```
In []:
import numpy as np
import torch
import torch.utils.data as tud
import torch.nn as tnn
                                                                                                        In [ ]:
import matplotlib.pyplot as plt
                                                                                                        In [ ]:
from copy import deepcopy as dcopy
                                                                                                        In [ ]:
import torchvision as tv
import torchvision.datasets as tvds
                                                                                                        In [ ]:
mnist_trainset = tvds.MNIST(root='./data', train=True, download=True, transform=tv.transforms.ToTensor())
mnist testset = tvds.MNIST(root='./data', train=False, download=True, transform=tv.transforms.ToTensor())
Downloading http://yann.lecun.com/exdb/mnist/train-images-idx3-ubyte.gz to ./data/MNIST/raw/train-
images-idx3-ubyte.gz
Extracting ./data/MNIST/raw/train-images-idx3-ubyte.gz to ./data/MNIST/raw
Downloading http://yann.lecun.com/exdb/mnist/train-labels-idx1-ubyte.gz to ./data/MNIST/raw/train-
labels-idx1-ubyte.gz
Extracting ./data/MNIST/raw/train-labels-idx1-ubyte.gz to ./data/MNIST/raw
Downloading http://yann.lecun.com/exdb/mnist/t10k-images-idx3-ubyte.gz to ./data/MNIST/raw/t10k-images-
idx3-ubyte.gz
Extracting ./data/MNIST/raw/t10k-images-idx3-ubyte.gz to ./data/MNIST/raw
Downloading http://yann.lecun.com/exdb/mnist/t10k-labels-idx1-ubyte.gz to ./data/MNIST/raw/t10k-labels-
Extracting ./data/MNIST/raw/t10k-labels-idx1-ubyte.gz to ./data/MNIST/raw
Processing...
Done!
/usr/local/lib/python3.6/dist-packages/torchvision/datasets/mnist.py:480: UserWarning: The given NumPy
array is not writeable, and PyTorch does not support non-writeable tensors. This means you can write to
the underlying (supposedly non-writeable) NumPy array using the tensor. You may want to copy the array
to protect its data or make it writeable before converting it to a tensor. This type of warning will be
suppressed for the rest of this program. (Triggered internally at
/pytorch/torch/csrc/utils/tensor numpy.cpp:141.)
 return torch.from_numpy(parsed.astype(m[2], copy=False)).view(*s)
                                                                                                        In [ ]:
train_set, val_set = tud.random_split(mnist_trainset, [50000,10000], generator=torch.Generator().manual_s
                                                                                                        In [ ]:
test_set=mnist_testset
                                                                                                        In [ ]:
del mnist testset, mnist trainset
                                                                                                        In [ ]:
# batch size increased for faster training
train_loader = tud.DataLoader(train_set, batch_size=64, shuffle=True, drop_last=True)
val loader = tud.DataLoader(val set, batch size=10000, shuffle=True, drop last=True)
test loader = tud.DataLoader(test set, batch size=10000, shuffle=True, drop last=True)
                                                                                                        In [ ]:
class my_nn_2 (tnn.Module):
  def init (self, h=128, d in=784, d out=10):
    super(my_nn_2, self).__init__()
    self.linear1 = tnn.Linear(d in, h)
    self.linear2 = tnn.Linear(h, d out)
    {\#\ https://medium.com/@zhang\_yang/understanding-cross-entropy-implementation-in-pytorch-softmax-log-superiority.}
     # softmax + nll loss is worse than cross entropy loss
  def forward(self, x):
    h relu = self.linear1(x).clamp(min=0)
    y pred = self.linear2(h relu)
    return y_pred
                                                                                                        In []:
crit bce = tnn.CrossEntropyLoss()
crit mse = tnn.MSELoss()
                                                                                                        In []:
def fit(h=128, epochs=10, criterion=tnn.CrossEntropyLoss(), lr=1e-3):
  model = my nn 2(h)
```

opt = torch.optim.SGD(model.parameters(), lr=lr)

```
tlh=[]
  tah=[]
  vlh=[]
  vah=[]
  vl min=10**10
  for ep in range (epochs):
    model.train()
    training_loss=0
    for (idx, b) in enumerate(train_loader):
      xb=b[0].reshape(-1,784).float()
      yb=b[1]
      yb\_pred = model(xb)
      loss=criterion(yb pred, yb)
      training_loss+=loss
      acc+=torch.sum(torch.argmax(yb_pred, axis=1)==yb)
      opt.zero grad()
      loss.backward()
      opt.step()
    tah.append(acc/50000)
    tlh.append(training_loss/50000)
    model.eval()
    with torch.no_grad():
      val loss=0
      acc=0
      for (idx, b) in enumerate(val_loader):
        xb=b[0].reshape(-1,784).float()
        yb=b[1]
        yb\_pred = model(xb)
        loss=criterion(yb_pred, yb)
        acc+=torch.sum(torch.argmax(yb pred, axis=1)==yb)
        val loss+=loss
      vah.append(acc/10000)
      vl=val loss/64
      if vl<vl min:</pre>
        best model=dcopy(model)
        vl min=vl
      vlh.append(vl)
  return best model, tlh, tah, vlh, vah
                                                                                                            In [ ]:
model, tlh, tah, vlh, vah = fit()
                                                                                                            In [ ]:
plt.plot(tlh, label="train loss")
plt.plot(vlh, label="validation loss")
plt.legend()
plt.show()
0.035
                                     train loss
                                     validation loss
0.030
0.025
0.020
0.015
0.010
plt.plot(tah, label="train accuracy")
plt.plot(vah, label="validation accuracy")
plt.legend()
```

plt.show()

```
train accuracy
        validation accuracy
0.7
0.6
0.5
0.4
0.3
                        4
              ż
                                           8
     Ó
                                                                                                                     In []:
hl_sizes=[32,64,128,256,512]
best_vl=[]
for hl in hl_sizes:
  _, tlh, tah, vlh, vah = fit(h=hl, epochs=20, lr=1e-3)
  best_vl.append(np.min(vlh))
                                                                                                                     In [ ]:
plt.plot(hl_sizes, best_vl)
plt.show()
0.00750
0.00745
0.00740
0.00735
0.00730
0.00725
0.00720
0.00715
0.00710
                      200
                               300
                                        400
                                                 500
                                                                                                                     In []:
# h=512 gives best results
                                                                                                                     In []:
lr_vals=[10**(i-5) for i in range(5)]
best_vl=[]
for lr in lr_vals:
   _, tlh, tah, vlh, vah = fit(epochs=20, lr=lr)
  best_vl.append(np.min(vlh))
                                                                                                                     In [ ]:
plt.plot(np.log10(lr_vals), best_vl)
plt.xlabel = "Learning rate as a power of 10"
plt.show()
0.035
0.030
0.025
0.020
0.015
0.010
```

In []:

1r=0.1 gives best results

-4.0 -3.5

-3.0 -2.5

-2.0 -1.5

-4.5

0.005

-5.0