

a)

When $C = 2$, Accuracy:

| Digit0 | Digit1 | Digit2 | Digit3 | Digit4 | Digit5 | Digit6 | Digit7 | Digit8 | Digit9 | Average |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|---------|
| 0.9873 | 0.9932 | 0.9796 | 0.9747 | 0.9814 | 0.9706 | 0.9807 | 0.9828 | 0.9517 | 0.9631 | 0.9076 |

When $C = 2$, Number of Support Vectors:

| Digit0 | Digit1 | Digit2 | Digit3 | Digit4 | Digit5 | Digit6 | Digit7 | Digit8 | Digit9 |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 464 | 505 | 1211 | 1422 | 900 | 1326 | 686 | 779 | 2093 | 1848 |

When $C = 4$, Accuracy:

| Digit0 | Digit1 | Digit2 | Digit3 | Digit4 | Digit5 | Digit6 | Digit7 | Digit8 | Digit9 | Average |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|---------|
| 0.9868 | 0.9922 | 0.9792 | 0.9742 | 0.9802 | 0.9749 | 0.9804 | 0.9821 | 0.9559 | 0.9631 | 0.9043 |

When $C = 4$, Number of Support Vectors:

| Digit0 | Digit1 | Digit2 | Digit3 | Digit4 | Digit5 | Digit6 | Digit7 | Digit8 | Digit9 |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 455 | 486 | 1201 | 1416 | 880 | 1292 | 671 | 770 | 2097 | 1836 |

When $C = 8$, Accuracy:

| Digit0 | Digit1 | Digit2 | Digit3 | Digit4 | Digit5 | Digit6 | Digit7 | Digit8 | Digit9 | Average |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|---------|
| 0.9854 | 0.9913 | 0.9787 | 0.9748 | 0.9796 | 0.9736 | 0.9792 | 0.9808 | 0.9555 | 0.9636 | 0.9013 |

When $C = 8$, Number of Support Vectors:

| Digit0 | Digit1 | Digit2 | Digit3 | Digit4 | Digit5 | Digit6 | Digit7 | Digit8 | Digit9 |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 436 | 455 | 1189 | 1400 | 869 | 1253 | 651 | 744 | 2077 | 1816 |

When $C = 2$, plot the 3 support vectors of the largest Lagrange multiplier

digit 0, $y_i = 1$



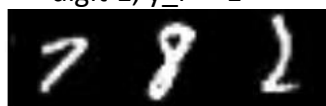
digit 0, $y_i = -1$



digit 1, $y_i = 1$



digit 1, $y_i = -1$



digit 2, $y_i = 1$



digit 2, $y_i = -1$



digit 3, $y_i = 1$ digit 3, $y_i = -1$ digit 4, $y_i = 1$ digit 4, $y_i = -1$ digit 5, $y_i = 1$ digit 5, $y_i = -1$ digit 6, $y_i = 1$ digit 6, $y_i = -1$ digit 7, $y_i = 1$ digit 7, $y_i = -1$ digit 8, $y_i = 1$ digit 8, $y_i = -1$ digit 9, $y_i = 1$ digit 9, $y_i = -1$ 

When $C = 4$, plot the 3 support vectors of the largest Lagrange multiplier

digit 0, $y_i = 1$ digit 0, $y_i = -1$ digit 1, $y_i = 1$ digit 1, $y_i = -1$ digit 2, $y_i = 1$ digit 2, $y_i = -1$ 



digit 3, $y_i = 1$



digit 3, $y_i = -1$



digit 4, $y_i = 1$



digit 4, $y_i = -1$



digit 5, $y_i = 1$



digit 5, $y_i = -1$



digit 6, $y_i = 1$



digit 6, $y_i = -1$



digit 7, $y_i = 1$



digit 7, $y_i = -1$



digit 8, $y_i = 1$



digit 8, $y_i = -1$



digit 9, $y_i = 1$



digit 9, $y_i = -1$



When $C = 8$, plot the 3 support vectors of the largest Lagrange multiplier

digit 0, $y_i = 1$



digit 0, $y_i = -1$



digit 1, $y_i = 1$

digit 1, $y_i = -1$



digit 2, $y_i = 1$



digit 2, $y_i = -1$



digit 3, $y_i = 1$



digit 3, $y_i = -1$



digit 4, $y_i = 1$



digit 4, $y_i = -1$



digit 5, $y_i = 1$



digit 5, $y_i = -1$



digit 6, $y_i = 1$



digit 6, $y_i = -1$



digit 7, $y_i = 1$



digit 7, $y_i = -1$



digit 8, $y_i = 1$



digit 8, $y_i = -1$



digit 9, $y_i = 1$



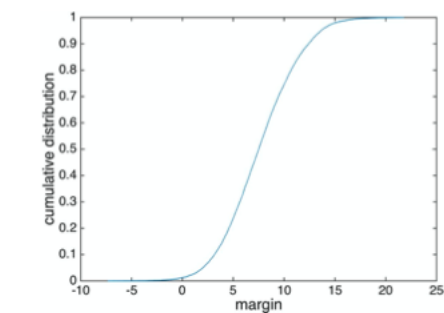
digit 9, $y_i = -1$



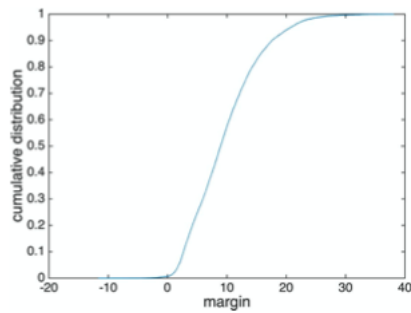
Comments: C doesn't make a lot of differences. Digit 8 and Digit 9 are the hardest to identify. They obtain the less accuracy and require the most support vectors.

b)

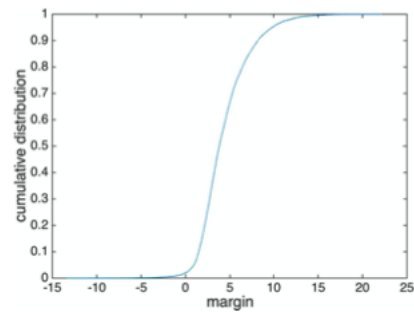
When $C = 2$, the cdf plots for digits 0-9:



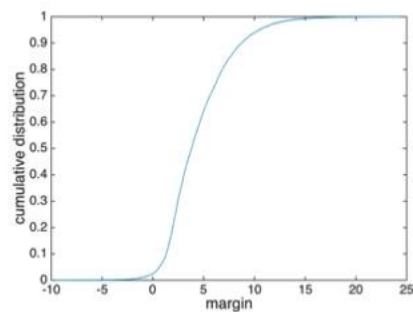
Digit0



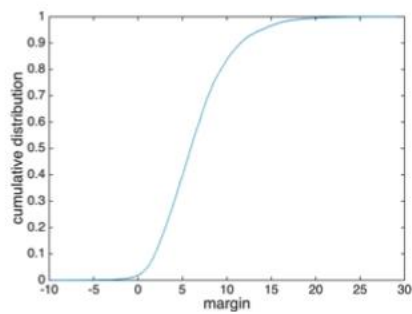
Digit1



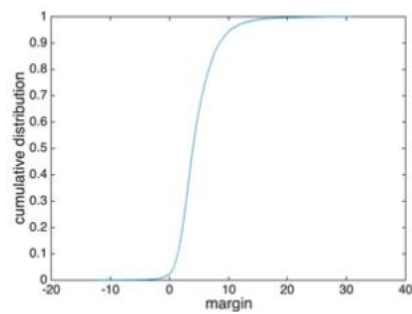
Digit2



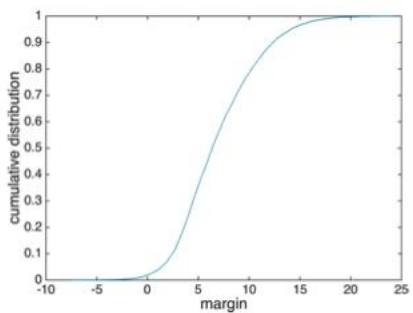
Digit3



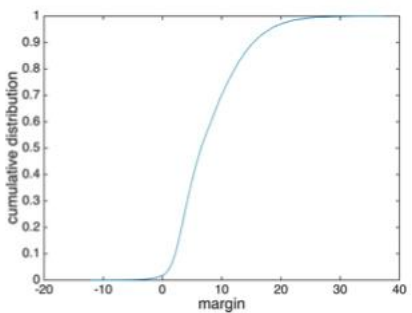
Digit4



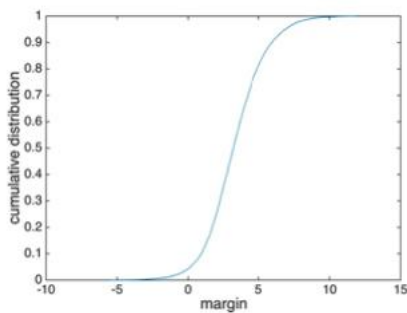
Digit5



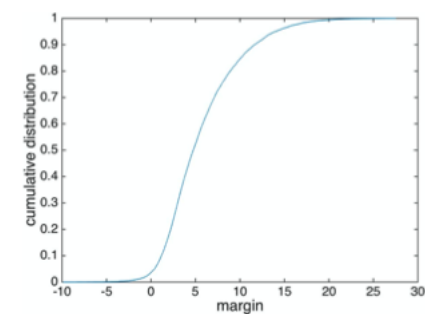
Digit6



Digit7

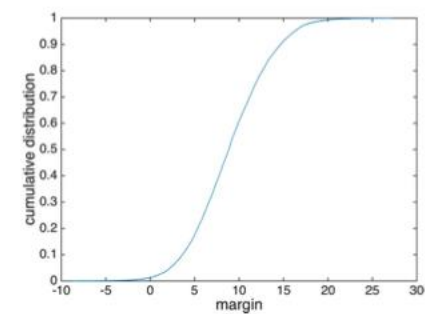


Digit8

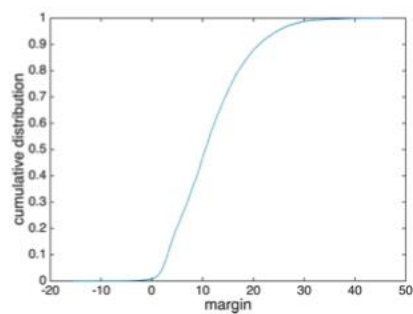


Digit9

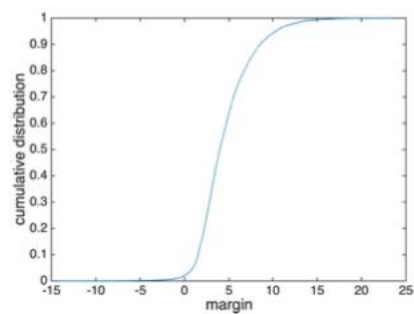
When $C = 4$, the cdf plots for digits 0-9:



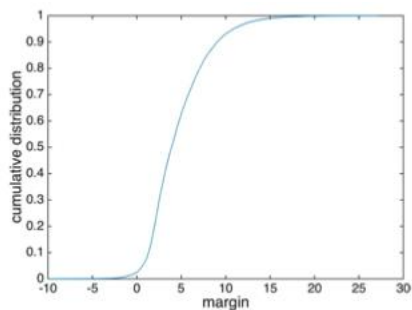
Digit0



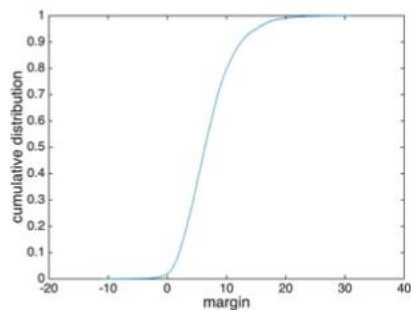
Digit1



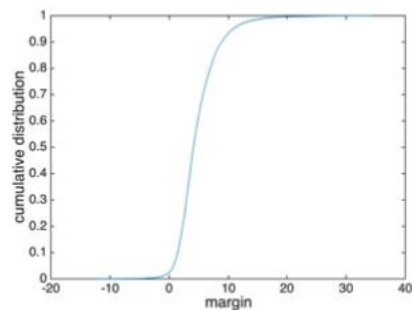
Digit2



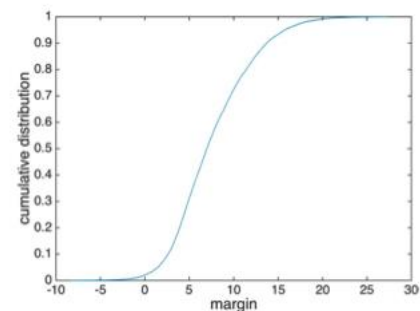
Digit3



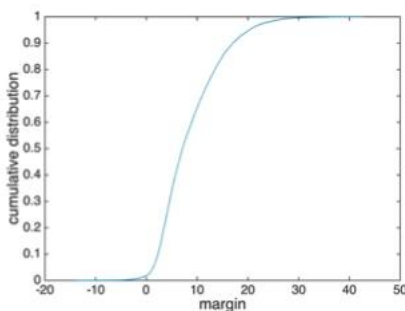
Digit4



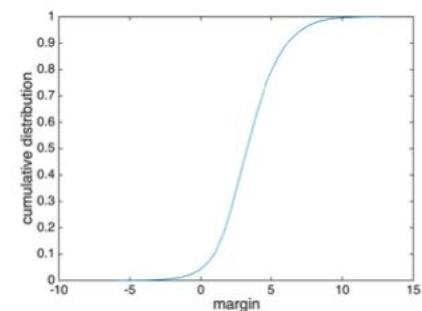
Digit5



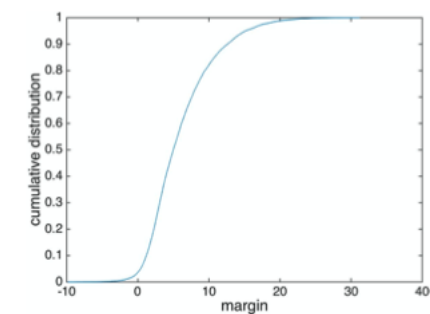
Digit6



Digit7

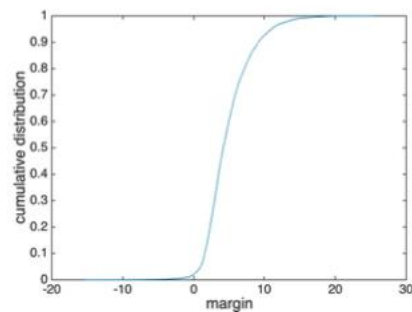
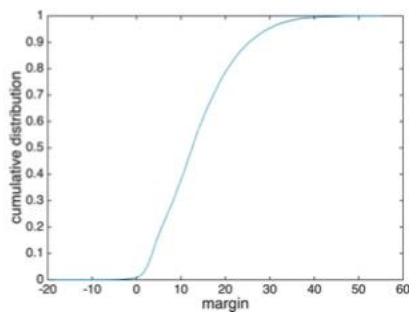
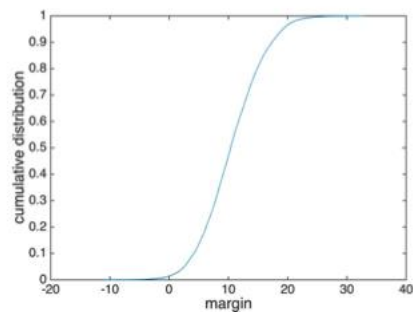


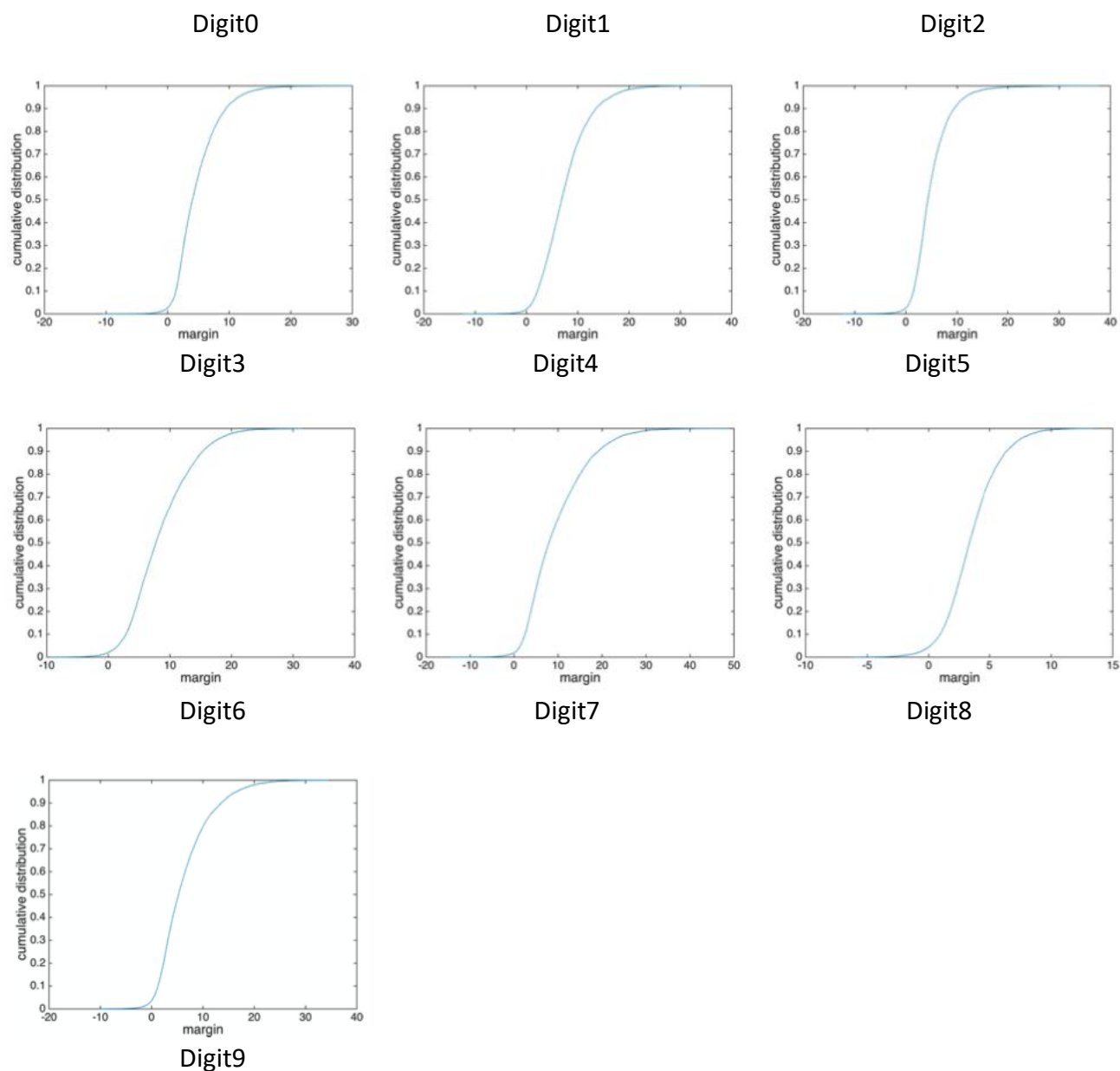
Digit8



Digit9

When $C = 8$, the cdf plots for digits 0-9:





c) When $C = 2$, $\gamma = 0.0625$, the test accuracy is better than those for linear svm

| Digit0 | Digit1 | Digit2 | Digit3 | Digit4 | Digit5 | Digit6 | Digit7 | Digit8 | Digit9 | Average |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|---------|
| 0.9953 | 0.9976 | 0.9888 | 0.9885 | 0.9915 | 0.9874 | 0.9930 | 0.9907 | 0.9837 | 0.9883 | 0.9742 |

When $C = 2$, $\gamma = 0.0625$, Number of Support Vectors are much higher than those for linear svm

| Digit0 | Digit1 | Digit2 | Digit3 | Digit4 | Digit5 | Digit6 | Digit7 | Digit8 | Digit9 |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 5861 | 2416 | 6892 | 7131 | 6302 | 6683 | 5648 | 5742 | 7672 | 6492 |