

Percentage

Solution:

- 1) let a, b and c be the ages of mother daughter and infant respectively

$$a+b+c=74$$

$$a=b+c+46 \text{ (given)}$$

$$c=b-60\% \text{ of } b$$

$$c=0.4b$$

in eq 1

$$b+c+46+b+c=74$$

$$b+0.4b+b+0.4b=28$$

$$2.8b=28$$

$$b=10\text{kgs (weight of daughter)}$$

$$c=4\text{kgs (of infant)}$$

$$\text{and } a=60\text{kgs (of mom)}$$

- 2) Let initially there were 100 labor and total work load was 100 units, so each labor's work=1 unit.

When there are 33.33% or $100/3$ more labor,

$$\text{Total laborers} = 100 + 100/3 = 400/3$$

As $400/3$ labors has to complete the same work of 100 units

$$\text{So each labor's work} = \frac{\text{Work}}{\text{No. of Labourers new}} = 100/400/3 = 3/4 \text{ unit.}$$

$$\text{Hence \% reduction in the work load of each labor} = (1 - 3/4) * 100 = 100/4 = 25\%$$

- 3) Three candidates contested an election and received 2561, 8000 and 15721.

$$\text{Total number of votes polled} = (2561 + 8000 + 15721) = 26282$$

$$\text{So, required percentage} = 15721/26282 \times 100 = 59.81\%$$

- 4) Paper A got 18 out of 70

$$\text{AS such \% } 18/70 \times 100 = 25.71$$

Paper B got 14 out of 30

$$\text{So \% } 14/30 \times 100 = 46.66$$

Well in paper B

- 5) $40,000 * (3/4)^3 = 16875$

- 6) Total no. of votes=x

$$\text{so } 30/100 \times x = 1200$$

$$x = 4000.$$

$$\text{Therefore, } 70/100 * 4000 = \text{no. of votes for 70\%}$$

7) Population 3 years hence :-

Current Population = 121000

Rate = 10% per annum

Time = 3 years

So,

→ Population after 3 years = Current Population * $[1 + (\text{rate}/100)]^{(\text{time})}$

→ Population after 3 years = $121000[1 + (10/100)]^3$

→ Population after 3 years = $121000[1 + (1/10)]^3$

→ Population after 3 years = $121000 * (11/10)^3$

→ Population after 3 years = $121000 * (1331/1000)$

→ Population after 3 years = 161051

Population 2 years ago :-

→ Current Population = 121000

→ Rate = 10% per annum

→ Time = 2 years

So,

→ Current Population = Population 2 years ago * $[1 + (\text{rate}/100)]^{(\text{time})}$

→ $121000 = \text{Population 2 years ago}[1 + (10/100)]^2$

→ $121000 = \text{Population 2 years ago}[1 + (1/10)]^2$

→ $121000 = \text{Population 2 years ago} * (11/10)^2$

→ $121000 = \text{Population 2 years ago} * (121/100)$

→ Population 2 years ago = $(121000 * 100)/121$

→ Population 2 years ago = 100000

therefore,

→ Required difference = $161051 - 100000 = 61051$ (Ans.)

8) Present population = $50000(1 - 5/100/10)^2$

= $50000 \times 95/100 \times 95/100$

= 45125

9) Party 2 and 3 Got 12 and 43% Respectively = 55% as a whole.

55% of 16000 = 8800 and Party 1 got 45% Vote = 45% of 16000 = 7200.

Margin of Votes = $8800 - 7200 = 1600$

10) Let us assume that, the marked price of the item is Rs.100 .

Case 1) :-

→ marked price = Rs100

→ commission = 12%.

Than,

→ Selling Price = List Price * (100 - commission%) / 100 = {100 * (100 - 12)} / 100 = Rs.88

Now, we have ,

→ selling Price of magazine = Rs.88

→ Profit % = 20%.

Than,

→ Cost Price of magazine = (Selling Price * 100) / (100 + Profit%) = (88 * 100) / (100 + 20) = (88 * 100) / 120 = Rs.(220/3).

Case 2) :-

→ marked price = Rs.100

→ commission = 23%.

Than,

→ Selling Price = marked Price * (100 - commission%) / 100 = {100 * (100 - 23)} / 100 = Rs.77

Now, we have ,

→ selling Price of magazine = Rs.77

→ Cost Price of magazine = Rs.(220/3) .

Therefore,

» Profit = selling Price - cost Price = 77 - (220/3) = Rs.(11/3) .

Hence,

→ Gain % = (gain in Rs. * 100) / (cost Price)

→ Gain % = (11 * 100 * 3) / (3 * 220)

→ Gain % = 5% (Ans.)

11)

According to the question

$$120 \times [(100-x) / 100] = 40 \times [(100+x) / 100]$$

$$=(100-x) / (100+x) = 40/120 = 1/3$$

$$=x=50$$

$$\text{Now, } x\% \text{ of } 210 = 210 \times 50/100 = 105$$

$$=(x + 20)\% \text{ of } 180 = 180 \times 70/100 = 126$$

$$\text{:Required percentage} = [(126-105)/126] \times 100 = 16 \frac{2}{3}\%$$

12) Let the expenditure of Raju=100Rs.

So, income of Raju=120Rs.

Hence, the saving amount=20Rs.

When the income was increased by 60%,

then the new income amount= $120 \times 160 / 100 = 192$ Rs.

The increased expenditure= $170 \times 100 / 100 = 170$ Rs.

Hence, the new saving amount= $192 - 170 = 22$ Rs

Hence, the required percentage = $(22-20) \times 100 / 20 = 2 \times 100 / 20 = 10\%$

13) Let the income of B be 4x.

The income of A = $4x + 25\%$ of $4x = 5x$

The income of C = $(4x + 5x) \times [35/100] = 3.15x$

\therefore Required percentage = $[(5x - 3.15x) / 5x] \times 100 = 37\%$

14) Students failed in English only = $(50 - 15)\% = 35\%$

Students failed in Math only = $(40 - 15)\% = 25\%$

Students failed in both subjects = 15%

Therefore, Students failed in either or both subjects = $35 + 25 + 15 = 75\%$

Therefore, Students passed in both subjects = $(100 - 75)\% = 25\%$

But students passed = 200 (i.e. 8 times of 25)

Therefore, Students appeared = $8 \times 100 = 800$

15) Let total sales be 100a and price of each item be 100b

So, Total Revenue = 10000ab

Price after 20% reduction = 80a

$10000ab(1 + 25\%) = 80b \times 100a(1 + x\%)$

$\Rightarrow 12500ab = 8000ab \times (100 + x)/100$

$\Rightarrow 1250/8 = 100 + x$

$\Rightarrow 8x = 450$

$\Rightarrow x = 56.25\%$

\therefore The value of x is 56.25%

16) We know, $20\% = 1/5$ $30\% = 3/10$ & $25\% = 1/4$

Ratio of A to B = 4: 5 ----(1)

Ratio of C to D = 13:10 --(2)

Ratio of D to A = 3:4 -- --(3)

= Ratio of A,B and D = 4:5: 3 ·(4)

\therefore Ratio of A, B,C and D = 40:50:39:30

= C : B = 39:50

= C/B = 39/50

= C = 39/50 \times B

= C = 0.78B

17) $(100 \times 100) / 120 = 83.33 \text{ kg}$

Let the man have Rs 100 and price of 100 kg sugar is Rs 100

Now price is increased,

New price of sugar = Rs 120 for 100 kg

And man his increase his expenditure by 8% = Rs 108

So, man will buy in Rs 108 = $(100 \times 108) / 120 = 90 \text{ kg}$

So he have to decrease his consumption by $100 - 90 = 10\%$.

18) $15\% \rightarrow 75$

$100\% \rightarrow 500$

19) Let income of Sudha be $200x$.

Saving of Sudha = $200x \times [15/100] = 30x$

Expenditure of Sudha = $200x - 30x = 170x$

New Expenditure of Sudha = $170x \times [6/5] = 204x$

New Savings of Sudha = $30x \times [8/5] = 48x$

New income of Sudha = $204x + 48x = 252x$

New income increased by = $252x - 200x = 52x$

..Required percentage = $[52x/200x] \times 100 = 26\%$

20) Let the income of Surbhi = 100

Surbhi spends 75% of her income

Expenditure of Surbhi = 75

Savings of Surbhi = 25

Income increases by 20%,

\rightarrow The new income of Surbhi = 120

Savings decrease by 1%

New savings = $99/100 \times 25 = 99/4$

New Expenditure = New Income - New savings = $120 - 99/4 = 381/4$

Increase in expenditure = $381/4 - 75 = 81/4$

..Percentage increase in expenditure = $81/4 / 75 \times 100 = 81/(4 \times 75) \times 100 = 27\%$