

### 3.d.1

If the outlook is sunny is true and humidity is high is true, then not play tennis +1;

If the outlook is sunny is true and humidity is high is false, then play tennis+1;

If the outlook is sunny is false, is overcast is true, then play tennis+1;

If the outlook is sunny is false, is overcast is false, and wind is strong is true, then not play tennis+1;

If the outlook is sunny is false, is overcast is false, and wind is strong is false, then play tennis+1.

### 3.d.2

You can set an n-channel root to n-1 true and another 1 false question;

## 4.

$$P(H|X) = P(X|H) * P(H)/P(X)$$

### 4.a

$$P(\text{play} = \text{"yes"}) = 9/14 = 0.643$$

$$P(\text{play} = \text{"no"}) = 5/14 = 0.357$$

### 4.b

For outlook:

$$P(O|\text{yes}) = 4/9 = 0.44$$

$$P(R|\text{yes}) = 3/9 = 0.33$$

$$P(S|\text{yes}) = 2/9 = 0.22$$

For temperature:

$$P(\text{Hot}|\text{yes}) = 2/9 = 0.22$$

$$P(\text{Mild}|\text{yes}) = 4/9 = 0.44$$

$$P(\text{Cool}|\text{yes}) = 3/9 = 0.33$$

For humidity:

$$P(\text{High}|\text{yes}) = 3/9 = 0.33$$

$$P(\text{Normal}|\text{yes}) = 6/9 = 0.67$$

For wind:

$$P(\text{Strong}|\text{yes}) = 3/9 = 0.33$$

$$P(\text{Weak}|\text{yes}) = 6/9 = 0.67$$

#### 4.C

For outlook:

$$P(O|no) = 0/5 = 0$$

$$P(R|no) = 2/5 = 0.4$$

$$P(S|no) = 3/5 = 0.6$$

For temperature:

$$P(Hot|no) = 2/5 = 0.4$$

$$P(Mild|no) = 2/5 = 0.4$$

$$P(Cool|no) = 1/5 = 0.2$$

For humidity:

$$P(High|no) = 4/5 = 0.8$$

$$P(Normal|no) = 1/5 = 0.2$$

For wind:

$$P(Strong|no) = 3/5 = 0.6$$

$$P(Weak|no) = 2/5 = 0.4$$

#### 4.d

For  $x_1 = [\text{overcast, hot, high, strong}]$ :

$$P(x_1|yes) = 0.44 * 0.22 * 0.33 * 0.33 = 0.01$$

$$p(x_1|no) = 0$$

$$P(yes|x_1) = 0.01 * 0.64 = 0.06$$

$$P(no|x_1) = 0$$

$x_1$  belongs to yes.

For  $x_2 = [\text{sunny, hot, normal, weak}]$ :

$$P(x_2|yes) = 0.22 * 0.22 * 0.67 * 0.67 = 0.022$$

$$p(x_2|no) = 0.6 * 0.4 * 0.2 * 0.4 = 0.019$$

$$P(yes|x_2) = 0.022 * 0.64 = 0.014$$

$$P(no|x_2) = 0.019 * 0.36 = 0.007$$

$x_2$  belongs to yes.

For  $x_3 = [\text{rain, mild, normal, strong}]$ :

$$P(x_3 | \text{yes}) = 0.33 * 0.44 * 0.67 * 0.33 = 0.032$$

$$p(x_3 | \text{no}) = 0.4 * 0.4 * 0.2 * 0.6 = 0.019$$

$$P(\text{yes} | x_3) = 0.032 * 0.64 = 0.020$$

$$P(\text{no} | x_3) = 0.019 * 0.36 = 0.007$$

$x_3$  belongs to yes.

For  $x_4 = [\text{overcast, cool, high, strong}]$ :

$$P(x_4 | \text{yes}) = 0.44 * 0.33 * 0.33 * 0.33 = 0.015$$

$$p(x_4 | \text{no}) = 0$$

$$P(\text{yes} | x_4) = 0.015 * 0.64 = 0.01$$

$$P(\text{no} | x_4) = 0$$

$x_4$  belongs to yes.

We can find the result are all “yes” for play tennis.

4.e

Confusion matrix:

Actual class/ predicted class	Play(predicted)	Not Play(predicted)
Play(actual)	2	0
Not Play(actual)	2	0

$$\text{Precision} = 2 / (2+2) = 0.5$$

$$\text{Recall} = 2 / (2+0) = 1$$

4.f

Decision Tree: Pros: Easy to understand

Cons: Poor accuracy for unseen samples

Naïve Bayes: Pros: Easy to implement

Cons: loss of accuracy