

Shay Lebovitz

4) a)

```
library(GPArotation)

data <- read.table('/Users/shaylebovitz/R/employment.txt', header = TRUE)
employment <- data[,1:7]

(employment_fa2 <- factanal(employment, 2))
```

```
##
## Call:
## factanal(x = employment, factors = 2)
##
## Uniquenesses:
##   AGR   MAN   CON   SER   FIN   SPS   TC
## 0.005 0.882 0.793 0.364 0.619 0.329 0.192
##
## Loadings:
##      Factor1 Factor2
## AGR -0.738  -0.671
## MAN  0.344
## CON           0.451
## SER           0.791
## FIN -0.268   0.556
## SPS  0.672   0.468
## TC   0.869  -0.230
##
##              Factor1 Factor2
## SS loadings      1.955   1.861
## Proportion Var    0.279   0.266
## Cumulative Var    0.279   0.545
##
## Test of the hypothesis that 2 factors are sufficient.
## The chi square statistic is 15.8 on 8 degrees of freedom.
## The p-value is 0.0453
```

b)

```
emp_loadings <- matrix(c(-0.738, 0.344, 0.060, 0.099, -0.268, 0.672, 0.869,
                        -0.671, -0.005, 0.451, 0.791, 0.556, 0.468, -0.230),
                      nrow = 7, ncol = 2)
t_emp_loadings <- matrix(c(-0.738, -0.671, 0.344, -0.005, 0.060, 0.451, 0.099,
                          0.791, -0.268, 0.556, 0.672, 0.468, 0.869, -0.230),
                        nrow = 2, ncol = 7)
(employment_fa2_cor <- emp_loadings %*% t_emp_loadings +
  + diag(employment_fa2$unique))
```

```
##           [,1]      [,2]      [,3]      [,4]      [,5]      [,6]      [,7]
```

```
## [1,] 0.999885 -0.250517 -0.346901 -0.6038230 -0.175292 -0.8099640 -0.4869920
## [2,] -0.250517 1.000222 0.018385 0.0301010 -0.094972 0.2288280 0.3000860
## [3,] -0.346901 0.018385 1.000055 0.3626810 0.234676 0.2513880 -0.0515900
## [4,] -0.603823 0.030101 0.362681 0.9995095 0.413264 0.4367160 -0.0958990
## [5,] -0.175292 -0.094972 0.234676 0.4132640 1.000383 0.0801120 -0.3607720
## [6,] -0.809964 0.228828 0.251388 0.4367160 0.080112 0.9991911 0.4763280
## [7,] -0.486992 0.300086 -0.051590 -0.0958990 -0.360772 0.4763280 0.9999779
```

```
cor(employment)
```

```
##          AGR          MAN          CON          SER          FIN          SPS
## AGR  1.0000000 -0.2543889 -0.34861031 -0.60471243 -0.17575329 -0.81147553
## MAN -0.2543889 1.00000000 -0.03445846 -0.03294004 -0.27374053 0.05028408
## CON -0.3486103 -0.03445846 1.00000000 0.47308319 -0.01802316 0.07200705
## SER -0.6047124 -0.03294004 0.47308319 1.00000000 0.37928368 0.38798122
## FIN -0.1757533 -0.27374053 -0.01802316 0.37928368 1.00000000 0.16601516
## SPS -0.8114755 0.05028408 0.07200705 0.38798122 0.16601516 1.00000000
## TC  -0.4873331 0.24290323 -0.05460530 -0.08489430 -0.39132021 0.47492344
##          TC
## AGR -0.4873331
## MAN 0.2429032
## CON -0.0546053
## SER -0.0848943
## FIN -0.3913202
## SPS 0.4749234
## TC 1.0000000
```

Overall these two correlation matrices are very similar, It appears as though pretty much every element is within 20% of each other. Thus, the factor analysis model appears to capture the observed correlations between the variables.

c)

```
print(employment_fa2$loadings, cutoff = 0.4)
```

```
##
## Loadings:
##      Factor1 Factor2
## AGR -0.738  -0.671
## MAN
## CON      0.451
## SER      0.791
## FIN      0.556
## SPS 0.672  0.468
## TC 0.869
##
##      Factor1 Factor2
## SS loadings      1.955 1.861
## Proportion Var    0.279 0.266
## Cumulative Var    0.279 0.545
```

```
print(factanal(employment, 2, rotation = "quartimax")$loadings, cutoff = 0.4)
```

```
##
## Loadings:
##      Factor1 Factor2
## AGR -0.991
```

```
## MAN
## CON
## SER 0.659 0.449
## FIN 0.568
## SPS 0.796
## TC 0.402 -0.804
##
##          Factor1 Factor2
## SS loadings 2.463 1.353
## Proportion Var 0.352 0.193
## Cumulative Var 0.352 0.545

print(factanal(employment, 2, rotation = "infomaxT")$loadings, cutoff= 0.4)
```

```
##
## Loadings:
##      Factor1 Factor2
## AGR -0.997
## MAN
## CON
## SER 0.585 0.542
## FIN 0.598
## SPS 0.816
## TC 0.518 -0.735
##
##          Factor1 Factor2
## SS loadings 2.473 1.343
## Proportion Var 0.353 0.192
## Cumulative Var 0.353 0.545
```

All these rotations have two rows with a non-zero loading in each column, which is not ideal. ‘quartimax’ and ‘infomaxT’ have essentially identical loading matrices. I believe the original (‘varimax’) loading matrix is the best, as it has 4 rows with a non-zero loading in just one column, whereas the other two have only 3 with that property.

d)

```
(employment_fa3 <- factanal(employment, 3))
```

```
##
## Call:
## factanal(x = employment, factors = 3)
##
## Uniquenesses:
##   AGR  MAN  CON  SER  FIN  SPS  TC
## 0.005 0.820 0.414 0.322 0.230 0.255 0.293
##
## Loadings:
##      Factor1 Factor2 Factor3
## AGR -0.902      -0.422
## MAN 0.220 -0.356
## CON      0.760
## SER 0.381 0.306 0.662
## FIN 0.216 0.847
## SPS 0.859
## TC 0.577 -0.588 -0.165
```

```
##
##               Factor1 Factor2 Factor3
## SS loadings    2.125   1.297   1.239
## Proportion Var  0.304   0.185   0.177
## Cumulative Var  0.304   0.489   0.666
##
## Test of the hypothesis that 3 factors are sufficient.
## The chi square statistic is 6.29 on 3 degrees of freedom.
## The p-value is 0.0984

emp_loadings3 <- matrix(c(-0.902, 0.220, 0.024, 0.381, 0.216, 0.859, 0.577,
                        0.062, -0.356, -0.089, 0.306, 0.847, -0.004, -0.588,
                        -0.422, 0.070, 0.760, 0.662, 0.078, 0.087, -0.165),
                        nrow = 7, ncol = 3)
t_emp_loadings3 <- matrix(c(-0.902, 0.062, -0.422, -0.220, -0.356, 0.070,
                        0.024, -0.089, 0.760, 0.381, 0.306, 0.662,
                        0.216, 0.847, 0.078, 0.859, -0.004, 0.087,
                        0.577, -0.588, -0.165), nrow = 3, ncol = 7)
(employment_fa3_cor <- emp_loadings3 %*% t_emp_loadings3 +
  + diag(employment_fa3$unique))

##           [,1]      [,2]      [,3]      [,4]      [,5]      [,6]      [,7]
## [1,]  1.000532  0.1468280 -0.347886 -0.6040540 -0.1752340 -0.811780 -0.4872800
## [2,] -0.250052  0.9028156  0.090164  0.0212240 -0.2485520  0.196494  0.3247180
## [3,] -0.347886  0.0796040  1.000435  0.4850300 -0.0109190  0.087092 -0.0592200
## [4,] -0.604054 -0.1464160  0.485030  0.9995255  0.3931140  0.383649 -0.0693210
## [5,] -0.175234 -0.3435920 -0.010919  0.3931140  0.9998512  0.188942 -0.3862740
## [6,] -0.811780 -0.1814660  0.087092  0.3836490  0.1889420  1.000679  0.4836400
## [7,] -0.487280  0.0708380 -0.059220 -0.0693210 -0.3862740  0.483640  0.9990704

cor(employment)

##           AGR          MAN          CON          SER          FIN          SPS
## AGR  1.0000000 -0.2543889 -0.34861031 -0.60471243 -0.17575329 -0.81147553
## MAN -0.2543889  1.0000000 -0.03445846 -0.03294004 -0.27374053  0.05028408
## CON -0.3486103 -0.03445846  1.00000000  0.47308319 -0.01802316  0.07200705
## SER -0.6047124 -0.03294004  0.47308319  1.00000000  0.37928368  0.38798122
## FIN -0.1757533 -0.27374053 -0.01802316  0.37928368  1.00000000  0.16601516
## SPS -0.8114755  0.05028408  0.07200705  0.38798122  0.16601516  1.00000000
## TC  -0.4873331  0.24290323 -0.05460530 -0.08489430 -0.39132021  0.47492344
##
##           TC
## AGR -0.4873331
## MAN  0.2429032
## CON -0.0546053
## SER -0.0848943
## FIN -0.3913202
## SPS  0.4749234
## TC   1.0000000
```

Again, we see that these two correlation matrices are extremely similar.

```
print (employment_fa3$loadings, cutoff = 0.4)
```

```
##
## Loadings:
##      Factor1 Factor2 Factor3
## AGR -0.902      -0.422
```

```
## MAN
## CON          0.760
## SER          0.662
## FIN          0.847
## SPS  0.859
## TC   0.577  -0.588
##
##          Factor1 Factor2 Factor3
## SS loadings    2.125    1.297    1.239
## Proportion Var    0.304    0.185    0.177
## Cumulative Var    0.304    0.489    0.666

print(factanal(employment, 3, rotation = "quartimax")$loadings, cutoff = 0.4)
```

```
##
## Loadings:
##      Factor1 Factor2 Factor3
## AGR -0.972
## MAN
## CON          0.740
## SER  0.481      0.545
## FIN          0.865
## SPS  0.854
## TC   0.583  -0.551
##
##          Factor1 Factor2 Factor3
## SS loadings    2.373    1.318    0.970
## Proportion Var    0.339    0.188    0.139
## Cumulative Var    0.339    0.527    0.666

print(factanal(employment, 3, rotation = "infomaxT")$loadings, cutoff= 0.4)
```

```
##
## Loadings:
##      Factor1 Factor2 Factor3
## AGR -0.896      -0.436
## MAN
## CON          0.765
## SER          0.640
## FIN          0.863
## SPS  0.855
## TC   0.617  -0.560
##
##          Factor1 Factor2 Factor3
## SS loadings    2.122    1.322    1.216
## Proportion Var    0.303    0.189    0.174
## Cumulative Var    0.303    0.492    0.666
```

Here, we see that all three rotations yield loadings with 4 rows with just one non-zero loading. Similarly, all three rotations contain at least $m = 3$ zeros in each column, and all three have two rows with two non-zero factors. From this perspective, I don't think that one rotation is clearly better than the others, they all seem very even.

e)

```
employment_fa1 <- factanal(employment, 1)
(phi <- 1 - c(sum(employment_fa1$unique), sum(employment_fa2$unique),
```

```
sum(employment_fa3$unique))/7)
```

```
## [1] 0.3532472 0.5451621 0.6657872
```

Based on these results, I would chose a model with three factors and use the 'varimax' rotation. Choosing $m = 2$ yields a Phi value of 0.55, which is too small. Even having $m = 3$ (Phi = 0.67) is a little small. As discussed earlier, there doesn't seem to be much of a difference between the loading rotations for a three factor model. For a three factor model with the 'varimax' rotation, we see that Factor 1 greatly predicts AGR, and SPS, as well as TC to a lesser extent. Factor 2 greatly predicts FIN, and TC again to a lesser extent. Factor 3 has a small predictive effect on AGR, and decent effect on SER and FIN. No factor significantly predicts MAN. Off the top of my head, I cannot think of a realistic representation of these factors, as it is unclear what agriculture, social services, and transport/communications would have in common, or what factor would determine finance and transport but is uncorrelated with Factor 1.

5) a)

```
apps <- read.table('/Users/shaylebovitz/R/applicants.txt', header = TRUE)
#m <= 3
apps_fa1 <- factanal(apps, 1)
apps_fa2 <- factanal(apps, 2)
apps_fa3 <- factanal(apps, 3)
(phi <- 1 - c(sum(apps_fa1$unique), sum(apps_fa2$unique), sum(apps_fa3$unique))/7)
```

```
## [1] 0.6432686 0.7813120 0.8333725
```

```
phi[-1] - phi[-3]
```

```
## [1] 0.13804337 0.05206048
```

```
apps_fa1$PVAL
```

```
## objective
## 0.000105917
```

```
apps_fa2$PVAL
```

```
## objective
## 0.03630386
```

```
apps_fa3$PVAL
```

```
## objective
## 0.3521931
```

Based on this analysis, I would say 2 factors is appropriate for this model, as they explain 78% of the variance, and it is also the last statistically significant P-value.

b)

```
print(apps_fa2$loadings, cutoff = 0.4)
```

```
##
## Loadings:
##      Factor1 Factor2
## Lik          0.667
## Con 0.868
## Luc 0.824
## Sal 0.902
## Dri 0.756  0.409
## Amb 0.856
```

```
## Ent          0.946
##
##              Factor1 Factor2
## SS loadings    3.693   1.776
## Proportion Var  0.528   0.254
## Cumulative Var  0.528   0.781
```

```
apps_fa2$uniquenesses
```

```
##      Lik      Con      Luc      Sal      Dri      Amb      Ent
## 0.5117955 0.2091670 0.2571750 0.1105795 0.2618704 0.1752284 0.0050000
```

```
1-apps_fa2$uniquenesses
```

```
##      Lik      Con      Luc      Sal      Dri      Amb      Ent
## 0.4882045 0.7908330 0.7428250 0.8894205 0.7381296 0.8247716 0.9950000
```

For a two factor model, we see that **Ent** has an extremely high communality, which suggests that its variance is highly explained by the factors. Most others have a relatively high communality, with **Con**, **Luc**, **Sal**, **Dri**, and **Amb** all having communalities > 0.74 . **Lik** has a lower communality of 0.49, suggesting the factor model isn't as applicable to it.

c)

```
print (apps_fa2$loadings, cutoff = 0.4)
```

```
##
## Loadings:
##      Factor1 Factor2
## Lik          0.667
## Con 0.868
## Luc 0.824
## Sal 0.902
## Dri 0.756   0.409
## Amb 0.856
## Ent          0.946
##
##              Factor1 Factor2
## SS loadings    3.693   1.776
## Proportion Var  0.528   0.254
## Cumulative Var  0.528   0.781
```

```
print(factanal(apps, 2, rotation = "quartimax")$loadings, cutoff = 0.4)
```

```
##
## Loadings:
##      Factor1 Factor2
## Lik          0.597
## Con  0.889
## Luc  0.861
## Sal  0.942
## Dri  0.832
## Amb  0.904
## Ent  0.536   0.841
##
##              Factor1 Factor2
## SS loadings    4.346   1.123
## Proportion Var  0.621   0.160
```

```
## Cumulative Var    0.621    0.781
print(factanal(apps, 2, rotation = "infomaxT")$loadings, cutoff= 0.4)
```

```
##
## Loadings:
##      Factor1 Factor2
## Lik          0.634
## Con 0.886
## Luc 0.850
## Sal 0.930
## Dri 0.803
## Amb 0.888
## Ent 0.438    0.896
##
##              Factor1 Factor2
## SS loadings      4.083    1.386
## Proportion Var   0.583    0.198
## Cumulative Var   0.583    0.781
```

Here, we see that ‘quartimax’ and ‘infomaxT’ are essentially identical in terms of their loading matrices. They both have one non-zero loading element for every row except Ent. The ‘varimax’ rotation is similar: it has one non-zero loading element for every row except Dri. I believe the original ‘varimax’ rotation is the best because it is the only one with both columns containing at least 2 zeros.

d)

```
print(factanal(apps, 2, rotation = "oblimin")$loadings, cutoff = 0.4)
```

```
##
## Loadings:
##      Factor1 Factor2
## Lik          0.702
## Con 0.939
## Luc 0.865
## Sal 0.949
## Dri 0.728
## Amb 0.884
## Ent          0.989
##
##              Factor1 Factor2
## SS loadings      3.842    1.521
## Proportion Var   0.549    0.217
## Cumulative Var   0.549    0.766
```

```
print(factanal(apps, 2, rotation = "promax")$loadings, cutoff= 0.4)
```

```
##
## Loadings:
##      Factor1 Factor2
## Lik          0.710
## Con 0.942
## Luc 0.867
## Sal 0.951
## Dri 0.726
## Amb 0.885
## Ent          1.000
```



```
##
##               Factor1 Factor2
## SS loadings    3.854    1.554
## Proportion Var  0.551    0.222
## Cumulative Var  0.551    0.773

print(factanal(apps, 2, rotation = "infomaxQ")$loadings, cutoff = 0.4)
```

```
##
## Loadings:
##      Factor1 Factor2
## Lik          0.731
## Con  0.930
## Luc  0.852
## Sal  0.934
## Dri  0.702
## Amb  0.867
## Ent          1.029
##
##               Factor1 Factor2
## SS loadings    3.715    1.654
## Proportion Var  0.531    0.236
## Cumulative Var  0.531    0.767
```

All three of these rotated loading matrices are essentially the same. Factor 1 has non-zero loadings in Con, Luc, Sal, Dri, and Amb, whereas Factor 2 has non-zero loadings in Lik and Ent. All of the loading elements are of similar magnitude as well. Thus there is no clear optimal choice.

e) It looks like the oblique rotations give a better loading matrix than the orthogonal rotations. I will randomly choose 'oblimin', as all the oblique rotations are essentially the same.

```
factor1 <- factanal(apps, 2, rotation = "oblimin")$loadings[,1]
factor2 <- factanal(apps, 2, rotation = "oblimin")$loadings[,2]
cor(factor1, factor2)
```

```
## [1] -0.973436
```

Factor 1 relates to self-confidence, lucidity, salesmanship, drive, and ambition, whereas Factor 2 relates to likeability and enthusiasm. Because it is an oblique rotation, Factor 2 is not necessarily uncorrelated with Factor 1. We see that Factor 1 and Factor 2 are highly negatively correlated, with a correlation of -0.97. Thus, whatever underlying factor increases confidence, lucidity, salesmanship, drive, and ambition yields decreases in likeability and enthusiasm.

6) a)

```
anx <- read.csv('/Users/shaylebovitz/R/anxiety.csv', header = TRUE)
anx <- as.matrix(anx[,-1])
(anx_fa2 <- factanal(factors = 2, covmat = list(cov = anx, n.obs = 335)))
```

```
##
## Call:
## factanal(factors = 2, covmat = list(cov = anx, n.obs = 335))
##
## Uniquenesses:
##      x1      x2      x3      x4      x5      x6      x7      x8      x9      x10     x11     x12     x13
## 0.607 0.594 0.644 0.565 0.483 0.721 0.461 0.488 0.520 0.746 0.431 0.564 0.650
##      x14     x15     x16     x17     x18     x19     x20
## 0.559 0.357 0.388 0.471 0.539 0.569 0.562
```

```
##
## Loadings:
##      Factor1 Factor2
## [1,] 0.542  0.315
## [2,] 0.592  0.235
## [3,] 0.288  0.522
## [4,] 0.471  0.462
## [5,] 0.115  0.710
## [6,] 0.276  0.450
## [7,] 0.375  0.631
## [8,] 0.665  0.266
## [9,] 0.657  0.219
## [10,] 0.454  0.219
## [11,] 0.697  0.289
## [12,] 0.584  0.308
## [13,] 0.509  0.302
## [14,] 0.408  0.524
## [15,] 0.686  0.415
## [16,] 0.733  0.275
## [17,] 0.315  0.655
## [18,] 0.617  0.284
## [19,] 0.565  0.335
## [20,] 0.523  0.405
##
##              Factor1 Factor2
## SS loadings      5.592  3.490
## Proportion Var   0.280  0.175
## Cumulative Var   0.280  0.454
##
## Test of the hypothesis that 2 factors are sufficient.
## The chi square statistic is 287.5 on 151 degrees of freedom.
## The p-value is 1.47e-10
```

```
print(anx_fa2$loadings, cutoff = 0.4)
```

```
##
## Loadings:
##      Factor1 Factor2
## [1,] 0.542
## [2,] 0.592
## [3,]      0.522
## [4,] 0.471  0.462
## [5,]      0.710
## [6,]      0.450
## [7,]      0.631
## [8,] 0.665
## [9,] 0.657
## [10,] 0.454
## [11,] 0.697
## [12,] 0.584
## [13,] 0.509
## [14,] 0.408  0.524
## [15,] 0.686  0.415
## [16,] 0.733
## [17,]      0.655
```

```
## [18,] 0.617
## [19,] 0.565
## [20,] 0.523    0.405
##
##           Factor1 Factor2
## SS loadings      5.592   3.490
## Proportion Var   0.280   0.175
## Cumulative Var   0.280   0.454
```

Only 4 out of the 20 rows of the loading matrix have a non-zero entry in each column, and thus the vast majority only have one non-zero loading. So it's off to a good start.

```
anx_fa1 <- factanal(factors = 1, covmat = list(cov = anx, n.obs = 335))
anx_fa3 <- factanal(factors = 3, covmat = list(cov = anx, n.obs = 335))
(phi <- 1 - c(sum(anx_fa1$unique), sum(anx_fa2$unique), sum(anx_fa3$unique))/20)
```

```
## [1] 0.4103534 0.4540977 0.4771117
```

Here, we see that two factors only explain roughly 45% of the correlation matrix, which is not adequate. This is enough information to declare that 2 factors is not appropriate for this model.

b)

```
anx_fa2_quart <- factanal(factors = 2,
                        covmat = list(cov = anx, n.obs = 335),
                        rotation = "quartimax")
anx_fa2_infoT <- factanal(factors = 2,
                        covmat = list(cov = anx, n.obs = 335),
                        rotation = "infomaxT")
anx_fa2_obl <- factanal(factors = 2,
                      covmat = list(cov = anx, n.obs = 335),
                      rotation = "oblimin")
anx_fa2_pro <- factanal(factors = 2,
                      covmat = list(cov = anx, n.obs = 335),
                      rotation = "promax")
anx_fa2_infoQ <- factanal(factors = 2,
                      covmat = list(cov = anx, n.obs = 335),
                      rotation = "infomaxQ")
print(anx_fa2$loadings, cutoff = 0.4) # overlap, 0 empty
```

```
##
## Loadings:
##           Factor1 Factor2
## [1,] 0.542
## [2,] 0.592
## [3,]      0.522
## [4,] 0.471   0.462
## [5,]      0.710
## [6,]      0.450
## [7,]      0.631
## [8,] 0.665
## [9,] 0.657
## [10,] 0.454
## [11,] 0.697
## [12,] 0.584
## [13,] 0.509
## [14,] 0.408   0.524
```

```
## [15,] 0.686 0.415
## [16,] 0.733
## [17,] 0.655
## [18,] 0.617
## [19,] 0.565
## [20,] 0.523 0.405
##
##          Factor1 Factor2
## SS loadings      5.592  3.490
## Proportion Var   0.280  0.175
## Cumulative Var   0.280  0.454

print(anx_fa2_quart$loadings, cutoff = 0.4) # 2 overlap, 0 empty
```

```
##
## Loadings:
##          Factor1 Factor2
## [1,] 0.627
## [2,] 0.629
## [3,] 0.515
## [4,] 0.641
## [5,] 0.462 0.551
## [6,] 0.467
## [7,] 0.645
## [8,] 0.707
## [9,] 0.677
## [10,] 0.502
## [11,] 0.746
## [12,] 0.659
## [13,] 0.591
## [14,] 0.619
## [15,] 0.802
## [16,] 0.770
## [17,] 0.606 0.402
## [18,] 0.675
## [19,] 0.657
## [20,] 0.657
##
##          Factor1 Factor2
## SS loadings      8.170  0.912
## Proportion Var   0.409  0.046
## Cumulative Var   0.409  0.454
```

```
print(anx_fa2_infoT$loadings, cutoff = 0.4) # 3 overlap, 1 empty
```

```
##
## Loadings:
##          Factor1 Factor2
## [1,] 0.596
## [2,] 0.629
## [3,] 0.451
## [4,] 0.557
## [5,] 0.670
## [6,]
## [7,] 0.498 0.539
```

```
## [8,] 0.706
## [9,] 0.689
## [10,] 0.490
## [11,] 0.742
## [12,] 0.635
## [13,] 0.560
## [14,] 0.509    0.427
## [15,] 0.758
## [16,] 0.774
## [17,] 0.445    0.575
## [18,] 0.662
## [19,] 0.622
## [20,] 0.596
##
##               Factor1 Factor2
## SS loadings      6.951   2.131
## Proportion Var   0.348   0.107
## Cumulative Var   0.348   0.454
```

```
print(anx_fa2_obl$loadings, cutoff = 0.4) # no overlap, 1 empty
```

```
##
## Loadings:
##           Factor1 Factor2
## [1,] 0.565
## [2,] 0.660
## [3,]      0.478
## [4,] 0.417
## [5,]      0.799
## [6,]
## [7,]      0.563
## [8,] 0.740
## [9,] 0.749
## [10,] 0.491
## [11,] 0.771
## [12,] 0.620
## [13,] 0.527
## [14,]      0.415
## [15,] 0.708
## [16,] 0.823
## [17,]      0.625
## [18,] 0.672
## [19,] 0.586
## [20,] 0.505
##
##               Factor1 Factor2
## SS loadings      6.011   2.104
## Proportion Var   0.301   0.105
## Cumulative Var   0.301   0.406
```

```
print(anx_fa2_pro$loadings, cutoff = 0.4) # no overlap, 1 empty
```

```
##
## Loadings:
##           Factor1 Factor2
```

```
## [1,] 0.551
## [2,] 0.671
## [3,]      0.544
## [4,]
## [5,]      0.911
## [6,]      0.451
## [7,]      0.639
## [8,] 0.751
## [9,] 0.771
## [10,] 0.489
## [11,] 0.781
## [12,] 0.612
## [13,] 0.512
## [14,]      0.470
## [15,] 0.686
## [16,] 0.840
## [17,]      0.711
## [18,] 0.673
## [19,] 0.569
## [20,] 0.467
##
##               Factor1 Factor2
## SS loadings      5.865   2.719
## Proportion Var   0.293   0.136
## Cumulative Var   0.293   0.429
```

```
print(anx_fa2_infoQ$loadings, cutoff = 0.4) # 1 overlap, no empty
```

```
##
## Loadings:
##       Factor1 Factor2
## [1,] 0.516
## [2,] 0.653
## [3,]      0.612
## [4,]      0.403
## [5,] -0.421   1.007
## [6,]      0.509
## [7,]      0.721
## [8,] 0.732
## [9,] 0.760
## [10,] 0.469
## [11,] 0.758
## [12,] 0.580
## [13,] 0.478
## [14,]      0.537
## [15,] 0.638
## [16,] 0.821
## [17,]      0.797
## [18,] 0.647
## [19,] 0.532
## [20,] 0.414
##
##               Factor1 Factor2
## SS loadings      5.415   3.454
## Proportion Var   0.271   0.173
```

```
## Cumulative Var    0.271    0.443
```

Based on the amount of overlap (non-zero element in both Factors) and empty (both factors have zero loading), I would choose either 'oblimin' or 'promax'. I'll go with 'oblimin'.

c)

```
print(anx_fa2_obl$loadings, cutoff = 0.4)
```

```
##
## Loadings:
##      Factor1 Factor2
## [1,]  0.565
## [2,]  0.660
## [3,]           0.478
## [4,]  0.417
## [5,]           0.799
## [6,]
## [7,]           0.563
## [8,]  0.740
## [9,]  0.749
## [10,] 0.491
## [11,] 0.771
## [12,] 0.620
## [13,] 0.527
## [14,]           0.415
## [15,] 0.708
## [16,] 0.823
## [17,]           0.625
## [18,] 0.672
## [19,] 0.586
## [20,] 0.505
##
##      Factor1 Factor2
## SS loadings    6.011    2.104
## Proportion Var    0.301    0.105
## Cumulative Var    0.301    0.406
```

Firstly, it is important to note that because 'oblimin' is an oblique rotation, the factors are likely correlated. Factor 1 is a decent measure of x1, x2, x4, x8, x9, x10, x11, x12, x13, x15, x18, x19, and x20, while Factor 2 is a measure of x3, x5, x7, x14, and x17. Neither factor explains x6 well. Since all the variables seem very related (all related to anxiety during test-taking), I cannot think of what these underlying factors might be.