

EE324, Control Systems Lab, Problem sheet 9

(Report submission date: 19th Oct 2021)

Q1) Compare Nyquist plots of a transfer function $G(s) = \frac{10}{s(\frac{s}{5} + 1)(\frac{s}{20} + 1)}$ and $C(s)G(s)$,

where $C(s)$ is:

i) A lag compensator with transfer function $\frac{s+3}{s+1}$

ii) A lead compensator with transfer function $\frac{s+1}{s+3}$

Comment on the variation in the gain margin and phase margin for $C(s)G(s)$ in comparison to the gain margin and phase margin of $G(s)$ for the cases (a) and (b).

Q2) A “Notch filter” is a band stop filter or band-reject filter that has a very low gain at a particular frequency. Determine a transfer function of a notch filter that rejects (or attenuates) a 50 Hz signal. Comment on a method to modify (or adjust) the steepness of the magnitude plot for the notch filter and prove the same by comparing the corresponding bode plots.

Q3) For the transfer function $C(s) = \frac{100}{s+30}$ how much **minimum delay** (in seconds) would be needed to destabilize the **closed-loop system**. Compare the Bode plots (magnitude and phase) of $C(s)$ and $C(s)G(s)$ where $G(s)$ is the delay calculated to achieve the destabilization. What can you comment on the gain and phase margins, with and without the delay?

Q4) For the given open-loop system $G(s) = \frac{1}{(s^3 + 3s^2 + 2s)}$, observe the difference in the gain

margin magnitudes on applying the following four techniques:

- i) Root-locus
- ii) Nyquist plot
- iii) Bode-plots: using the asymptotic plot for calculating the gain margin
- iv) Bode-plots: using the actual plot for calculating the gain margin

Q5) For the given open-loop system $G(s) = \frac{10s + 2000}{(s^3 + 202s^2 + 490s + 18001)}$, perform the

following operations:

- i) Plot the bode plot (magnitude and phase) of the system and comment on the gain margin and phase margin of the system.
- ii) Add a proportional gain ‘K’ to improve the steady-state error to 10% for the step response of the closed-loop system.
- iii) Observe the new phase and gain crossover frequencies and the gain and phase margins for the system obtained in question 5 (ii).

- iv) To improve the phase margin of the system obtained in question 5 (ii), cascade the open-loop system of question 5 (ii) with a zero such that the phase margin is greater than or equal to 90 degrees, but **without altering the dc gain** of the closed-loop system.
- v) Comment on the closed-loop system stability for the transfer function obtained in question 5 (iv).

Report Format:

Q1) Shows the nyquist plots of all the three required systems and comments as per question.

Q2) Show the Bode-plot of the obtained transfer function and write your answer along with the reason/explanation.

Q3) Show the Bode-plot of the transfer function and delayed transfer function and write your answer along with the reason/explanation.

Q4) a) Show the plot of the root locus.

b) Show the Nyquist plot of the transfer function

c) Show the Asymptotic bode-plot of the transfer function

d) Show the Bode-plot of the transfer function.

Q5) a) Show the Bode-plot of the transfer function

b) Show the Bode-plot of the closed-loop transfer function

c) Write your observation.

d) Show the Bode-plot

e) State your answer along with the reason/explanation.

Note:

- **At least these are things to be added to the report and if anyone wants to add extra required plots/values can be also added.**
Add the Scilab code for all questions.