Problem1

```
In [76]: data1 = [0,1,2,4,5,5,7,10,10,12,13,17,39]
          1.a
In [77]: def mean(data):
              mean1 = sum(data)/len(data)
              return round(mean1,3)
In [78]: mean(data1)
Out[78]: 9.0
         The mean is 9.0
In [79]: def variance(data):
              variance1 = 0
              for i in data:
                  variance1 = variance1 + (i-mean(data))**2
              variance1 = variance1/len(data)
              return round(variance1,3)
In [80]: | variance1 = variance(data1)
In [81]:
          std_dev1 = variance1**0.5
In [82]:
          "%.3f" % std_dev1
Out[82]:
         '9.790'
         The standard deviation is 9.79
```

1.b

```
In [83]: data1b = sorted(data1)
In [84]: data1b
Out[84]: [0, 1, 2, 4, 5, 5, 7, 10, 10, 12, 13, 17, 39]
```

the 1st quatile

```
def first_quartile(data):
In [85]:
              if (len(data) + 1) % 4 == 0:
                  return data[(len(data) + 1) / 4 - 1]
              else:
                  yushu = (len(data) + 1) % 4
                  weishu = (len(data) + 1) / 4
                  return (data[weishu-1]*(1-float(yushu)/4) + data[weishu]*(float(yushu)/4))
        "%.3f" % first_quartile(data1b)
In [86]:
Out[86]: '3.000'
         The first quatile is 3.0
         the 3rd quatile
In [87]: def third_quartile(data):
              if (len(data) + 1)*3 % 4 == 0:
                  return data[(len(data) + 1)*3 / 4 - 1]
              else:
                  yushu = (len(data) + 1)*3 % 4
                  weishu = (len(data) + 1)*3 / 4
                  return (data[weishu-1]*(1-float(yushu)/4) + data[weishu]*(float(yushu)/4))
In [88]:
          "%.3f" % third_quartile(data1b)
         '12.500'
Out[88]:
         The third quatile is 12.5
In [89]:
         interquartile = third_quartile(data1b) - first_quartile(data1b)
         "%.3f" % interquartile
In [90]:
Out[90]: '9.500'
         The interquartile is 9.5
```

1.c

```
In [91]: def mode(data):
    a = []
    a1 = []
    for i in data:
        if i not in a:
            a.append(i)
    b = [0]*len(a)
    for i in range(len(a)):
        for ii in data:
            if a[i] == ii:
                b[i] += 1
    for i in range(len(b)):
        if b[i] == max(b):
            a1.append(a[i])
    return a1
```

```
In [92]: mode(data1)
```

Out[92]: [5, 10]

The mode is 5 and 10

1.d

```
In [93]: f = open("./data.freeway.txt", "r")
```

```
In [94]: all_text = f.read()
```

```
In [95]: all_text
 Out[95]: 'Timestamp\tSpeed (mph)\tOccupancy (%)\n05/23/2016 00:00\t62.3\t6.7\n05/23/20
          16 00:05\t62.7\t5\n05/23/2016 00:10\t62.5\t5.4\n05/23/2016 00:15\t63.5\t4.5\n
          05/23/2016 00:20\t64.3\t4.8\n05/23/2016 00:25\t63.9\t4.2\n05/23/2016 00:30\t6
          4.1\t4.2\n05/23/2016 00:35\t63\t3.8\n05/23/2016 00:40\t63.1\t3.4\n05/23/2016
           00:45\t63.7\t3.3\n05/23/2016 00:50\t63.5\t3.3\n05/23/2016 00:55\t63.4\t3\n0
          5/23/2016 01:00\t62.8\t3.6\n05/23/2016 01:05\t63\t3.1\n05/23/2016 01:10\t62.8
          \t3.7\n05/23/2016 01:15\t63.6\t3\n05/23/2016 01:20\t61.9\t3.6\n05/23/2016 01:
          25\t62.5\t2.9\n05/23/2016 01:30\t62.7\t3.1\n05/23/2016 01:35\t63.3\t3\n05/23/
          2016 01:40\t61.3\t3.6\n05/23/2016 01:45\t62.9\t2.6\n05/23/2016 01:50\t62.8\t
          2.9\n05/23/2016 01:55\t61.4\t3\n05/23/2016 02:00\t60.3\t3.6\n05/23/2016 02:05
          \t63.3\t2.8\n05/23/2016 02:10\t63.3\t3\n05/23/2016 02:15\t63.8\t2.6\n05/23/20
          16 02:20\t62.9\t3.3\n05/23/2016 02:25\t63\t2.6\n05/23/2016 02:30\t63\t2.7\n0
          5/23/2016 02:35\t63.6\t2.7\n05/23/2016 02:40\t63.9\t3\n05/23/2016 02:45\t63.2
          \t2.8\n05/23/2016 02:50\t63\t2.7\n05/23/2016 02:55\t63.2\t2.6\n05/23/2016 03:
          00\t63.1\t3.2\n05/23/2016 03:05\t63.3\t2.6\n05/23/2016 03:10\t63.4\t2.6\n05/2
          3/2016 03:15\t63.1\t2.6\n05/23/2016 03:20\t62.9\t3.3\n05/23/2016 03:25\t63.1
          \t2.7\n05/23/2016 03:30\t63.1\t3.3\n05/23/2016 03:35\t63.4\t3.3\n05/23/2016 0
          3:40\t63.3\t3.4\n05/23/2016 03:45\t63.4\t3.8\n05/23/2016 03:50\t65\t3.4\n05/2
          3/2016 03:55\t63.1\t4\n05/23/2016 04:00\t63.5\t3.1\n05/23/2016 04:05\t64.2\t
          2 01-05/22/2016 04.101+62 01+41-05/22/2016 04.151+62 01+4 11-05/22/2016 04.20
 In [96]: c = all_text.split("\n")
 In [97]: c.pop(0), c.pop(-1)
 Out[97]: ('Timestamp\tSpeed (mph)\tOccupancy (%)', '')
 In [98]:
          Timestamp =[0]*len(c)
          Speed = [0]*len(c)
          Occupancy = [0]*len(c)
          for i in range(len(c)):
              Timestamp[i] = c[i].split("\t")[0]
              Speed[i] = float(c[i].split("\t")[1])
              Occupancy[i] = float(c[i].split("\t")[2])
 In [99]:
          def median(data):
              if (len(data)+1)%2 ==0:
                  return data[(len(data)+1)/2]
              else:
                  return ((data[len(data)/2]+data[len(data)/2+1])/2)
          Speed1 = sorted(Speed)
In [100]:
          Q1= first_quartile(Speed1)
          Q3 = third_quartile(Speed1)
          Mean = mean(Speed1)
          Median = median(Speed1)
          Mode = mode(Speed1)
          "%.3f" % Q1
In [101]:
Out[101]: '35.700'
```

The first quatile is 35.7

In [102]: "%.3f" % Q3

Out[102]: '63.100'

The third quatile is 63.1

In [103]: "%.3f" % Median

Out[103]: '44.800'

The median is 44.8

In [104]: "%.3f" % Mean

Out[104]: '48.092'

The mean is 48.902

In [105]: Mode

Out[105]: [63.5]

The Mode is 63.5

1.e

Since the mean is larger than the median, the distribution has a positive skewness.

Probelm 2

2.a

Since J=q/(q+r+s)

In [106]: J = round((42),3)/(42+30+38)

```
"%.3f" % J
In [107]:
Out[107]: '0.382'
           The Jaccard coefficient is 0.382
           2.b
           Suppose Jack, Jim and Mary are the 1st, 2nd and 3rd in the following column
           let Y and P be 1, N be 0
In [108]: disease = [0]*3
           disease[0] = [1,1,1,1,0,0]
           disease[1] = [1,0,1,0,0,0]
           disease[2] = [1,1,0,1,0,0]
In [109]: disease
Out[109]: [[1, 1, 1, 1, 0, 0], [1, 0, 1, 0, 0, 0], [1, 1, 0, 1, 0, 0]]
           For asymmetric data, we use the (r+s)/(q+r+s) to evaluate dissimilarity
           since r+s = whole-q-t, and q+r+s = whole-t
In [110]:
          def dissimilarity(data):
               dissimilarity = [[] for i in range(len(data))]
               for i in range(len(data)):
                    for ii in range(len(data)):
                        if i > ii :
                            q = 0
                            t = 0
                            for iii in range(len(data[i])):
                                if data[i][iii]==1 and data[ii][iii]==1:
                                     q += 1
                                if data[i][iii]==0 and data[ii][iii]==0:
                                     t += 1
                            dissimilarity[i].append(float((len(data[0])-q-t))/(len(data[0])-t)
                        if i == ii:
                            dissimilarity[i].append(0)
               return dissimilarity
In [111]: | dissimilarity(disease)
Out[111]: [[0], [0.5, 0], [0.25, 0.75, 0]]
```

```
http://localhost:8888/notebooks/Desktop/COURSE/CS412%20Datamining/HW/HW1.ipynb#
```

We can find the 1st and 3rd patient have the lest disimilarity 0.25

So we can determine they have the same disease

2.c

For category data, we take 3 more features in the data matrix

```
In [113]: bi_dis = dissimilarity(matrix)
```

Suppose excellent is 3, good is 2, fair is 1

```
For ordinal variables, use Z = (ri-1)/(M-1), which means: excellemt = (3-1)/(3-1) = 1
```

```
good = (2-1)/(3-1) = 0.5
fair = (1-1)/(3-1) = 0
```

suppose the weights of each feature is 0.5

```
In [117]: mixed_dis = [[] for i in range(len(nu_dis))]
           for i in range(len(nu dis)):
               for ii in range(len(nu dis[i])):
                   mixed dis[i].append(bi_dis[i][ii]*0.5 + nu_dis[i][ii]*0.5)
In [118]: mixed_dis
Out[118]: [[0.0], [1.0, 0.0], [0.5, 1.0, 0.0], [0.75, 0.25, 0.75, 0.0]]
          2.d
In [119]: def eucl_dist(a,b):
               distance = 0
               for i in range(len(a)):
                   distance += (a[i]-b[i])**2
               return round(float(distance)**0.5,3)
In [120]: def manh dist(a,b):
               distance = 0
               for i in range(len(a)):
                   distance += abs((a[i]-b[i]))
               return round(distance,3)
In [121]: def mink_dist(a,b):
               distance = 0
               for i in range(len(a)):
                   if distance < abs((a[i]-b[i])):</pre>
                       distance = abs((a[i]-b[i]))
               return round(distance,3)
In [122]: A = [4,4,2]
           B = [-3, 2, 6]
           print "the Euclidean distance is "
           print eucl_dist(A,B)
           print "the Manhattan distance is "
           print manh dist(A,B)
           print "the Minkowski distance is "
           print mink dist(A,B)
          the Euclidean distance is
          8.307
          the Manhattan distance is
          13.0
          the Minkowski distance is
          7.0
```

```
2.e
In [123]: | def cos_sim(a,b):
               vector = 0
               A len = 0
               B len = 0
               for i in range(len(a)):
                   vector += a[i]*b[i]
                   A_{len} += a[i]**2
                   B len += b[i]**2
               return round(vector/((float(A_len)**0.5)*(float(B_len)**0.5)),3)
In [124]:
           f2 = open("./home.txt", "r")
In [125]:
          text = f2.read()
In [126]:
           text
           'Geo-ID\tPlace\t% of Homes Built 2000 to 2009\t% of Homes Built 1990 to 1999
Out[126]:
```

\t% of Homes Built 1980 to 1989\t% of Homes Built 1970 to 1979\t% of Homes Bu ilt 1960 to 1969\t% of Homes Built 1950 to 1959\t% of Homes Built 1940 to 194 9\t% of Homes Built 1939 or earlier\t% of Homes No bed rooms\t% of Homes 1 be d rooms\t% of Homes 2 bed rooms\t% of Homes 3 bed rooms\t% of Homes 4 bed ro oms\t% of Homes 5 or more bed rooms\n16000us0600135\tAcalanes Ridge\t3\t9\t10 \t3\t47\t14\t0\t14\t4\t0\t9\t47\t34\t5\n16000us0600156\tAcampo\t81\t0\t0\t0\t 0\t0\t19\t0\t0\t0\t0\t10\t0\t0\t0\n16000us0600212\tActon\t25\t41\t12\t3\t3\t3\t 1\t12\t0\t1\t11\t43\t36\t9\n16000us0600296\tAdelanto\t33\t8\t8\t6\t3\t1\t2\t3 8\t1\t6\t16\t41\t28\t8\n16000us0600310\tAdin\t4\t26\t8\t9\t24\t3\t17\t8\t0\t8 \t26\t57\t9\t0\n16000us0600394\tAgoura Hills\t4\t37\t36\t10\t4\t2\t1\t7\t1\t8 \t16\t25\t36\t15\n16000us0600450\tAgua Dulce\t20\t28\t16\t5\t3\t3\t4\t21\t0\t 4\t11\t35\t39\t11\n16000us0600464\tAguanga\t43\t15\t29\t0\t0\t0\t0\t12\t0\t35 \t7\t46\t12\t0\n16000us0600478\tAhwahnee\t12\t19\t21\t9\t8\t7\t0\t24\t3\t5\t1 5\t51\t25\t2\n16000us0600562\tAlameda\t5\t11\t16\t16\t6\t7\t35\t4\t3\t20\t35 \t28\t12\t3\n05000us06001\tAlameda County\t8\t11\t17\t14\t13\t8\t21\t7\t4\t18 \t29\t30\t15\t4\n16000us0600618\tAlamo\t12\t22\t22\t12\t15\t8\t1\t9\t0\t1\t7 \t26\t45\t20\n16000us0600674\tAlbany\t5\t7\t8\t7\t8\t12\t39\t14\t0\t18\t48\t2 4\t7\t2\n16000us0600786\tAlderpoint\t15\t17\t41\t0\t0\t0\t26\t0\t15\t0\t54

```
In [127]: line = text.split("\n")
```

In [128]: line.pop(0),line.pop(-1)

Out[128]: ('Geo-ID\tPlace\t% of Homes Built 2000 to 2009\t% of Homes Built 1990 to 1999 \t% of Homes Built 1980 to 1989\t% of Homes Built 1970 to 1979\t% of Homes Built 1960 to 1969\t% of Homes Built 1950 to 1959\t% of Homes Built 1940 to 1949\t% of Homes Built 1939 or earlier\t% of Homes No bed rooms\t% of Homes 1 bed room s\t% of Homes 2 bed rooms\t% of Homes 3 bed rooms\t% of Homes 4 bed rooms\t% of Homes 5 or more bed rooms',
''')

```
In [129]: Geo_ID = [0]*len(line)
          Place = [0]*len(line)
          area = [[] for i in range(len(line))]
          for i in range(len(line)):
              Geo_ID[i] = line[i].split("\t")[0]
              Place[i] = line[i].split("\t")[1]
              for ii in range(2,len(line[i].split("\t"))):
                   area[i].append(int(line[i].split("\t")[ii]))
In [130]: Alto = [0,0,12,34,14,21,13,5,0,30,41,23,3,2]
In [131]: cos_ans = [[] for i in range(len(area))]
          for i in range(len(area)):
              cos_ans[i].append(cos_sim(Alto,area[i]))
              cos_ans[i].append(Geo_ID[i])
              cos_ans[i].append(Place[i])
          import numpy as np
In [132]:
          def sort_by_col(data,icol):
              data1 = np.array(data).tolist()
              data1.sort(key=lambda x:x[icol])
              return np.array(data1)
In [133]: ans = sort by col(cos ans, 0)
In [134]: for i in range(1,6):
              print ans[-i]
          ['0.927' '16000us0604870' 'Bell']
          ['0.924' '16000us0604996' 'Bell Gardens']
          ['0.923' '16000us0608954' 'Burbank']
          ['0.919' '16000us0602980' 'Ashland']
          ['0.915' '16000us0603209' 'August']
```

Problem 3

3.a

zi=(xi-min(x))/(max(x)-min(x))

```
In [376]: def norm(data):
               data1 = [0]*len(data)
               for i in range(len(data)):
                   data1[i] = round(float((data[i]-min(data)))/(max(data)-min(data)),3)
               return data1
           empl[1] = norm(empl[1])
In [378]:
           empl[2] = norm(empl[2])
In [379]:
          empl
Out[379]: [[1, 2, 3, 4, 5],
            [0.0, 0.96, 1.0, 0.24, 0.72],
            [0.0, 0.556, 1.0, 0.444, 0.321]]
          3.b
          \sigma = (sum(X-mean)^2/n)^0.5
          z = (x-\mu)/\sigma
In [139]: def std norm(data,test):
               m = mean(data)
               pstd = variance(data)**0.5
               z = [0]*len(data)
               for i in range(len(data)):
                   z[i] = (data[i] - m)/pstd
               test = (test - m)/pstd
               return z, round(test,3)
In [140]: | std_speed, speed_55 = std_norm(Speed,55)
In [141]: mean(Speed), mean(std speed)
Out[141]: (48.092, -0.0)
In [142]: variance(Speed), variance(std_speed)
Out[142]: (200.021, 1.0)
In [108]: round(speed55,3)
Out[108]: 0.488
```

The mean of speed before normalization is 48.092 The mean of speed after normalization 0.0

The variance before normalization 200.021 The variance after normalization 1.0

The correspoding speed after normalization is 0.488

Problem 4

4.I.a

```
data = [[2.5,0.5,2.2,1.9,3.1,2.3,2,1.0,1.5,1.1],[2.4,0.7,2.9,2.2,3.0,2.7,1.6,1.1,1]
In [204]:
In [205]:
          A = data[0]
           B = data[1]
In [206]:
          A mean = mean(data[0])
           B_mean = mean(data[1])
           A_std = variance(data[0])**0.5
           B std = variance(data[1])**0.5
In [207]:
          AB = 0
           for i in range(len(A)):
               AB += A[i] * B[i]
In [209]:
          coefficient = (AB-len(A)*A mean*B mean)/(len(A)*A std*B std)
         round(coefficient,3)
In [211]:
Out[211]: 0.926
```

We can find the x-axis's data is highly related to the y-axis's data

4.I.b

If a data has a high variance in signal while low variance in noises, we need consider use the PCA.

Since the correlation is close to 1, which means x-axis's data is highly related to the y-axis's data, if we use the x-y basis, there would be high redundancy.

If we chose to use PCA, it would change the aspect and show the most difference in noise.

In this case, we should use PCA to do the job.

4.I.c

```
In [213]: covariance = AB/len(A)-A_mean*B_mean
In [215]: | round(covariance,3)
Out[215]: 0.554
          Since the Co-variance is higher than 0,
           data in X-axis rise with Y-axis.
          4.II
In [331]: a = [[1,-1,0,0],[1,0,0,-1]]
           m = len(a)
           n = len(a[0])
           for i in range(m):
               for ii in range(n):
                   a[i][ii] = a[i][ii] - mean(a[i])
In [344]: def transpose(data):
               data = [[row[col] for row in data] for col in range(len(data[0]))]
               return data
In [345]: def dot_mult(A, B):
               ans = [[0] * len(B[0]) for i in range(len(A))]
               for i in range(len(A)):
                   for ii in range(len(B[0])):
                       for iii in range(len(B)):
                           ans[i][ii] += A[i][iii] * B[iii][ii]
               return ans
In [346]: def cov(data):
               n = len(data[0])
               m = len(data)
               cov = [[0]*m for i in range(m)]
               for i in range(m):
                   for ii in range(m):
                       cov[i][ii] = dot_mult(data,transpose(data))[i][ii]/n
               return cov
In [335]: cov_a = cov(a)
```

```
In [336]: cov_a
Out[336]: [[0.5, 0.25], [0.25, 0.5]]
In [337]: from sympy import *
           def eigenvlaues(data):
                dat = data
                x = Symbol('x')
                for i in range(len(dat)):
                    dat[i][i] -= x
                a = Matrix(dat)
                print a.det()
                return solve(a.det(),x)
In [338]: | e_value = eigenvlaues(cov_a)
           x^{**2} - 1.0^*x + 0.1875
In [339]: e_value
Out[339]: [0.25000000000000, 0.750000000000000]
           When e value is 0.25, it would be cov a minus e value in the diagnol
           [[0.25,0.25],[0.25,0.25]]
           this means the eigenvector is [1,-1]
           When e value is 0.75, it would be cov a minus e value in the diagnol [[-0.25,0.25],[0.25,-0.25]]
           this means the eigenvector is [1,1]
In [340]: P = [[1,-1],[1,1]]
In [341]: Y = dot_mult(P,a)
In [342]: Y
Out[342]: [[0.0, -1.0, 0.0, 1.0], [2.0, -1.0, 0.0, -1.0]]
In [349]: cov_y = cov(Y)
In [350]: cov_y
Out[350]: [[0.5, 0.0], [0.0, 1.5]]
           Now the Y become a diagonal matrix
           since 1.5>0.5, the frist principle vector is the 2nd row
```

http://localhost:8888/notebooks/Desktop/COURSE/CS412%20Datamining/HW/HW1.ipynb#

if we make it norminalization

```
In [405]: P1 = [round((1**2+1**2)**0.5/2,3),round((1**2+1**2)**0.5/2,3)]
In [406]: P1
Out[406]: [0.707, 0.707]
```

4.II.b

The coordinate should be P[1]*a in 1-d space

```
In [407]: a_1d = [0]*4
for ii in range(4):
    a_1d[ii] = P1[0]*a[0][ii] + P1[0]*a[1][ii]
```

```
In [408]: a_1d
```

Out[408]: [1.414, -0.707, 0.0, -0.707]

4.II.C

we need to use transposed P[1]*a_1d to recover

```
In [409]: P_tran = [[0.707],[0.707]]
```

```
In [414]: a_recover
```

```
Out[414]: [[1.0, -0.5, 0.0, -0.5], [1.0, -0.5, 0.0, -0.5]]
```

```
In [412]: a
```

```
Out[412]: [[1.0, -1.0, 0.0, 0.0], [1.0, 0.0, 0.0, -1.0]]
```

After compare, we can find half of the data(2 of 4) can be recoverd.

```
In [ ]:
```