by the best fitting M/L from the pr
    reduced chi squared[i] = m.chi2
    i = i+1
# plot the inclinations
fig, axs = plt.subplots()
axs.plot(inclinations, reduced chi squared)
axs.set ylabel(r'Reduced $\chi^2$')
axs.set xlabel('Inclination')
Inclination of 40 degrees
jam axi proj sph zz (analytic los=False) elapsed time sec: 1.74
```

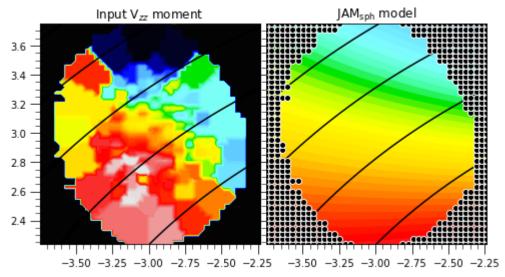
```
inc=40.0; beta[0]=0.20; kappa=1.00; M/L=0.646; BH=6.5e+07; chi2/D0F=4.39
Total mass MGE (MSun): 1.720e+12
```

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Inclination of 50 degrees

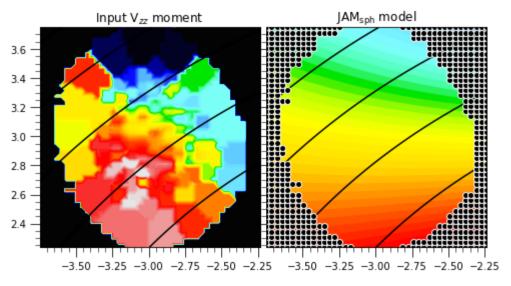
jam\_axi\_proj\_sph\_zz (analytic\_los=False) elapsed time sec: 1.70 inc=50.0; beta[0]=0.20; kappa=1.00; M/L=1.05; BH=1.0e+08; chi2/D0F=5.38 Total mass MGE (MSun): 1.804e+12



## 

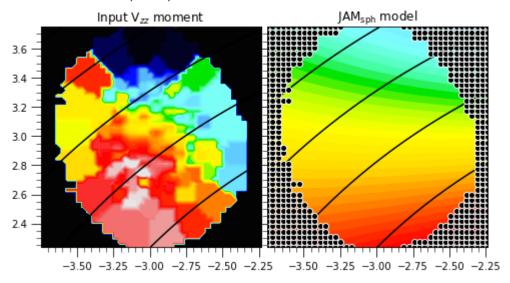
Inclination of 60 degrees

jam\_axi\_proj\_sph\_zz (analytic\_los=False) elapsed time sec: 1.60
inc=60.0; beta[0]=0.20; kappa=1.00; M/L=1.01; BH=1.0e+08; chi2/D0F=5.77
Total mass MGE (MSun): 1.817e+12



Inclination of 70 degrees

jam\_axi\_proj\_sph\_zz (analytic\_los=False) elapsed time sec: 1.35
inc=70.0; beta[0]=0.20; kappa=1.00; M/L=1.00; BH=1.0e+08; chi2/D0F=5.95
Total mass MGE (MSun): 1.821e+12

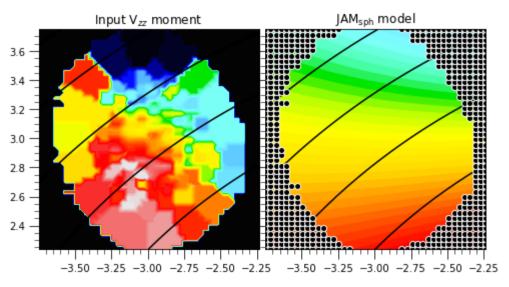


#### 

Inclination of 80 degrees

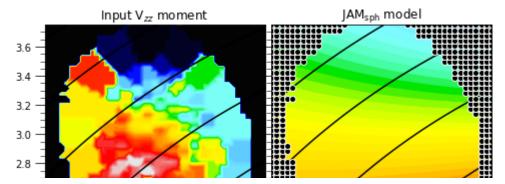
jam\_axi\_proj\_sph\_zz (analytic\_los=False) elapsed time sec: 1.31
inc=80.0; beta[0]=0.20; kappa=1.00; M/L=1.00; BH=1.0e+08; chi2/D0F=6.04

Total mass MGE (MSun): 1.823e+12



Inclination of 90 degrees

jam\_axi\_proj\_sph\_zz (analytic\_los=False) elapsed time sec: 1.34 inc=90.0; beta[0]=0.20; kappa=1.00; M/L=1.00; BH=1.0e+08; chi2/D0F=6.06 Total mass MGE (MSun): 1.824e+12



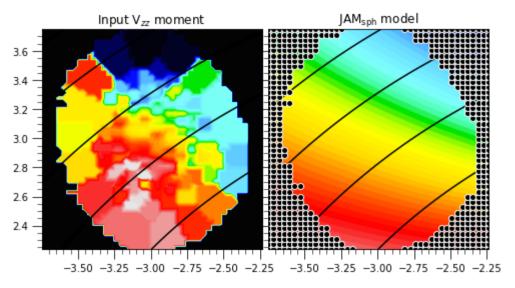
```
In [105...
          # try for a different value of beta
             Copyright (C) 2019-2021, Michele Cappellari
             E-mail: michele.cappellari at physics.ox.ac.uk
             Updated versions of the software are available from my web page
             http://purl.org/cappellari/software
          CHANGELOG
          _____
          V1.1.0: MC, Oxford, 16 July 2020
             - Compute both Vrms and LOS velocity.
          V1.0.1: MC, Oxford, 21 April 2020
             - Made a separate file
          V1.0.0: Michele Cappellari, Oxford, 08 November 2019
              - Written and tested
          import numpy as np
          import matplotlib.pyplot as plt
          from jampy.jam axi proj import jam axi proj
          from jampy.jam axi proj import rotate points
          from plotbin.plot velfield import plot velfield
          #np.random.seed(123)
          #xbin, ybin = np.random.uniform(low=[-55, -40], high=[55, 40], size=[1000, 2]
         What do I do for inclination?
          inclinations = np.arange(40, 100, 10)
                                                      # Assumed galaxy inclination
         \#r = np.sqrt(xbin^{**}2 + (ybin/np.cos(np.radians(inc)))^{**}2) \# Radius in the pla
          \#a = 40
                                                                  # Scale length in a
          #vr = 2000*np.sqrt(r)/(r + a)
                                                                  # Assumed velocity
         #vel = vr * np.sin(np.radians(inc))*xbin/r
                                                                  # Projected velocit
         \#sig = 8700/(r + a)
                                                                  # Assumed velocity
         \#rms = np.sqrt(vel^{**}2 + siq^{**}2)
                                                                  # Vrms field in km/
          # Until here I computed some fake input kinematics to fit with JAM.
         # Ina real application, instead of the above lines one will read the
         # measured stellar kinematics, e.g. from integral-field spectroscopy
          1.1.1
          Open kinematics maps
          V = np.genfromtxt(file dir + obj name + ' V_2d.txt', delimiter=',')
          dV = np.genfromtxt(file dir + obj name + ' dV 2d.txt', delimiter=',')
         VD = np.genfromtxt(file dir + obj name + 'VD 2d.txt', delimiter=',')
          dVD = np.genfromtxt(file dir + obj name + ' dVD 2d.txt', delimiter=',')
          # compute rms velocity
         Vrms = np.sqrt(V**2 + VD**2)
          dVrms = np.sqrt((dV*V)**2 + (dVD*VD)**2)/Vrms
```

```
x and y bins (pixels)
\# write the grid of xbins and ybins with (0,0) at the center and the x-axis c
\# set x and y bins so that center is (0, 0)
size = V.shape[0]
xbin arcsec = np.linspace(-np.floor(size/2), np.floor(size/2), size) * scale
ybin arcsec = np.linspace(-np.floor(size/2), np.floor(size/2), size) * scale
# set PA from mean photometry fitting
PA = theta mean
# set new arrays with the rotated coordinates
xbin rot = np.zeros(size)
ybin rot = np.zeros(size)
# rotate the coordinates and append to array
for i in range(len(xbin arcsec)):
    for j in range(len(ybin arcsec)):
        x new, y new = rotate points(xbin arcsec[i], ybin arcsec[j], PA)
        xbin rot[i] = x new
        ybin rot[j] = y new
xbin, ybin = np.meshqrid(xbin rot, ybin rot)
1.1.1
flatten data and bins
V = V.flatten()
dV = dV.flatten()
VD = VD.flatten()
dVD = dVD.flatten()
Vrms = Vrms.flatten()
dVrms = dVrms.flatten()
xbin = xbin.flatten()
ybin = ybin.flatten()
surface density
# take the surface density, etc from mge
surf = surf density # surf dens list[2] <- this was with psf 0.75</pre>
sigma = sigma #sigma list[2]
q0bs = q #q list[2]
from astropy.cosmology import Planck18 as cosmo # Planck 2018
# redshift, convert to angular diameter dist in Mpc
z = 0.195
distance = cosmo.angular diameter distance(z).value
mbh = 1e8 # Black hole mass in solar masses
# try different beta # TBD
\#beta\ list = [0.1, 0.2, 0.3, 0.4, 0.5]
beta = np.full like(surf, 0.5)
# Below I assume mass follows light, but in a real application one
# will generally include a dark halo in surf pot, sigma pot, gobs pot.
```

```
# See e.g. Cappellari (2013) for an example
# https://ui.adsabs.harvard.edu/abs/2013MNRAS.432.1709C
surf lum = surf pot = surf
sigma lum = sigma pot = sigma
qobs lum = qobs pot = q0bs
sigmapsf = 0.75
sigmapsf = np.atleast 1d(sigmapsf)
sigmaX2 = sigma lum**2 + sigmapsf[:, None]**2
sigmaY2 = (sigma lum*qobs lum)**2 + sigmapsf[:, None]**2
\#normpsf = [0.7, 0.3]
pixsize = scale #0.8
goodbins = np.isfinite(Vrms) # take finite data
run JAM
# I use a loop below, just to higlight the fact that all parameters
# remain the same for the two JAM calls, except for 'moment' and 'data'
plt.figure(1)
reduced chi squared = np.zeros((len(inclinations)))
i=0
for inc in inclinations:
    print('#################")
    print(f'Inclination of {inc} degrees')
    #for moment, data, errors in zip(['zz', 'z'], [Vrms, V], [dVrms, dV]):
         print()
         print(f'Moment {moment}')
    moment = 'zz'
    data = Vrms
    errors = dVrms
    # The model is by design similar but not identical to the adopted kinemat
    m = jam axi proj(surf lum, sigma lum, qobs lum, surf pot, sigma pot, qobs
                    inc, mbh, distance, xbin, ybin, plot=True, data=data, er
                    sigmapsf=sigmapsf, #normpsf=normpsf,
                    beta=beta, pixsize=pixsize,
                    moment=moment, goodbins=goodbins,
                    align='sph', ml=None, nodots=True)
    plt.pause(3)
    plt.figure(2)
    surf pot *= m.ml # Scale the density by the best fitting M/L from the pr
    reduced chi squared[i] = m.chi2
    i = i+1
# plot the inclinations
fig, axs = plt.subplots()
axs.plot(inclinations, reduced chi squared)
axs.set ylabel(r'Reduced $\chi^2$')
axs.set xlabel('Inclination')
Inclination of 40 degrees
```

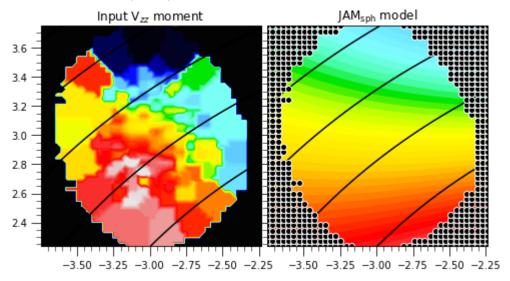
jam\_axi\_proj\_sph\_zz (analytic\_los=False) elapsed time sec: 1.59
inc=40.0; beta[0]=0.50; kappa=1.00; M/L=0.623; BH=6.2e+07; chi2/DOF=4.55
Total mass MGE (MSun): 1.996e+12

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Inclination of 50 degrees

jam\_axi\_proj\_sph\_zz (analytic\_los=False) elapsed time sec: 1.71
inc=50.0; beta[0]=0.50; kappa=1.00; M/L=1.21; BH=1.2e+08; chi2/D0F=5.44
Total mass MGE (MSun): 2.416e+12

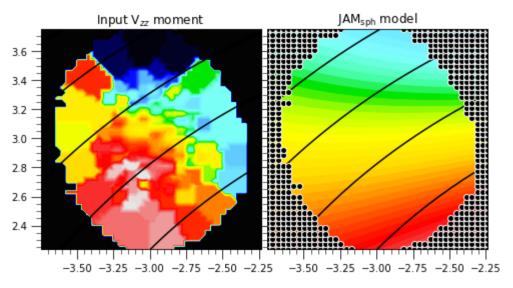


## 

Inclination of 60 degrees

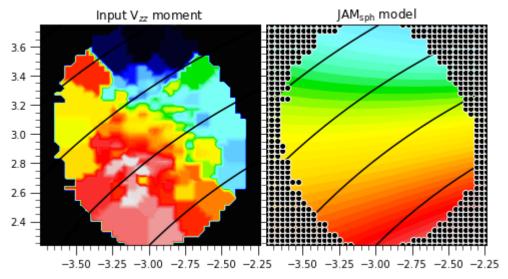
jam\_axi\_proj\_sph\_zz (analytic\_los=False) elapsed time sec: 1.46
inc=60.0; beta[0]=0.50; kappa=1.00; M/L=1.06; BH=1.1e+08; chi2/D0F=5.69

Total mass MGE (MSun): 2.557e+12



Inclination of 70 degrees

jam\_axi\_proj\_sph\_zz (analytic\_los=False) elapsed time sec: 1.42
inc=70.0; beta[0]=0.50; kappa=1.00; M/L=1.03; BH=1.0e+08; chi2/D0F=5.80
Total mass MGE (MSun): 2.623e+12

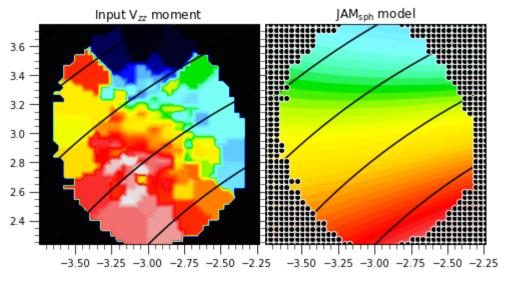


#### 

Inclination of 80 degrees

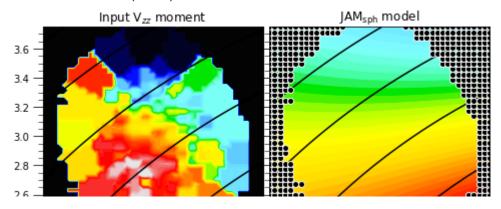
jam\_axi\_proj\_sph\_zz (analytic\_los=False) elapsed time sec: 1.46
inc=80.0; beta[0]=0.50; kappa=1.00; M/L=1.01; BH=1.0e+08; chi2/D0F=5.85

Total mass MGE (MSun): 2.655e+12



Inclination of 90 degrees

jam\_axi\_proj\_sph\_zz (analytic\_los=False) elapsed time sec: 1.51 inc=90.0; beta[0]=0.50; kappa=1.00; M/L=1.00; BH=1.0e+08; chi2/D0F=5.86 Total mass MGE (MSun): 2.664e+12



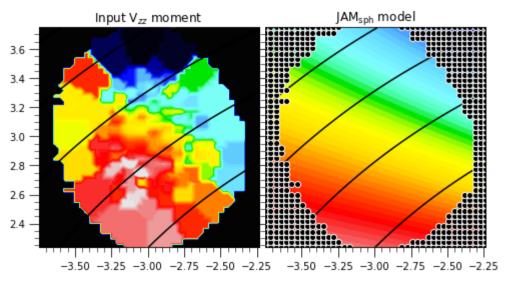
take it at 40 degrees and vary beta

```
In [101...
          # try for a different value of beta
             Copyright (C) 2019-2021, Michele Cappellari
             E-mail: michele.cappellari at physics.ox.ac.uk
             Updated versions of the software are available from my web page
             http://purl.org/cappellari/software
          CHANGELOG
          _____
         V1.1.0: MC, Oxford, 16 July 2020
             - Compute both Vrms and LOS velocity.
         V1.0.1: MC, Oxford, 21 April 2020
             - Made a separate file
         V1.0.0: Michele Cappellari, Oxford, 08 November 2019
              - Written and tested
          import numpy as np
          import matplotlib.pyplot as plt
          from jampy.jam axi proj import jam axi proj
          from jampy.jam axi proj import rotate points
          from plotbin.plot velfield import plot velfield
          #np.random.seed(123)
         #xbin, ybin = np.random.uniform(low=[-55, -40], high=[55, 40], size=[1000, 2]
         What do I do for inclination?
         \#inclinations = [40.,45.,50.,55.,60.,65.,70.,75.,80.,85.,90.]
                                                                             # Assu
          inc = 40.
         \#r = np.sgrt(xbin**2 + (ybin/np.cos(np.radians(inc)))**2) \# Radius in the pla
         \#a = 40
                                                                  # Scale length in a
         \#vr = 2000*np.sqrt(r)/(r + a)
                                                                  # Assumed velocity
         #vel = vr * np.sin(np.radians(inc))*xbin/r
                                                                 # Projected velocit
         \#sig = 8700/(r + a)
                                                                  # Assumed velocity
         \#rms = np.sqrt(vel^{**}2 + siq^{**}2)
                                                                  # Vrms field in km/
         # Until here I computed some fake input kinematics to fit with JAM.
         # Ina real application, instead of the above lines one will read the
         # measured stellar kinematics, e.g. from integral-field spectroscopy
          Open kinematics maps
         V = np.genfromtxt(file dir + obj name + ' V 2d.txt', delimiter=',')
         dV = np.genfromtxt(file_dir + obj_name + '_dV_2d.txt', delimiter=',')
         VD = np.genfromtxt(file dir + obj name + ' VD 2d.txt', delimiter=',')
         dVD = np.genfromtxt(file dir + obj name + ' dVD 2d.txt', delimiter=',')
         # compute rms velocity
         Vrms = np.sqrt(V**2 + VD**2)
```

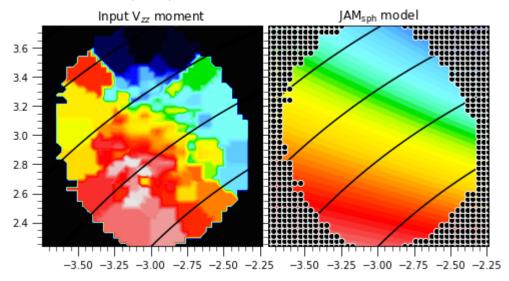
```
dVrms = np.sqrt((dV*V)**2 + (dVD*VD)**2)/Vrms
1.1.1
x and y bins (pixels)
# write the grid of xbins and ybins with (0,0) at the center and the x-axis c
\# set x and y bins so that center is (0, 0)
size = V.shape[0]
xbin arcsec = np.linspace(-np.floor(size/2), np.floor(size/2), size) * scale
ybin arcsec = np.linspace(-np.floor(size/2), np.floor(size/2), size) * scale
# set PA from mean photometry fitting
PA = theta mean
# set new arrays with the rotated coordinates
xbin rot = np.zeros(size)
ybin rot = np.zeros(size)
# rotate the coordinates and append to array
for i in range(len(xbin arcsec)):
    for j in range(len(ybin arcsec)):
        x new, y new = rotate points(xbin arcsec[i], ybin arcsec[j], PA)
        xbin rot[i] = x new
        ybin rot[j] = y new
xbin, ybin = np.meshgrid(xbin rot, ybin rot)
1.1.1
flatten data and bins
V = V.flatten()
dV = dV.flatten()
VD = VD.flatten()
dVD = dVD.flatten()
Vrms = Vrms.flatten()
dVrms = dVrms.flatten()
xbin = xbin.flatten()
ybin = ybin.flatten()
surface density
# take the surface density, etc from mge
surf = surf_density # surf dens list[2] <- this was with psf 0.75</pre>
sigma = sigma #sigma list[2]
q0bs = q #q list[2]
from astropy.cosmology import Planck18 as cosmo # Planck 2018
# redshift, convert to angular diameter dist in Mpc
z = 0.195
distance = cosmo.angular diameter distance(z).value
mbh = 1e8 # Black hole mass in solar masses
# try different beta # TBD
betas = np.arange(0.05, 0.5, 0.05)
# Below I assume mass follows light, but in a real application one
# will generally include a dark halo in surf pot, sigma pot, gobs pot.
```

```
# See e.g. Cappellari (2013) for an example
# https://ui.adsabs.harvard.edu/abs/2013MNRAS.432.1709C
surf lum = surf pot = surf
sigma lum = sigma pot = sigma
qobs lum = qobs pot = q0bs
sigmapsf = 0.75
sigmapsf = np.atleast 1d(sigmapsf)
sigmaX2 = sigma lum**2 + sigmapsf[:, None]**2
sigmaY2 = (sigma lum*qobs lum)**2 + sigmapsf[:, None]**2
\#normpsf = [0.7, 0.3]
pixsize = scale #0.8
goodbins = np.isfinite(Vrms) # take finite data
run JAM
# I use a loop below, just to higlight the fact that all parameters
# remain the same for the two JAM calls, except for 'moment' and 'data'
plt.figure(1)
reduced chi squared = np.zeros((len(betas)))
i=0
for beta in betas:
    print('##############")
    print(f'Beta={beta}')
    beta = np.full like(surf, beta)
    #for moment, data, errors in zip(['zz', 'z'], [Vrms, V], [dVrms, dV]):
         print(f'Moment {moment}')
    moment = 'zz'
    data = Vrms
    errors = dVrms
    # The model is by design similar but not identical to the adopted kinemat
    m = jam axi proj(surf lum, sigma lum, qobs lum, surf pot, sigma pot, qobs
                    inc, mbh, distance, xbin, ybin, plot=True, data=data, er
                    sigmapsf=sigmapsf, #normpsf=normpsf,
                    beta=beta, pixsize=pixsize,
                    moment=moment, goodbins=goodbins,
                    align='sph', ml=None, nodots=True)
    plt.pause(3)
    plt.figure(2)
    surf_pot *= m.ml # Scale the density by the best fitting M/L from the pr
    reduced chi squared[i] = m.chi2
    i = i+1
# plot the inclinations
fig, axs = plt.subplots()
axs.plot(betas, reduced chi squared)
axs.set ylabel(r'Reduced $\chi^2$')
axs.set xlabel(r'$\beta$')
Beta=0.05
```

```
Beta=0.05
jam_axi_proj_sph_zz (analytic_los=False) elapsed time sec: 1.69
inc=40.0; beta[0]=0.050; kappa=1.00; M/L=1.01; BH=1.0e+08; chi2/D0F=4.36
Total mass MGE (MSun): 1.648e+12
```

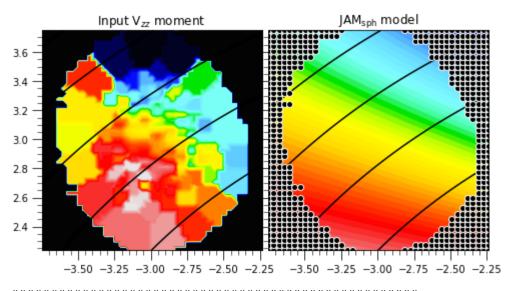


jam\_axi\_proj\_sph\_zz (analytic\_los=False) elapsed time sec: 1.74 inc=40.0; beta[0]=0.10; kappa=1.00; M/L=1.01; BH=1.0e+08; chi2/D0F=4.37 Total mass MGE (MSun): 1.669e+12



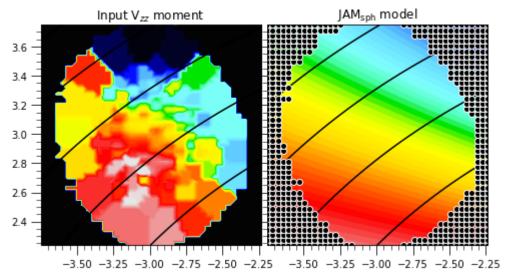
## 

Beta=0.150000000000000002



## Beta=0.2

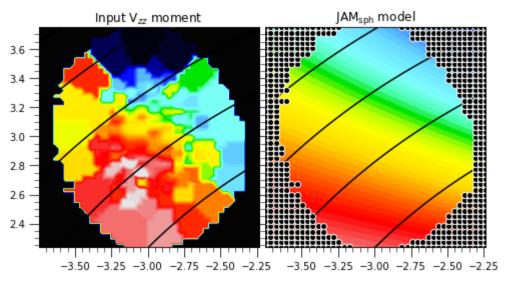
jam\_axi\_proj\_sph\_zz (analytic\_los=False) elapsed time sec: 1.86
inc=40.0; beta[0]=0.20; kappa=1.00; M/L=1.02; BH=1.0e+08; chi2/D0F=4.39
Total mass MGE (MSun): 1.720e+12



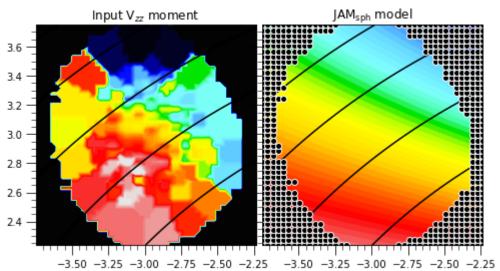
## 

## Beta=0.25

 $\label{localize} $$ jam_axi_proj_sph_zz $ (analytic_los=False) elapsed time sec: 1.72 inc=40.0; beta[0]=0.25; kappa=1.00; M/L=1.02; BH=1.0e+08; chi2/D0F=4.41 Total mass MGE (MSun): 1.751e+12$ 



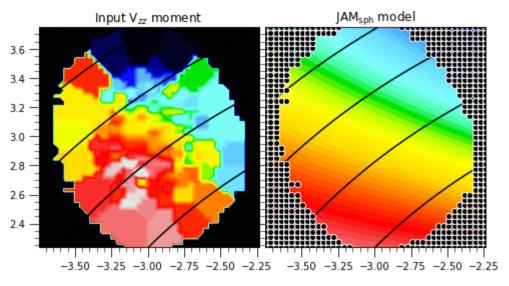
jam\_axi\_proj\_sph\_zz (analytic\_los=False) elapsed time sec: 1.68 inc=40.0; beta[0]=0.30; kappa=1.00; M/L=1.02; BH=1.0e+08; chi2/D0F=4.42 Total mass MGE (MSun): 1.786e+12



## 

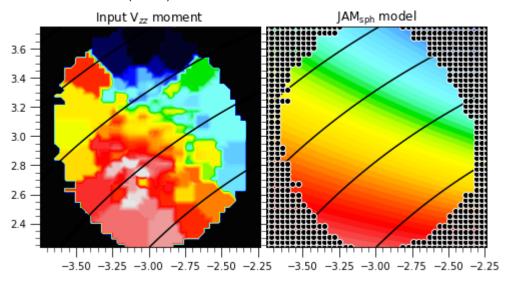
Beta=0.35000000000000003

jam\_axi\_proj\_sph\_zz (analytic\_los=False) elapsed time sec: 1.70
inc=40.0; beta[0]=0.35; kappa=1.00; M/L=1.02; BH=1.0e+08; chi2/D0F=4.45
Total mass MGE (MSun): 1.826e+12



#### Beta=0.4

jam\_axi\_proj\_sph\_zz (analytic\_los=False) elapsed time sec: 1.76 inc=40.0; beta[0]=0.40; kappa=1.00; M/L=1.03; BH=1.0e+08; chi2/D0F=4.47 Total mass MGE (MSun): 1.874e+12



## 

Beta=0.45

jam\_axi\_proj\_sph\_zz (analytic\_los=False) elapsed time sec: 1.65 inc=40 0 heta[0]=0 45 kanna=1 00 M/L=1 03 RH=1 0e+08 chi2/DOF=4 50

In [31]: V = np.genfromtxt(file\_dir + obj\_name + '\_V\_2d.txt', delimiter=',')
plt.imshow(V)

Out[31]: <matplotlib.image.AxesImage at 0x7ff85c8ce210>

```
10 -
15 -
20 -
25 -
```

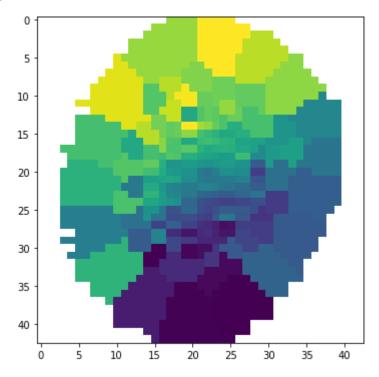
```
In [47]: #The image is flipped vertically!!!
```

 ${\tt Out[47]:}$  '\nThe image is flipped vertically!!!! This was so weird to try to figure ou t.\n'

```
In [51]: V = V.flatten()
V = V.reshape(43,43)
plt.imshow(V)

#Does it get flipped in JAM?
```

Out[51]: <matplotlib.image.AxesImage at 0x7ff85c285610>



```
In [ ]:
```