

# KIT103/KMA155 Programming Assignment 4: Number Theory 2

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Enter your answers to these questions in the accompanying Python script file `kit103_assign4.py`. Include your name and student ID in the places indicated in the header comment.

Submit your completed script file to the *Programming Assignment 4 (Number Theory 2)* assignment folder on MyLO by **1500 (3pm) Wednesday 4 October 2017**.

Test your solutions thoroughly. Your submission is expected to run without failure (even if it doesn't produce the correct answer for each question). If we have to correct your submission in order for it to run then the maximum total mark you can receive will be 3/5 (1.5/2.5 if in KMA155).

KMA155 students will be assessed primarily on Questions [1a](#) and [2](#) (which are also marked with an asterisk (\*)), but may attempt all questions if they wish.

## Question 1: Decode Linux Permissions (2 marks)

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Linux file permissions can be modified by a command (`chmod`) that accepts a three-digit octal number as one of its inputs. *Refer to the A8 lecture slides for details of the structure of this number and how to interpret it.*

Linus Torvalds, the creator of the Linux family of operating systems, is (perhaps undeservedly) renowned for naming his creations after himself. Although the Linux file permissions utility `chmod` is actually from the earlier Unix family of operating systems, it is still fitting that this question be personalised, so you will answer questions about the permissions indicated by octal triplets (000–777) derived from your student ID.

### Task 1: Enter your student ID and learn which octal numbers you will decode (0–2 marks)

In the assignment script file is a dictionary of answers for this question and a helper function, `sid2permissions(sid)`, which will generate a pair of octal triplets based on the student ID `sid` it is given.

**Your first task** is to replace the 0 that is currently assigned to `q1['sid']` with your student ID as an integer with no leading zeroes. Then run the script and inspect the values of `q1['file A']` and `q1['file B']` to learn what octal numbers you will be decoding in the [next task](#).

For example, if your student ID were 134567 then upon running the script you would find that:

- `sid2permissions(q1['sid'])` returns the value `('406', '647')`, so
- `q1['both permissions']`  $\mapsto$  `('406', '647')`
- `q1['file A']`  $\mapsto$  `'406'`
- `q1['file B']`  $\mapsto$  `'647'`

Completing this task contributes no marks in itself, but you will receive zero for all of Question 1 in any of the following situations: you do not modify the `'sid'` entry; you use a student ID that is not your own; or you modify the values that the script generates and assigns to `'both permissions'`, `'file A'` or `'file B'`.

### Task 2: Answer questions about those permission sets (2 marks)

Now it's time to answer questions about the permissions for two fictitious files, 'file A' and 'file B'. You may use any approach to arrive at answers to the questions below that doesn't involve asking someone else to derive the answer on your behalf. All of them can be answered without the assistance of a computer (once you know the numbers you are to decode), but if you find it useful to use a function to generate the answer then feel free to do so.

- a. (\*) The following questions relate to the permissions on **file A**
  1. Rewrite the octal permissions value as a binary literal (a 9-bit integer beginning with 0b)  
In parts 2–4 write **True**, **False** or any valid Boolean expression that will calculate the answer.  
Given these permissions:
  2. Can the user's *group* write to file A?
  3. Can the user's *group* execute file A?
  4. Can all *other* users read file A?
- b. The following questions related to the permissions on **file B**
  1. Rewrite the octal permissions value as a binary literal (a 9-bit integer beginning with 0b)  
In parts 2–4 write **True**, **False** or any valid Boolean expression that will calculate the answer.  
Given these permissions:
  2. Can the *user* write to file B?
  3. Can the user's *group* read file B?
  4. Can all *other* users read file B?

## Question 2: base2base (1.5 marks, \*)

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In general, to convert a number in base  $b_1 \neq 10$  to another base  $b_2 \neq 10$  involves two steps: base  $b_1$  to base 10, and then base 10 to base  $b_2$ . (Although there exist shortcuts when converting between binary and octal, and binary and hexadecimal, we won't use them here.) **Your task** is to complete the implementation of the stub function `base2base(n, b1, b2)` according to the following specifications:

- The parameter `n` is a *string* representing a number in base  $b_1$ . You may assume that `n` will always represent a valid number in base  $b_1$ . The bases  $b_1$  and  $b_2$  are integers in the range 2 through 36 (inclusive)
- The output of the function is a string representing the equivalent value in base  $b_2$
- You may define an additional function to perform one of the steps. That function may be your own creation, or come from the lecture slides or lab solutions
- For a solution to receive full marks the body of `base2base` must be one line of code (and not merely an alias for another, longer function). Anything longer will receive a maximum of 1 mark

## Question 3: Really Stupid Encryption (RSE) (1.5 marks)

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Bonus content in the lecture slides introduced the nearly-unbreakable form of encryption [RSA](#), but in this question you will consider an alternative form of encryption suggested by the Week 10 practical: Really Stupid Encryption (RSE).

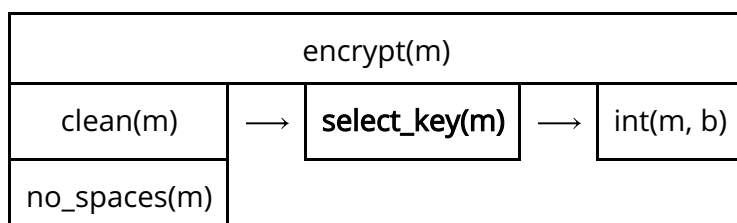
In this encryption system a plain text message is written using the digits 0–9 and upper case letters A–Z, which is then 'encrypted' by parsing (converting) that string to a decimal integer using a suitable original base (for example, base 36 allows all digits and letters to be used). Decryption is done by converting the integer value back into a string representing a number in the original base.

If the key (base) 36 was used in all instances then this system would be too easy to break, so there is a function `select_key(m)` whose role is to select the *smallest valid key* that can be used to encrypt the

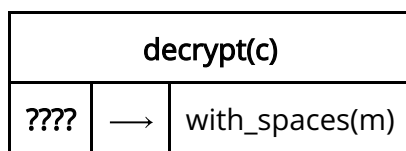
message `m`. In other words, it should select a base to use so that every letter in the original message is a valid digit in that base. (The current implementation just selects 36 all the time though.)

The assignment script file already contains a number of functions that can be used to implement this system, and your task will be to provide implementations of the remaining components and, in the last task, write a utility to 'break' the encryption by trying every possible key (original base). These diagrams summarise the various functions and how they work together, and indicates which are already **done** and which **you need to modify**:

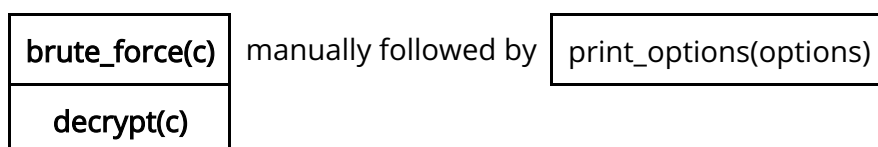
### Encryption:



### Decryption:



### Code breaking:



### Your tasks:

- Implement `select_key(m)`** such that it returns the *smallest valid key* that can be used to encrypt the message `m`. **Hint:** Look at the documentation for Python lists to identify a list method that will help in this task.
- Implement `decrypt(c, b)`** such that it converts the integer `m` back into a string of base `b` digits and then calls `with_spaces(m)` on the result. **Hint:** Consider if anything you did in Question 2 will be useful here.
- Implement `brute_force(c)`** such that it enumerates the possible bases (2–36) that may have been used to generate the encrypted message `c` and what decrypted message is obtained in each case. The function should return a list of pairs in the form  $(b, m)$ , where  $b$  is the candidate key and  $m$  the result of `decrypt(c, b)`. Its current, default implementation returns a list of just one pair, which is the original encrypted message (which is in base 10). You may find it helpful to use `print_options(brute_force(c))` to display the results generated by `brute_force(c)`

Your answers will be assessed such that you will gain marks for any completed component, even if other parts have not been done.

### Sample test cases

- For `select_key()`:
  - `select_key('123456789')`  $\mapsto$  10
  - `select_key('HELP')`  $\mapsto$  26

- `select_key('ATOZ')`  $\mapsto$  36
  - `select_key('ZTOA')`  $\mapsto$  36
  - For `decrypt()`:
    - `decrypt(123456789, 10)`  $\mapsto$  '123456789'
    - `decrypt(308827, 26)`  $\mapsto$  'HELP'
    - `decrypt(505043, 36)`  $\mapsto$  'ATOZ'
    - `decrypt(606045923, 36)`  $\mapsto$  'A TO Z'
  - Then try your `brute_force()` on the following and look through the decrypted options to see if one looks like a valid English message:
    - 13393764796
    - 13020462164572244307999285192829454
    - 14385889152344428191009519205879627478812
    - 152640406481713219640895194672
    - 1371576329515556924408915322199930911422016416558583644466644047
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