

# Signal Processing - 1 by One

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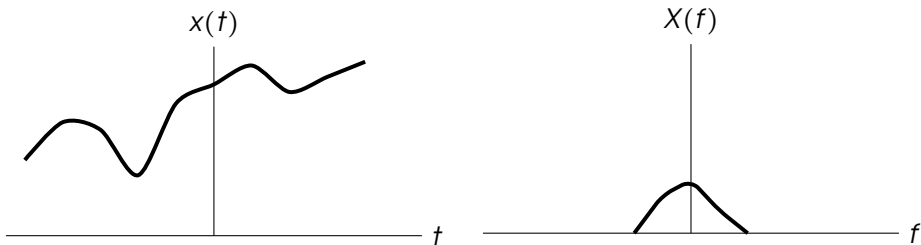
- So Far: Sampling and Convolution
- Fourier Analysis
- Previous Week: Sampling and DTFT
- Today: DTFT and Circular Convolution



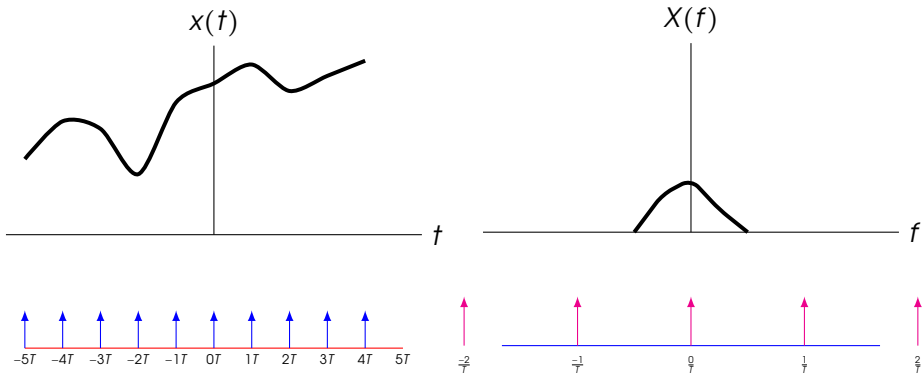
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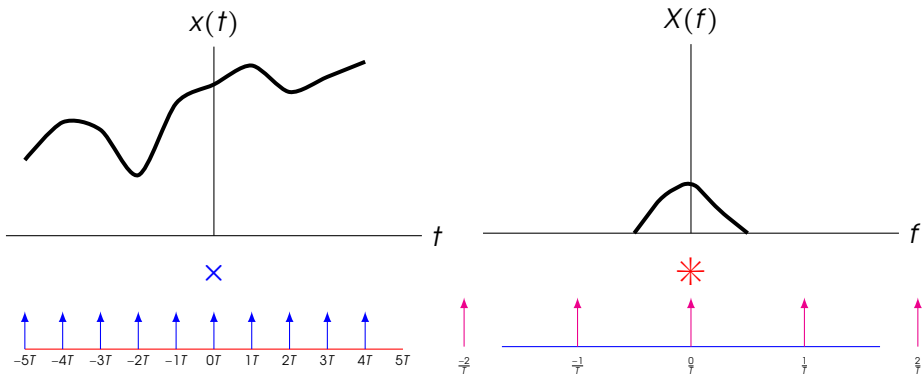
# DTFT Illustration



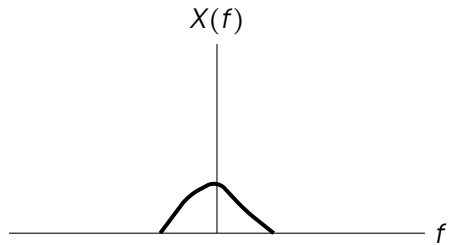
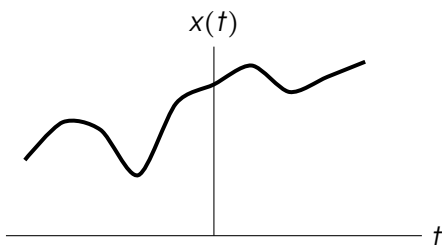
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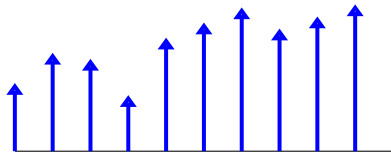
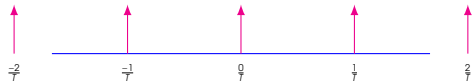
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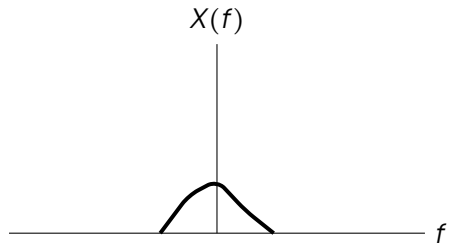
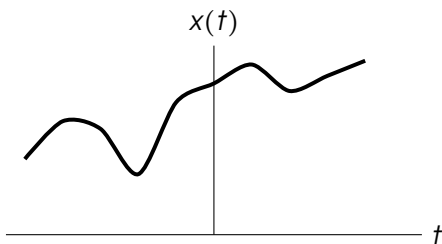
$\times$



$*$



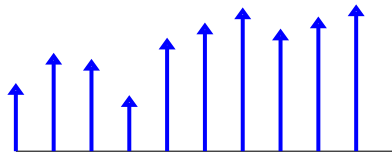
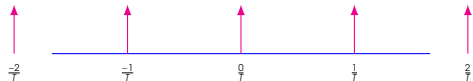
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$\times$



$*$

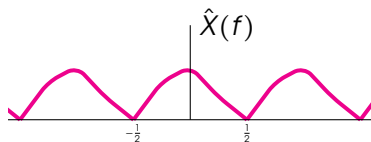
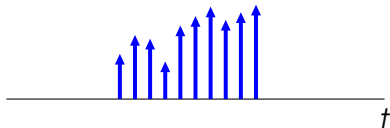


Take  $T = 1$  for DTFT

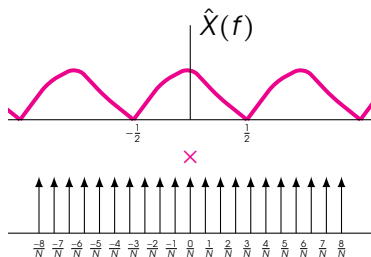
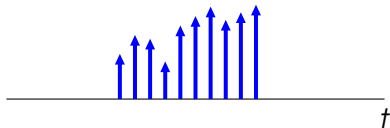




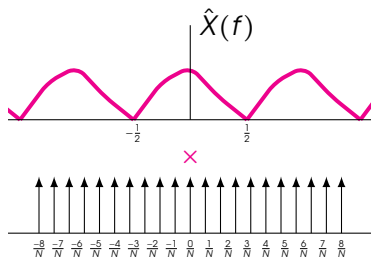
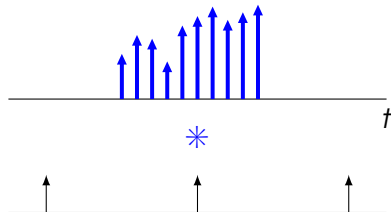
# DFT: Sampling DTFT



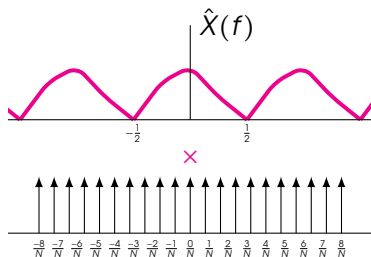
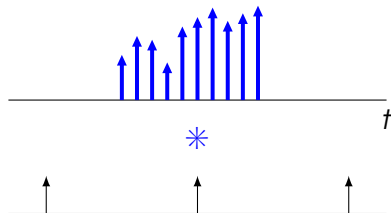
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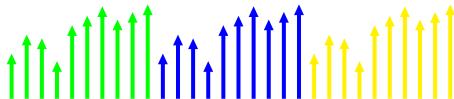
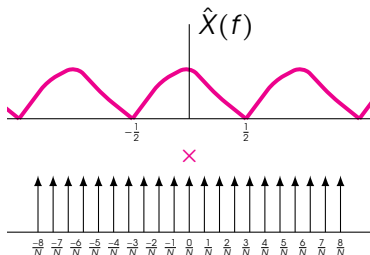
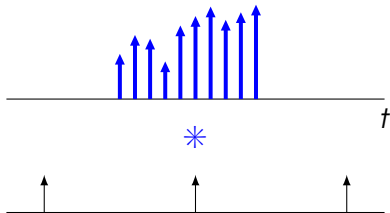
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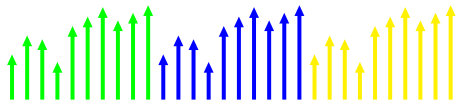
## DFT: Discrete Fourier Transform

$$X[k] = \hat{X}\left(\frac{k}{N}\right) = \sum_{n=0}^{N-1} x[n] \exp\left(-j2\pi \frac{k}{N} n\right).$$

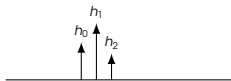


# DFT-DTFT Product

$$x_c[n] = \sum_{l \in \mathbb{Z}} x[n + lN]$$



\*



$$X[k]$$



×



$$y[n] = x_c[n] * h[n]$$

$$\hat{H}\left(\frac{k}{N}\right)\hat{X}\left(\frac{k}{N}\right)$$



# Circular Convolution

$$x[n] \circledast h[n] \triangleq x_c[n] * h[n] \quad \text{"One period"}$$

