

High Performance Computing

ADVANCED SCIENTIFIC COMPUTING

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LECTURE 6

Parallel Programming with OpenMP

September 26th, 2017

Room TG-227



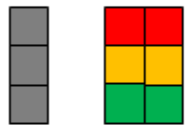
UNIVERSITY OF ICELAND
SCHOOL OF ENGINEERING AND NATURAL SCIENCES

FACULTY OF INDUSTRIAL ENGINEERING,
MECHANICAL ENGINEERING AND COMPUTER SCIENCE



Review of Lecture 5 – Parallel Algorithms & Data Structures

■ Using MPI Collectives



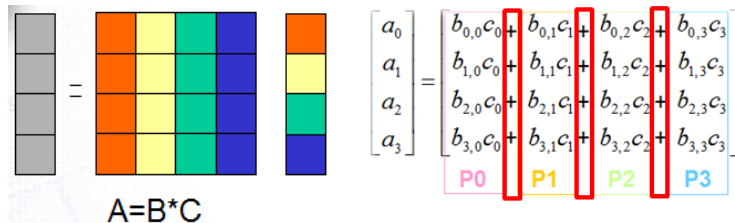
$$Z = X + Y$$

```
MPI_Scatter(x,CHUNK,MPI_DOUBLE,xpart,CHUNK,MPI_DOUBLE,0,MPI_COMM_WORLD);
MPI_Scatter(y,CHUNK,MPI_DOUBLE,ypart,CHUNK,MPI_DOUBLE,0,MPI_COMM_WORLD);
```

```
for (i=0; i<CHUNK; i++)
    zpart[i] = xpart[i] + ypart[i];
```

```
/* Collect the result */
```

```
MPI_Gather(zpart,CHUNK,MPI_DOUBLE,z,CHUNK,MPI_DOUBLE,0,MPI_COMM_WORLD);
```



```
/* Scatter matrix B */
```

```
MPI_Scatter(B,NCOLS,MPI_FLOAT,Bpart,NCOLS,MPI_FLOAT,0,MPI_COMM_WORLD);
```

```
/* Scatter vector C */
```

```
MPI_Scatter(C,1,MPI_FLOAT,Cpart,1,MPI_FLOAT, 0,MPI_COMM_WORLD);
```

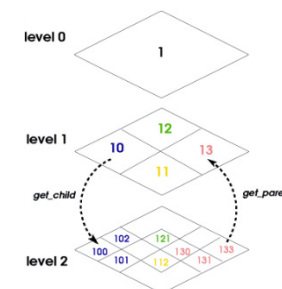
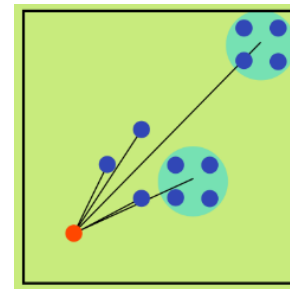
```
/* Do the vector-scalar multiplication */
```

```
for(j=0; j < NCOLS; j++)
    Apart[j] = Cpart[0] * Bpart[j];
```

```
/* Reduce to matrix A */
```

```
MPI_Reduce(Apart,A,NCOLS,MPI_FLOAT,MPI_SUM, 0,MPI_COMM_WORLD);
```

■ Tree-Code Approaches



■ MPI Derived Datatypes

```
MPI_Type_contiguous( 3, oldtype, newtype );
```

```
MPI_Type_vector( 5, 2, 3, oldtype, newtype );
```

```
array_of_blocklengths[] = {2,3,1,2,2,2} /* below BL */
array_of_displacements[] = {3,9,12,15,18} /* below DIS */
```

```
MPI_Type_indexed ( 6, array_of_blocklengths, array_of_displacements, oldtype, newtype);
```



[1] Parallel Algorithms

[2] PEPC Webpage

Outline of the Course

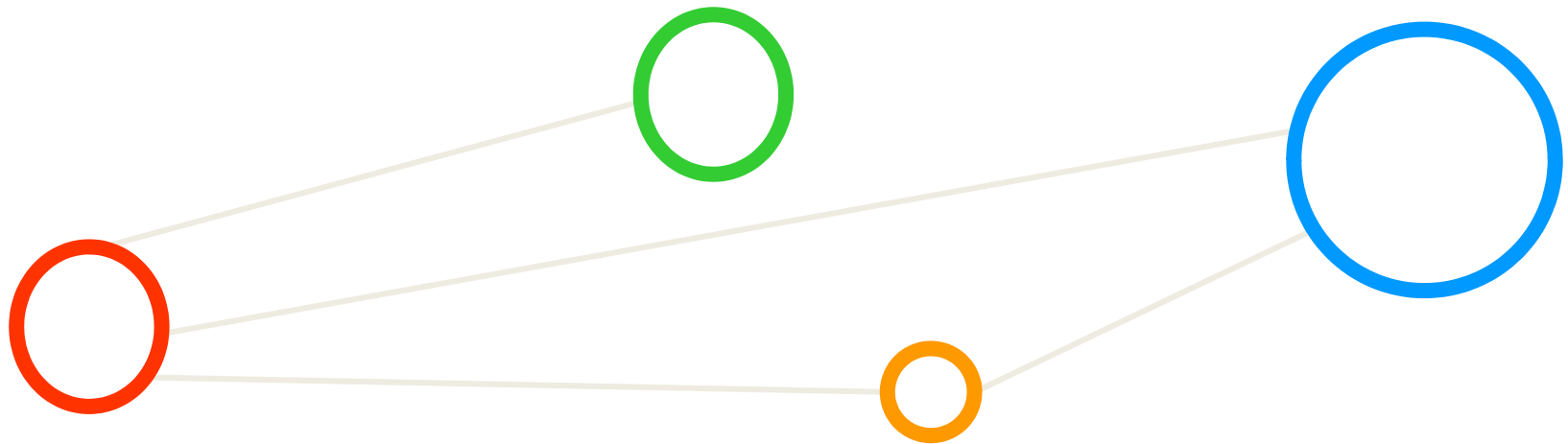
1. High Performance Computing
 2. Parallelization Fundamentals
 3. Parallel Programming with MPI
 4. Advanced MPI Techniques
 5. Parallel Algorithms & Data Structures
 6. Parallel Programming with OpenMP
 7. Hybrid Programming & Patterns
 8. Debugging & Profiling Techniques
 9. Performance Optimization & Tools
 10. Scalable HPC Infrastructures & GPUs
 11. Scientific Visualization & Steering
 12. Terrestrial Systems & Climate
 13. Systems Biology & Bioinformatics
 14. Molecular Systems & Libraries
 15. Computational Fluid Dynamics
 16. Finite Elements Method
 17. Machine Learning & Data Mining
 18. Epilogue
- + additional practical lectures for our hands-on exercises in context

Outline

- Shared-Memory Programming Concepts
 - Parallel and Serial Regions
 - Fork/Join & Master and Worker Threads
 - Standard & Portability
 - Hybrid Programming Motivation
 - Scientific Application Examples
- OpenMP Parallel Programming Basics
 - Basic building blocks
 - Local/shared variables & Loops
 - Synchronization & Critical Regions
 - Jacobi 2D Application Example
 - Selected Comparisons with MPI & Evolutions

- Promises from previous lecture(s):
- **Lecture 1:** Lecture 6 will give in-depth details on the shared-memory programming model with OpenMP
- **Lecture 2:** Lecture 6 about OpenMP will include 'data parallelism on loops' methods that are useful here
- **Lecture 5:** Lecture 6 provides a detailed introduction to OpenMP used for shared memory programming

Shared-Memory Programming Concepts



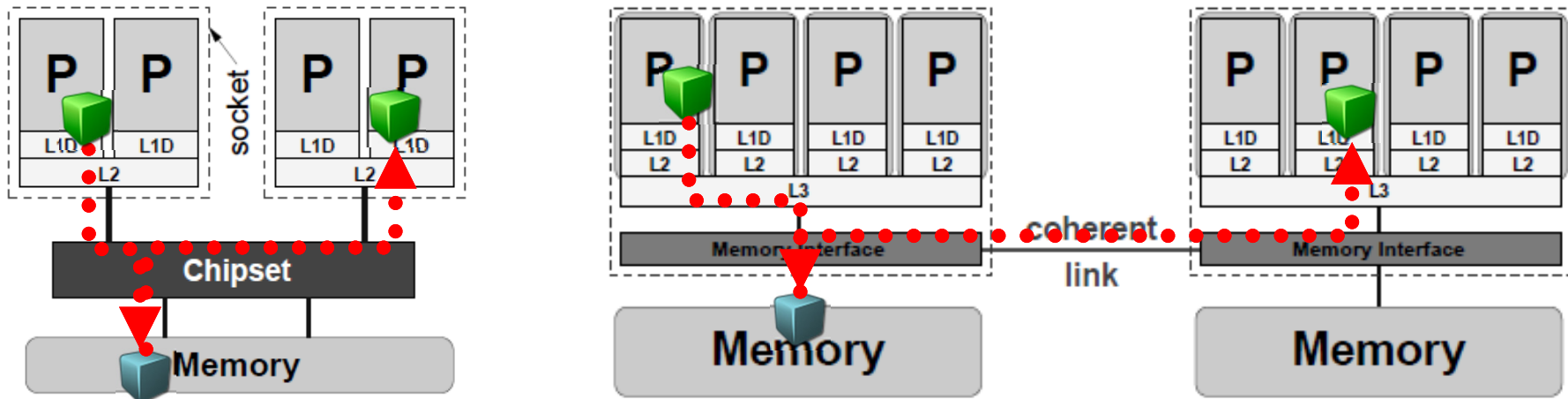
Shared-Memory Computers: Reviewed

- A shared-memory parallel computer is a system in which a number of CPUs work on a common, shared physical address space

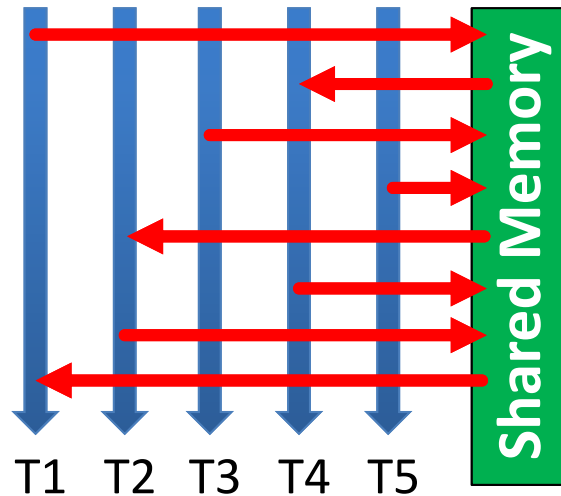
[3] Introduction to High Performance Computing for Scientists and Engineers

- Two varieties of shared-memory systems:
 1. Unified Memory Access (UMA)
 2. Cache-coherent Nonuniform Memory Access (ccNUMA)

(programming model: work on shared address space – ‘local access to memory’)



Programming with Shared Memory using OpenMP



- Shared-memory programming enables immediate access to all data from all processors without explicit communication
- OpenMP is dominant shared-memory programming standard today (v3)

[4] OpenMP API Specification

- OpenMP is a set of **compiler directives** to ‘mark parallel regions’
- Bindings are defined for C, C++, and Fortran languages
- Threads TX are ‘**lightweight processes**’ that mutually access data
- (Shared-Memory concept itself is very old, like POSIX Threads)

What is OpenMP?

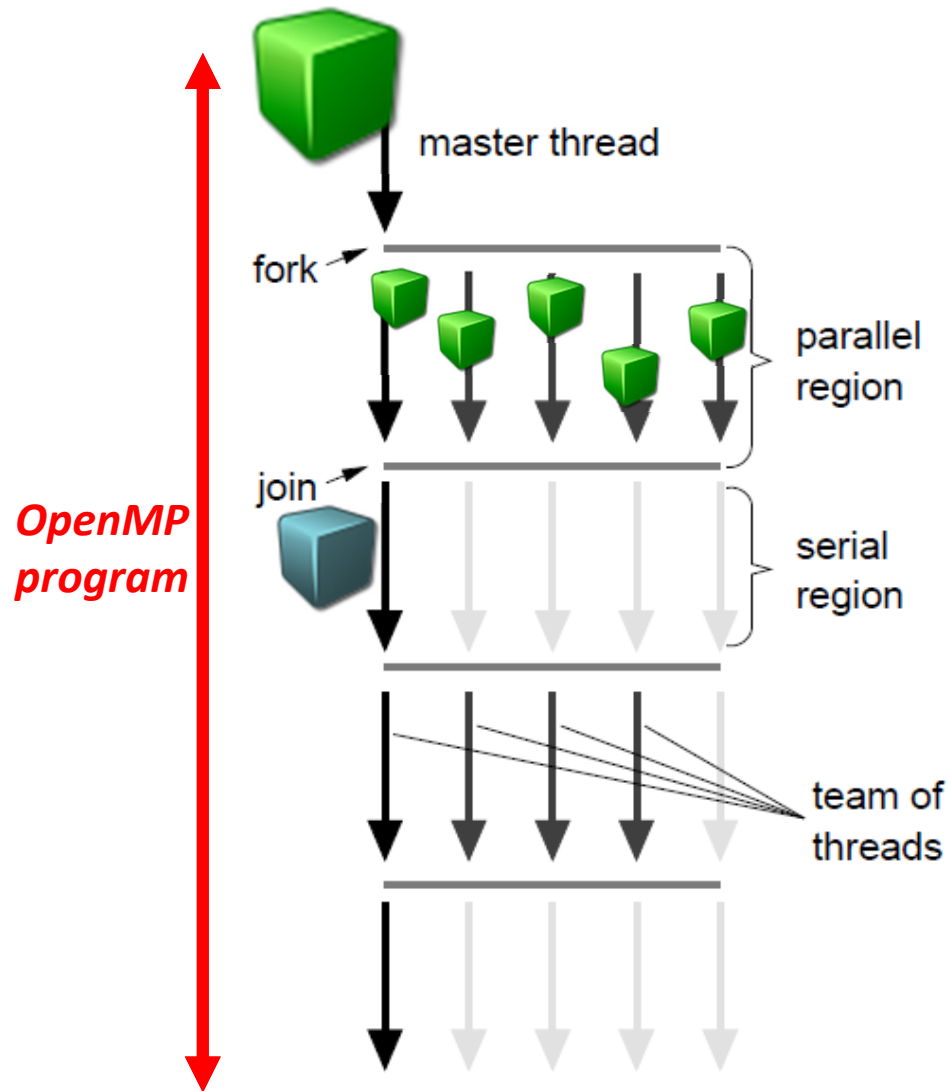
- OpenMP is a library for specifying ‘parallel regions in serial code’
 - Defined by major computer hardware/software vendors → **portability!**
 - Enable **scalability** with parallelization constructs w/o fixed thread numbers
 - Offers a **suitable data environment** for easier parallel processing of data
 - Uses **specific environment variables** for clever decoupling of code/problem
 - Included in standard C compiler distributions (e.g. gcc)
- Threads are the central entity in OpenMP
 - Threads enable ‘work-sharing’ and **share address space (where data resides)**
 - Threads can be synchronized if needed
 - Lightweight process that share common address space with other threads
 - **Initiating (aka ‘spawning’) n threads is less costly than n processes (e.g. variable space)**



- Recall ‘computing nodes’ are independent computing processors (that may also have N cores each) and that are all part of one big parallel computer
- Threads are lightweight processes that work with data in memory

Parallel and Serial Regions

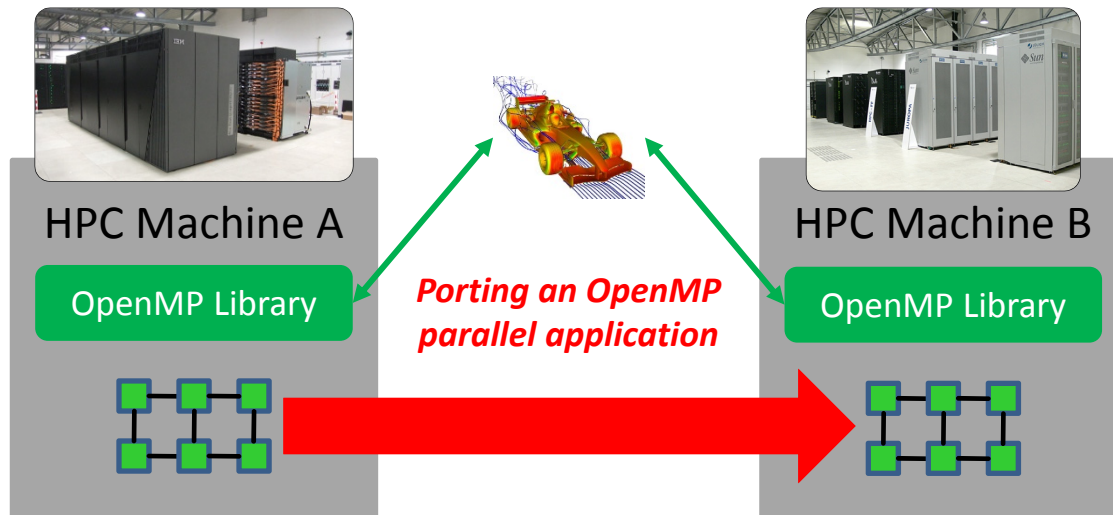
modified from [3] Introduction to High Performance Computing for Scientists and Engineers



- `fork()` initiated by master thread (exists always) creates team of threads
- Team of threads concurrently work on shared-memory data actively in parallel regions
- `join()` initiates the 'shutdown' of the parallel region and terminates team of threads
- Team of threads maybe also put to sleep until next parallel region begins
- Number of threads can be different in each parallel region

OpenMP Standard enables Portability

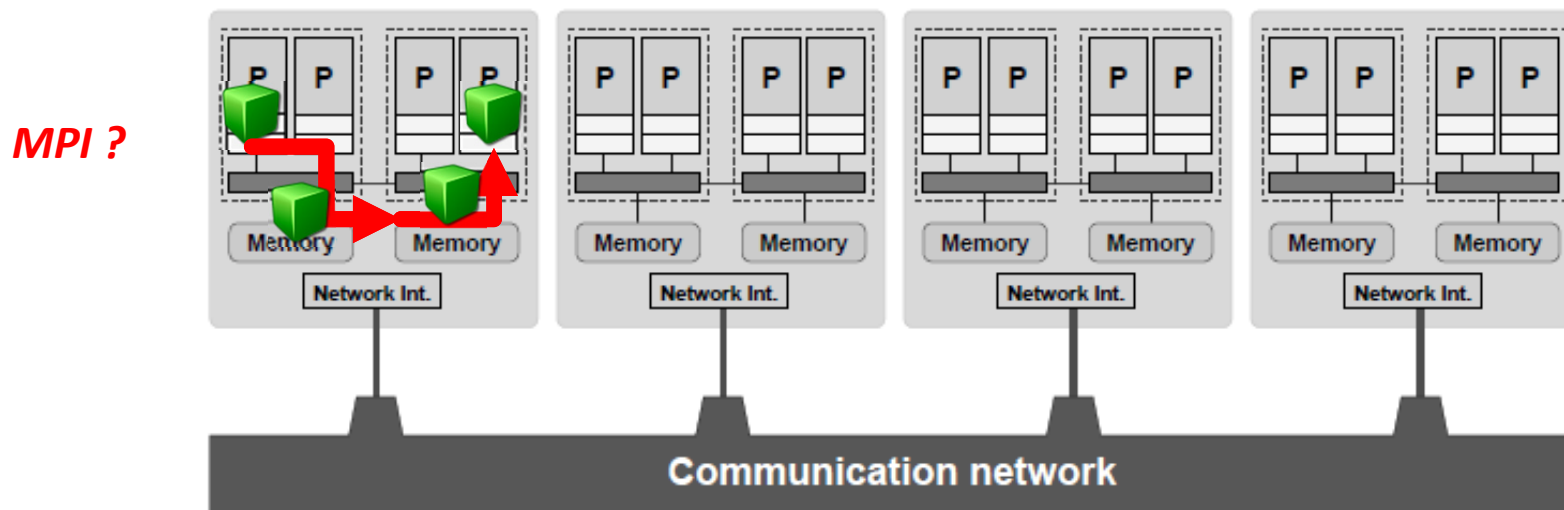
- Key **reasons** for requiring a standard programming library
 - **Technical advancement** in supercomputers is extremely fast
 - Parallel computing experts switch organizations and **face another system**
- Applications using proprietary libraries where **not portable**
 - Create whole **applications from scratch** or **time-consuming code updates**
- OpenMP is **parallel programming model** for UMA and ccNUMA



- OpenMP is an open standard that significantly supports the portability of parallel shared-memory applications
- But different vendors might implement it differently

Programming Hybrid Systems – Motivation

- Inefficient ‘on-node communications’
 - MPI uses ‘buffering techniques’ to transfer data (cf. Lecture 3 & 4)
 - Transfers may require ‘multiple memory copies’ to get data from A to B
 - Comparable to a ‘memory copy’ between different MPI processes



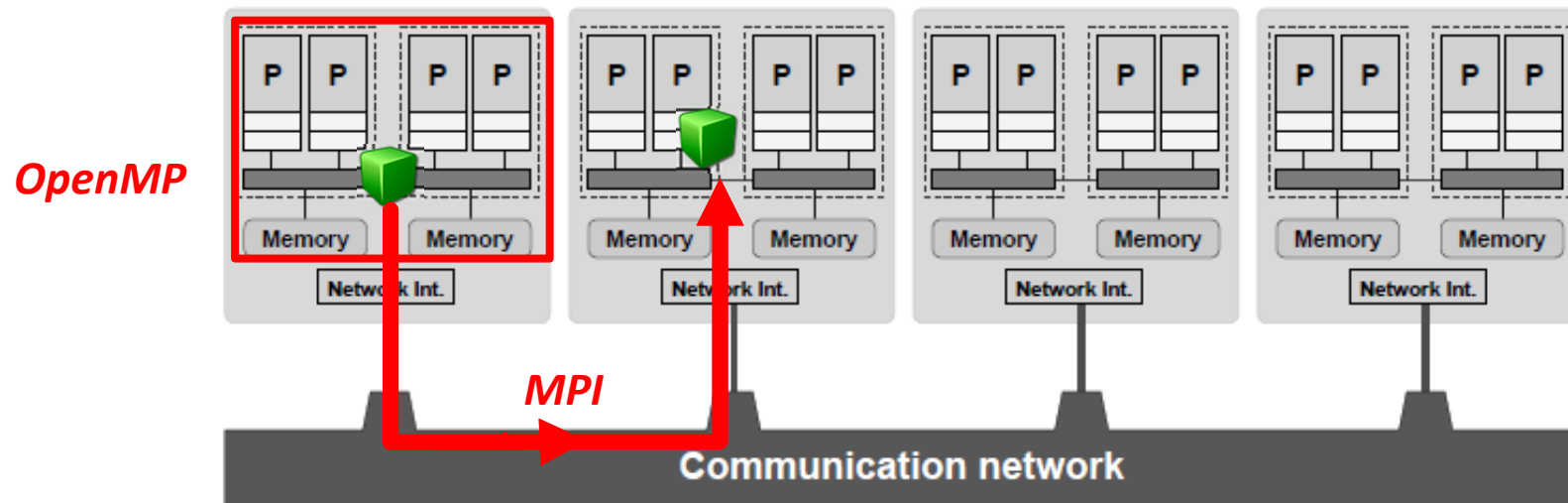
modified from [3] Introduction to High Performance Computing for Scientists and Engineers

- Take advantage of shared memory techniques where feasible
 - OpenMP threads can read memory on the same node

Hierarchical Hybrid Computers – Revisited

- A hierarchical hybrid parallel computer is neither a purely shared-memory nor a purely distributed-memory type system but a mixture of both
- Large-scale ‘hybrid’ parallel computers have shared-memory building blocks interconnected with a fast network today

[3] Introduction to High Performance Computing for Scientists and Engineers

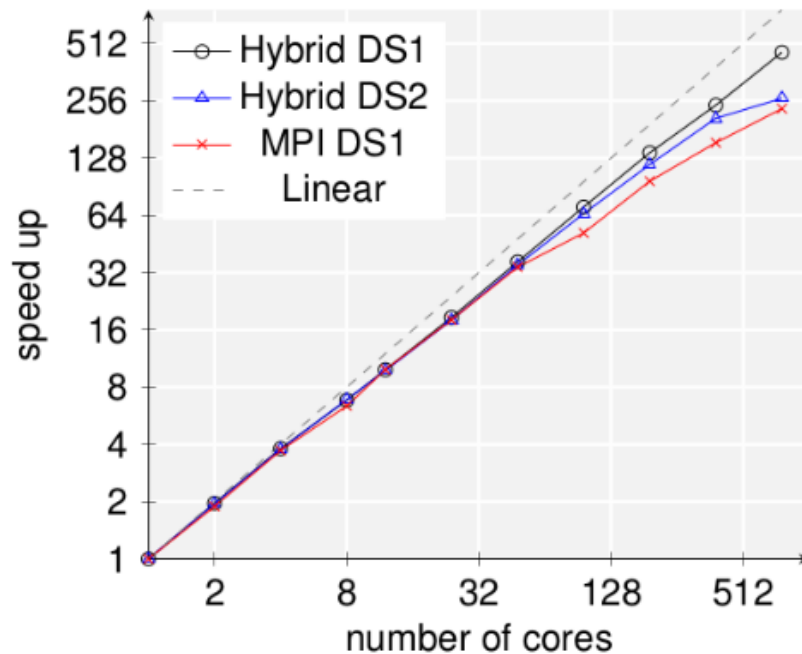


- Shared-memory nodes (i.e. ccNUMA) with local Network Int. (NI)
 - NI mediates connections to other remote ‘SMP nodes’

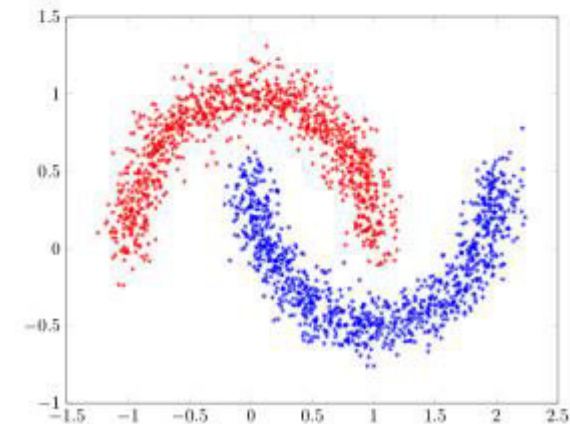
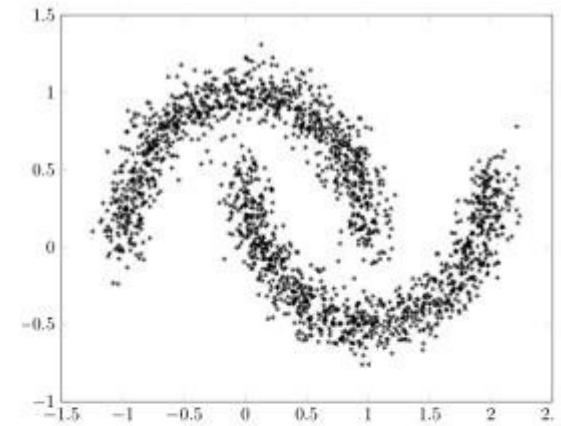
➤ Lecture 7 offers more insights into hybrid programming jointly using both MPI and OpenMP

Scientific Application Example: Data Mining & Clustering

- Hybrid data mining algorithm example
 - Parallel Density-based Spatial Clustering for Applications with Noise (DBSCAN)
 - Using MPI and OpenMP to scale better

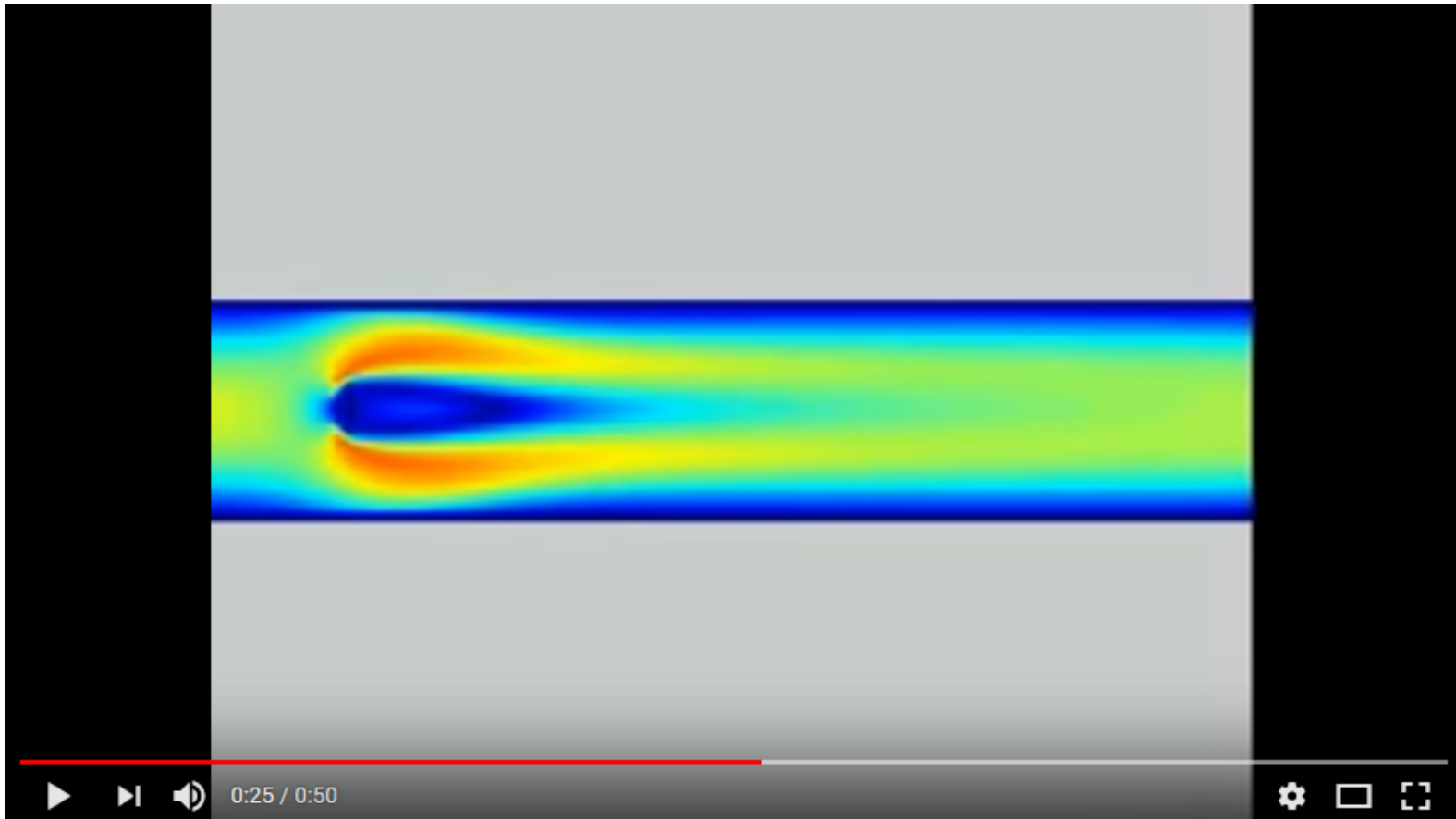


[5] M. Goetz & M. Riedel et al., 'Highly Parallel DBSCAN', MLHPC Workshop, SC2015



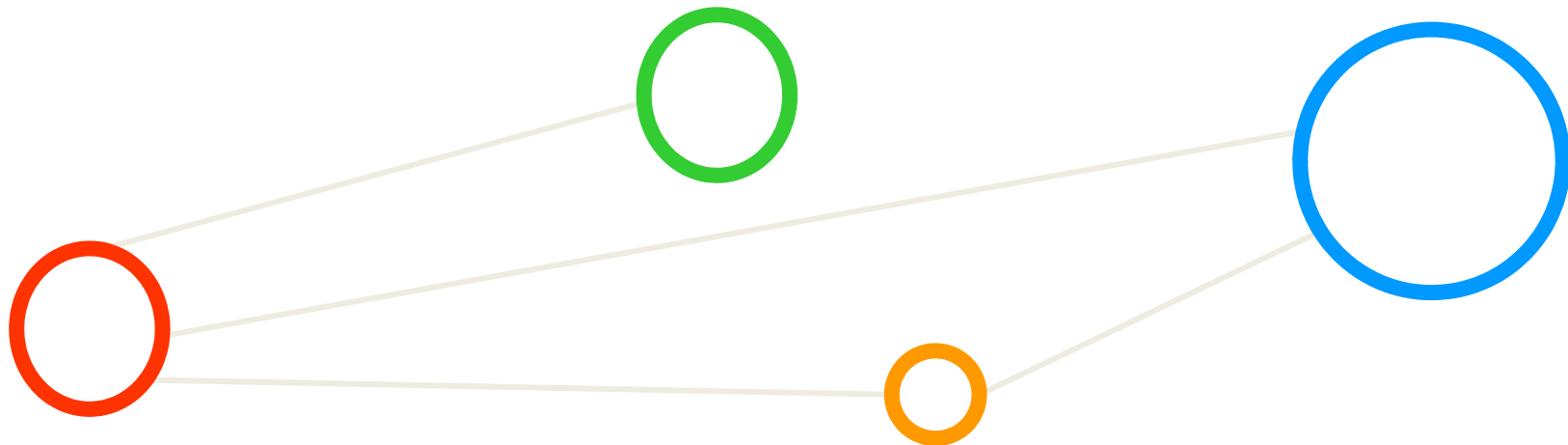
➤ Lecture 17 gives insights into machine learning & data mining applications using OpenMP & MPI

[Video] Scientific Application Example using OpenMP



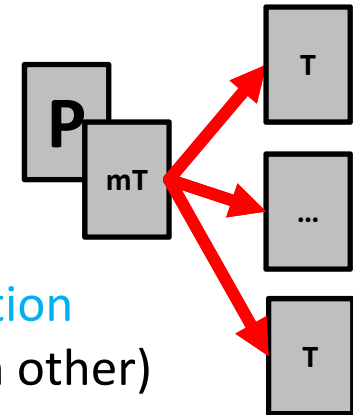
[6] Lattice Boltzmann – Flow past an obstacle, YouTube Video

OpenMP Parallel Programming Basics



Start 'Thinking' Parallel

- Parallel OpenMP programs know about the **existence of a certain number of threads** that all work together as part of a bigger picture
- OpenMP programs are written in a **sequential** programming language and some parts are **executed in parallel**
 - OpenMP programs run on a processor that 'spawns' numerous threads
- **Parallelization of dedicated n parallel regions** is key to the design in OpenMP ($n = 1, 2, 3, \dots$)
 - E.g. **loops/additions are good candidates for parallelization** (if individual loop iterations are independent from each other)
- Start with the **basic building blocks** using OpenMP
 - Defining code that enables '**parallel computing**', step-by-step is possible

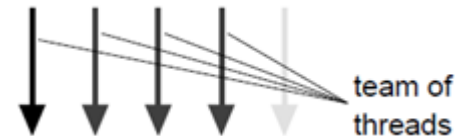


Number of Threads & Scalability

- OpenMP programs should be always written in a way that it does not assume a specific number of threads → Scalable program

- The real number of threads normally **not known at compile time**
 - (There are methods for doing it in the program → do not use them!)
 - Number is **set in scripts and/or environment variable** before executing

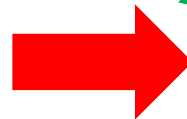
```
export OMP_NUM_THREADS=4
```



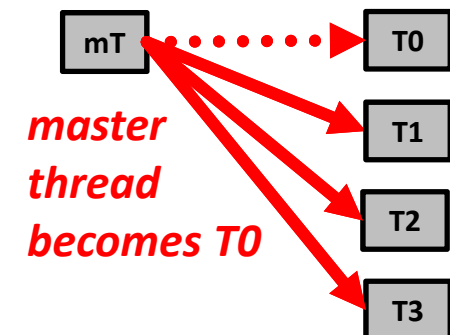
- Parallel programming is done without knowing number of threads

```
int main()
{
    #pragma omp parallel
    printf("Hello World");
}
```

*compile &
execute*



```
./helloworld.exe
Hello World
Hello World
Hello World
Hello World
```



OpenMP Basic Building Blocks: Library & Sentinel

'standard fortran programming...'

```
use omp_lib
```

```
print *, 'I am the
```

```
!$OMP PARALLEL
```

```
call do_work_package(
```

```
!$OMP END PARALLEL
```

- The OpenMP library contains OpenMP API definitions

'standard C/C++ programming...'

```
#include <omp.h>
```

```
std::cout << "I am the master, and I am alone",
```

```
#pragma omp parallel
```

```
{
```

```
do_work_package
```

```
}
```

- The Sentinel is a special string that starts an OpenMP compiler directive

- Practice view: programming OpenMP in C/C++ and fortran is slightly different, but providing the same basic concepts (e.g. no end of parallel region in C/C++, local variables, etc.)

OpenMP Basic Building Blocks: Unique Thread IDs

'standard fortran programming...'

```
use omp_lib

print *, 'I am the
!$OMP PARALLEL
  call do_work_package(omp_get_thread_num(), omp_get_num_threads())
!$OMP END PARALLEL
```

- `omp_get_thread_num()` function provides unique Thread ID (0...n-1)

'standard C/C++ programming...'

```
#include <omp.h>

std::cout << "I am the master, and I am alone";
#pragma omp parallel
{
  do_work_package(omp_get_thread_num(), omp_get_num_threads());
}
```

- `omp_get_num_threads()` function obtains number of active threads in the current parallel region

- `do_work_package()` routine code is now executed in parallel by each thread
- BUT also sub-routines of that routine are now executed in parallel

OpenMP Basic Building Blocks: Private Variables (Fortran)

```
integer :: bstart, bend, blen, numth, tid, i
integer :: N
double precision, dimension(N) :: a,b,c
...
!$OMP PARALLEL PRIVATE(bstart,bend,blen,numth,tid,i)
  numth = omp_get_num_threads()
  tid = omp_get_thread_num()
  blen = N/numth
  if(tid.lt.mod(N,numth)) then
    blen = blen + 1
    bstart = blen * tid + 1
  else
    bstart = blen * tid + mod(N,numth) + 1
  endif
  bend = bstart + blen - 1
  do i = bstart,bend
    a(i) = b(i) + c(i)
  enddo
!$OMP END PARALLEL
```

- PRIVATE defines local variables for each thread
- Each thread works independently and thus needs space to 'store' local results

- Same code executed n times with n threads, BUT tid is unique and thus different for each thread

- Practice view: the real parallelization idea is here in the loop: the simple sum of two arrays
- For each value of i we can compute and store array values independently from each other

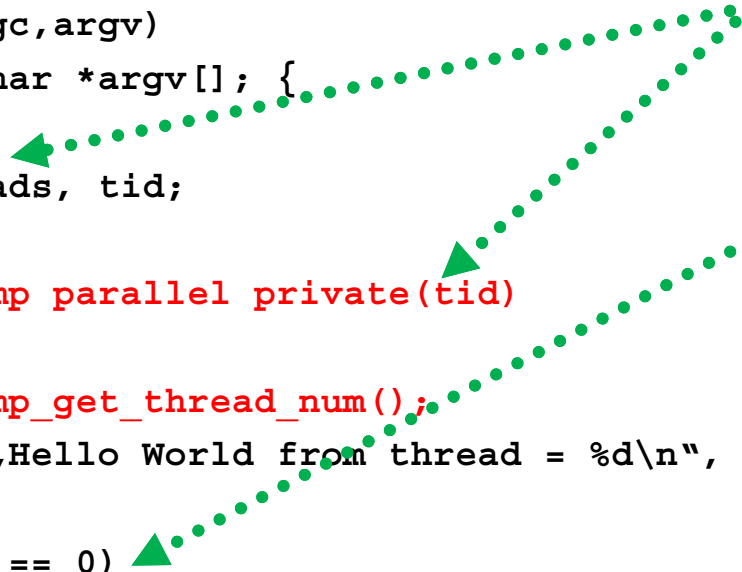
Traditional HelloWorld Example (C/C++)

```
#include <omp.h>
#include <stdio.h>
int main(argc,argv)
int argc; char *argv[]; {

    int nthreads, tid;

    #pragma omp parallel private(tid)
    {
        tid = omp_get_thread_num();
        printf(„Hello World from thread = %d\\n“, tid);

        if (tid == 0)
        {
            nthreads = omp_get_num_threads();
            printf(„Number of threads in parallel region = %d\\n“, nthreads);
        }
    }
}
```



- Shared variable nthreads
- Local variable tid

- Simple Parallel Program
- Only the master (tid=0) provides output of how many threads are existing in the parallel region

➤ Practical lectures focus on MPI and not OpenMP, but both are important programming models

OpenMP Basic Building Blocks: Loops (do, for in C/C++)

```
double precision :: pi,w,sum,x
integer :: i,N=1000000

pi = 0.d0
w = 1.d0/N
sum = 0.d0
!$OMP PARALLEL PRIVATE(x) FIRSTPRIVATE(sum)
!$OMP DO
do i=1,n
  x = w*(i-0.5d0)
  sum = sum + 4.d0/(1.d0+x*x)
enddo
!$OMP END DO
!$OMP END PARALLEL
```

local sum exists, but where is the global sum?

$$\pi = \int_0^1 dx \frac{4}{1+x^2}$$

- **FIRSTPRIVATE()** copies initial value of shared variable to local variable (simple init here otherwise problems in loop)

- **DO loop** (in front of usual do) distributes (automatically) loop iterations among threads as specifically supported 'work-sharing' construct)

- Smart programming support by OpenMP: Loops are very often part of scientific applications
- Less burden for programmer: no manual definition of local variables (e.g. i automatically localized)

OpenMP Basic Building Blocks: Critical Regions

```
double precision :: pi,w,sum,x
integer :: i,N=1000000

pi = 0.d0
w = 1.d0/N
sum = 0.d0
!$OMP PARALLEL PRIVATE(x) FIRSTPRIVATE(sum)
!$OMP DO
  do i=1,n
    x = w*(i-0.5d0)
    sum = sum + 4.d0/(1.d0+x*x)
  enddo
!$OMP END DO
!$OMP CRITICAL
  pi = pi + w*sum
!$OMP END CRITICAL
!$OMP END PARALLEL
```

- Local sum exists in each of the different threads
- We have n times the local variable value for sum now

- Race Condition in shared-memory: shared variable pi will be set concurrently by the different threads
- Value of pi depends on the exact order the threads access pi and assign wrong values

- Critical regions define a region within a parallel region where at most one thread at a time executes code (e.g. sum of new pi based on pi)

OpenMP Basic Building Blocks: Reduction

```
double precision :: r,s
double precision, dimension(N) :: a

call RANDOM_SEED()
!$OMP PARALLEL DO PRIVATE(r) REDUCTION(+:s)
do i=1,N
    call RANDOM_NUMBER(r) ! thread safe
    a(i) = a(i) + func(r) ! func() is thread safe
    s = s + a(i) * a(i)
enddo
!$OMP END PARALLEL DO

print *, 'Sum = ', s
```

- Reduction operations are a smart alternative to manual critical regions definitions around operations of variables
- Reduction operation automatically localizes variable

- Several operations are common in scientific applications
- +, *, -, &, |, ^, &&, ||, max, min

- REDUCTION() with operator + on variable s enables here ...
- Starting with a local copy of s for each thread
- During progress of parallel region each local copy of s will be accumulated separately by each thread
- At the end of the parallel region automatically synchronized and accumulated with resulting master thread variable

Vector Addition in OpenMP – Revisited (cf. Lecture 5)

```
#include <omp.h>

int main(int argv, char **argv)
{
    int n, i;
    double *x, *y;

    /* Get input size */
    n = atoi(argv[1]);
    x = (double *)malloc(n*sizeof(double));
    y = (double *)malloc(n*sizeof(double));

    #pragma omp parallel for private(i) shared (x,y)
    for (i=0; i<n; i++)
    {
        x[i] = x[i] + y[i];
    }

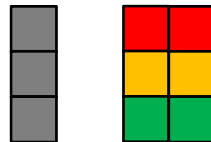
    /* x contains the result for all vector elements */
}
```

*'simplified
demo code'*

- The Sentinel is a special string that starts an OpenMP compiler directive
- Directive is optimized to enable a parallel loop (i.e. parallel for) starting a parallel region

- PRIVATE defines local variables for each thread
- Each thread works independently and thus needs space to 'store' local results – here i as index

- SHARED defines global variables that exist only one time
- Each thread works independently but SHARED variables can be written and read from all threads



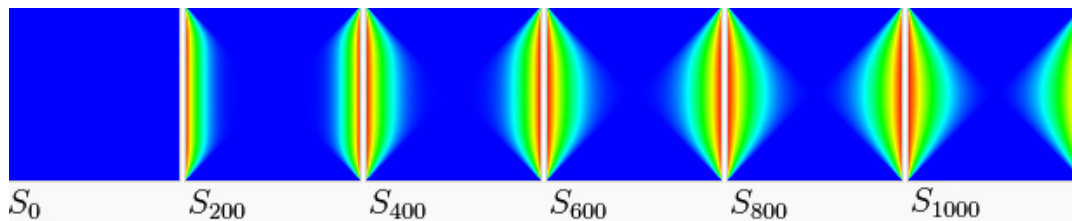
$$X = X + Y$$

Jacobi 2D Application Example – Revisited (cf. Lecture 2)

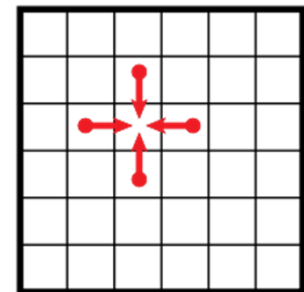
- The Jacobi iterative method is a stencil-based iterative method used in numerical linear algebra
- Algorithm for determining the solutions of diagonally dominant system of linear equations

- Solver
 - Each diagonal element is solved and approximate value is plugged in
 - The process is iterated until it **converges**
- Update function 2D Jacobi iterative method example
 - E.g. computes the arithmetic mean of a cell's four neighbours
 - E.g. solving diffusion equations (**heat dissipation example**)

[3] *Introduction to High Performance Computing for Scientists and Engineers*



[7] *Wikipedia on 'stencil code'*



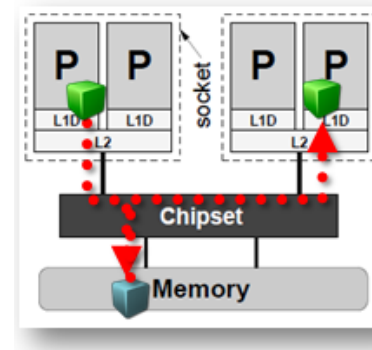
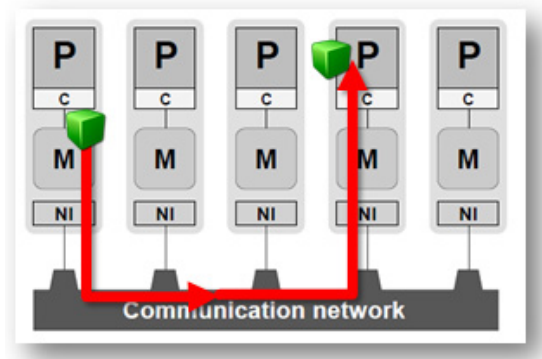
➤ Lecture 7 will provide more details about stencil-based iterative methods and used patterns

Advanced Example: 2D Jacobi Algorithm with OpenMP

```
double precision, dimension(0:N+1,0:N+1,0:1) :: phi
double precision :: maxdelta,eps
integer :: t0,t1
eps = 1.d-14      ! convergence threshold
t0 = 0 ; t1 = 1
maxdelta = 2.d0*eps
do while(maxdelta.gt.eps)
    maxdelta = 0.d0
    !$OMP PARALLEL DO REDUCTION(max:maxdelta)
    do k = 1,N
        do i = 1,N
            ! four flops, one store, four loads
            phi(i,k,t1) = ( phi(i+1,k,t0) + phi(i-1,k,t0)
                           + phi(i,k+1,t0) + phi(i,k-1,t0) ) * 0.25
            maxdelta = max(maxdelta,abs(phi(i,k,t1)-phi(i,k,t0)))
        enddo
    enddo
    !$OMP END PARALLEL DO
    ! swap arrays
    i = t0 ; t0=t1 ; t1=i
enddo
```

[3] Introduction to High Performance Computing for Scientists and Engineers

Selected Comparisons with MPI



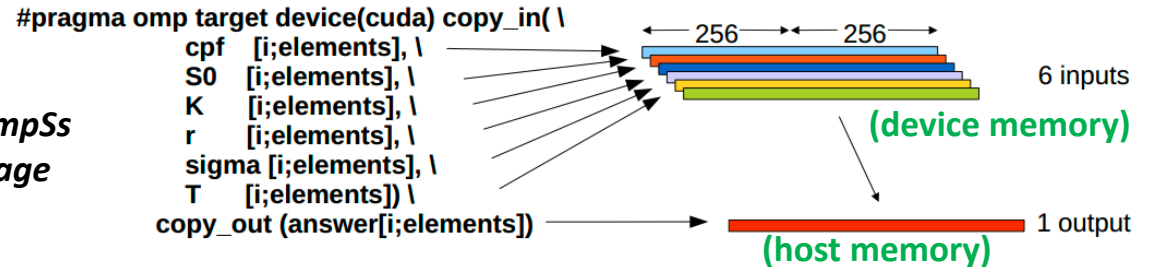
- Some aspects are similar, because both enable **parallel** computing
 - Obtaining **unique IDs**: MPI ranks vs. OpenMP thread-num
 - **Master-worker approach** (if rank==0 vs. if tid ==0)
- No **explicit communication constructs** to enable inter-process communication in OpenMP → assuming shared-memory
 - **Data exchange**: Message exchanges between processes vs. shared variable
 - **Synchronization** functions nevertheless exist in both: e.g. barriers
 - **Clever automatisms for usual problems**: MPI reduce vs. OpenMP reduction

DEEP-EST EU Project – OmpSs & OpenMP Evolutions

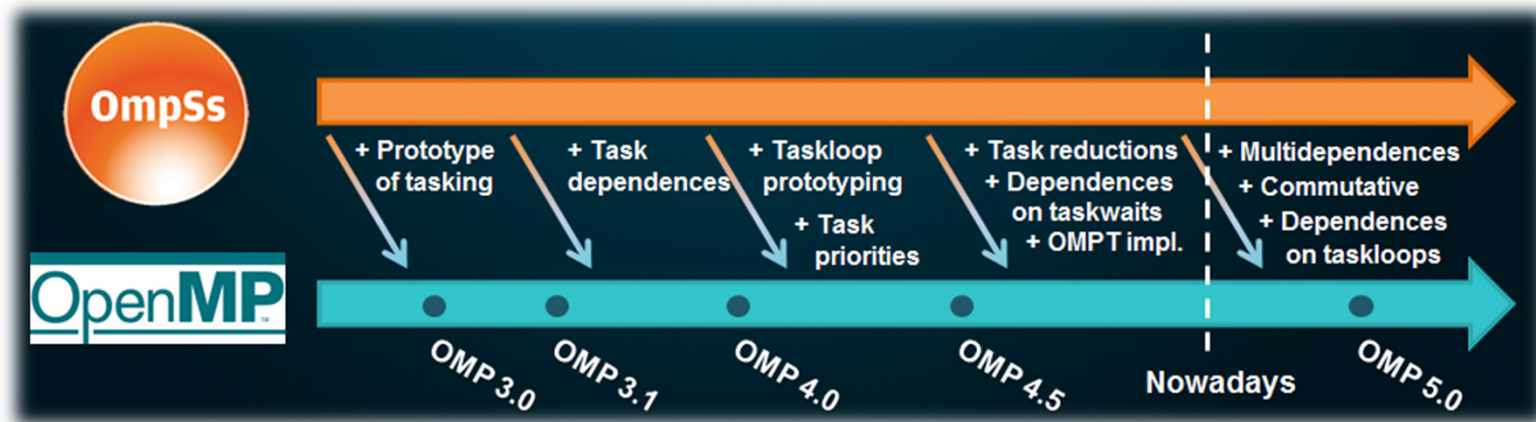
DEEP-EST

[9] DEEP-EST EU Project

[10] OmpSs
Web page

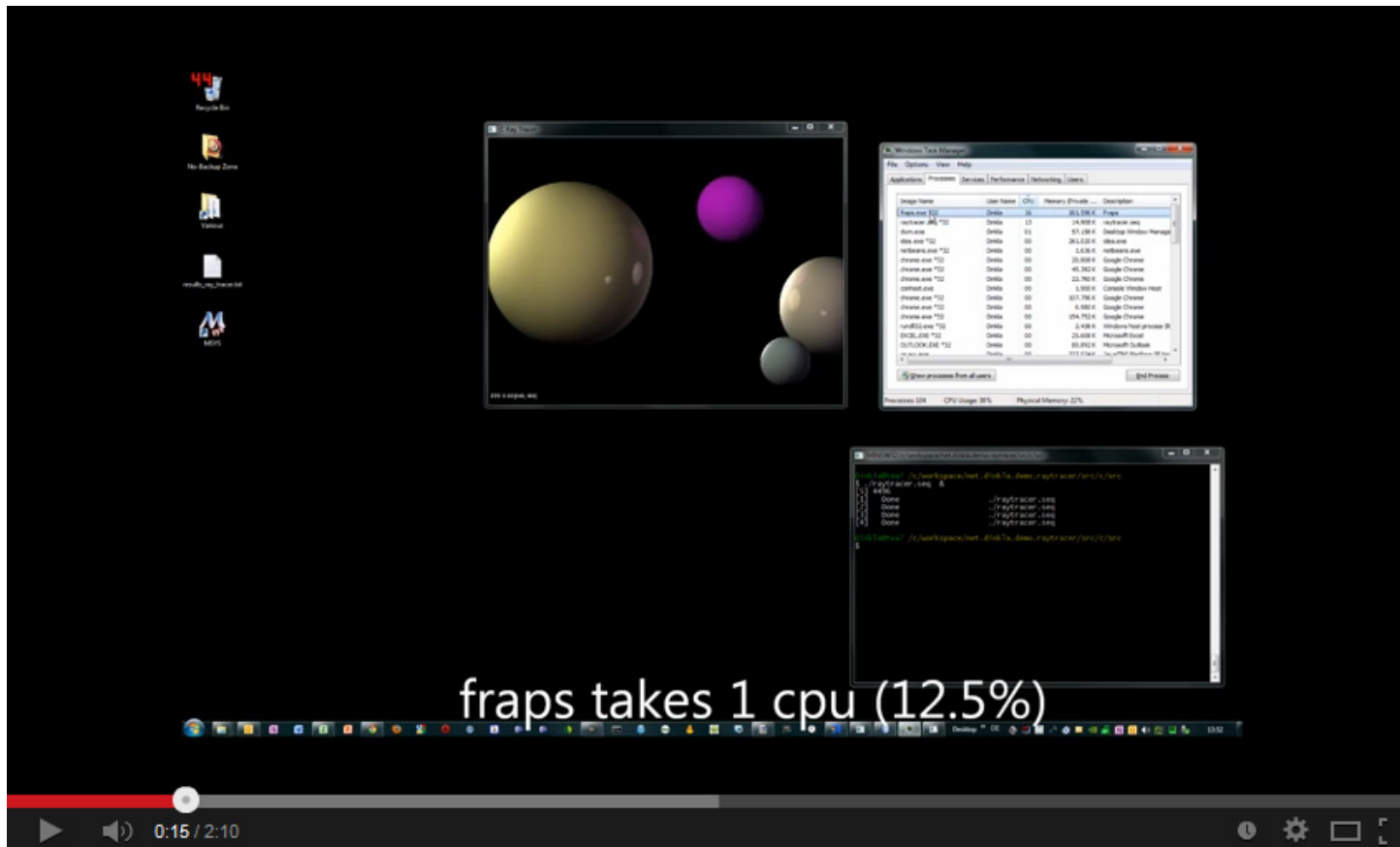


- OmpSs is an innovative programming model influencing OpenMP
 - Based on tasks and (data) dependencies – tasks as elementary unit of work
 - Extend OpenMP model: better data-flow & heterogeneity (e.g. GPGPUs)



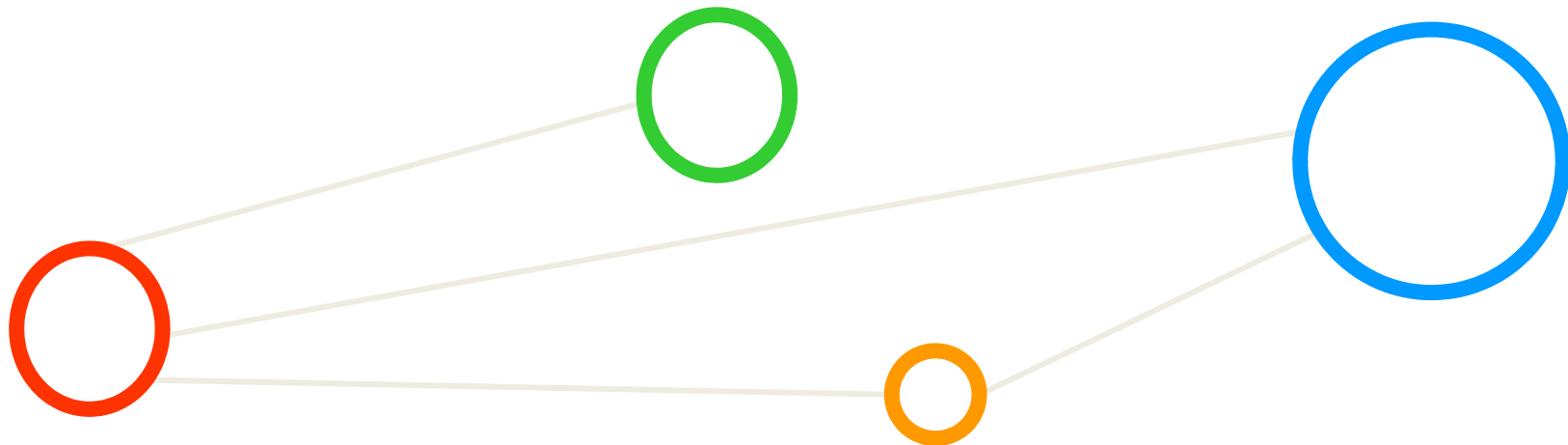
➤ Lecture 10 will provide more details about the use of accelerators and the benefits of GPGPUs

[Video] Raytracing Application with OpenMP



[8] Speeding up a Ray tracer with OpenMP, YouTube Video

Lecture Bibliography



Lecture Bibliography

- [1] Parallel Algorithms Underlying MPI Implementations, Online:
http://www.slidefinder.net/p/parallel_algorithms_underlying_mpi_implementations/13-parallelalgorithmsunderlyingmpiimplementations/17131238/p2
- [2] PEPC, FZ Juelich, Online:
<http://www.fz-juelich.de/ias/jsc/EN/AboutUs/Organisation/ComputationalScience/Simlabs/slpp/SoftwarePEPC/node.html>
- [3] Introduction to High Performance Computing for Scientists and Engineers, Georg Hager & Gerhard Wellein, Chapman & Hall/CRC Computational Science, ISBN 143981192X
- [4] The OpenMP API specification for parallel programming,
Online: <http://openmp.org/wp/openmp-specifications/>
- [5] M. Goetz, C. Bodenstein, M. Riedel, '*HPDBSCAN – Highly Parallel DBSCAN*', Proceedings of the ACM/IEEE International Conference for High Performance Computing, Networking, Storage, and Analysis (SC2015), Machine Learning in HPC Environments (MLHPC) Workshop, USA,
Online: <https://dl.acm.org/citation.cfm?doid=2834892.2834894>
- [6] Lattice Boltzmann – Flow past an obstacle,
Online: <https://www.youtube.com/watch?v=fspGcBpxguo>
- [7] Wikipedia on 'stencil code',
Online: http://en.wikipedia.org/wiki/Stencil_code
- [8] Speeding up a Ray tracer with OpenMP, YouTube Video,
Online: http://www.youtube.com/watch?v=S9Z5MeQS_LU
- [9] DEEP-EST EU Project,
Online: <http://www.deep-projects.eu/>
- [10] OmpSs Programming Model,
Online: https://pm.bsc.es/ompss-docs/specs/01_introduction.html

Useful Collection on OpenMP Tutorials/Materials

- YouTube – ‘PRACE Video Tutorial – Introduction to OpenMP’, Online:
<http://www.youtube.com/watch?v=LyKA77PEM3o>
- Introduction to OpenMP, HLRS Stuttgart, Online:
https://fs.hlrs.de/projects/par/par_prog_ws/pdf/openmp-intro7.pdf
- Using OpenMP – Portable Shared Memory Parallel Programming, B. Chapman, G. Jost, R. Van der Pas (2008)
- Parallel Programming in OpenMP R. Chandra, L. Dagum, D. Kohr, D. Maydan, J. McDonald, R. Menon (2001)
- LLNL OpenMP Tutorial, Online:
<https://computing.llnl.gov/tutorials/openMP/>
- **And if you don’t find something:**
„just google the OpenMP compiler directive
or environment variable in question
– good resources are out there“:

