

A Closed Time-Reversal Cavity for Electromagnetic Waves in Transmission Line Networks

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Abstract—A closed time-reversal (TR) cavity has been considered a purely theoretical concept whose experimental realization was assumed to be impossible. In this article, we demonstrate that it is, in fact, possible to realize a closed TR cavity using a network of transmission lines. The network is excited by either lumped voltage or current sources at arbitrary locations, and it is terminated on matched impedances. This system is an exact closed TR cavity in the sense that, in the backward-propagation stage, by back-injecting time-reversed measured responses (voltage or current) generated by a source at each line terminal, a time-reversed copy of the current and voltage distribution in the forward-propagation stage is obtained. We report for the first time an experimental realization of a TR cavity formed by a network of inhomogeneous transmission lines, in which the spatial and temporal signal distribution along the network is reproduced as in a sequence of the system state (i.e., voltages and or current along the lines) being played in reverse. We also discuss the interfering effect of the so-called diverging wave for observation points in the vicinity of the source. An active realization of a TR sink is proposed to effectively overcome the interfering effect caused by the diverging waves.

Index Terms—Electromagnetic time reversal (TR), electromagnetic wave, TR cavity, TR sink, transmission line.

I. INTRODUCTION

THE concept of a closed TR cavity was proposed by Cassereau and Fink (see [1]–[3]) for acoustic waves, and it was later extended to electromagnetic waves using the Lorentz reciprocity principle [4]. A TR cavity extends the concept of a TR mirror (e.g., [5]–[9]), a technique to refocus waves in a propagative medium back to the source [10]–[17].

A closed TR cavity for electromagnetic waves can be briefly described as follows. Consider the situation wherein a source is

situated in a linear, nonmagnetic, and time-invariant medium. Note that the medium can be inhomogeneous (see Fig. 1). Assume a closed, 3-D surface S surrounding the source and its ambient medium [Fig. 1(a)]. The source emits an electromagnetic pulse. Suppose that we are able to determine the tangential fields generated by the source at any point on this surface [Fig. 1(b)]. Making use of the equivalence theorem, it is possible to replace the source by equivalent electric and magnetic current sources (on the surface S) [Fig. 1(c)]. Time reversing the equivalent sources on the surface results in the TR of the electromagnetic fields within the cavity surface [Fig. 1(d)]. An observer would see the fields propagate inward, retracing the exact path the electromagnetic waves had followed as in a film being played in reverse or, equivalently, as if the observer were traveling backwards in time. The fields would then converge back to their originally generated location.

The concept of closed TR cavity allows therefore refocusing a wave back to its source, using a two-stage process. In the forward-propagation stage, generally named *direct time* (abbreviated as DT) in the TR theory, the electromagnetic fields generated by the source are determined, either theoretically or experimentally, over the surface S forming the cavity. Then in the backward-propagation stage, named *reversed time* (abbreviated as RT), the original source is removed from the medium and equivalent time-reversed sources (named secondary sources) on the surface are applied. The resulting field in the backward-propagation stage will be a time-reversed copy of that of the forward-propagation stage and, thus, it will converge back to the source.

It is generally assumed that the closed TR cavity is impossible to achieve experimentally because it requires an infinite number of observation points (e.g., transducers) covering a closed 3-D surface around the medium to obtain information about all wavefronts propagating in all directions¹ [1], [18]. In practice, the source-generated fields (e.g., acoustic or electromagnetic) are measured using a limited number of transducers in a layout over a finite angular aperture, namely a TR mirror. Even though the focusing property of TR remains intact (see [7], [18]–[20]), the field distribution resulting from the injection of the time-reversed fields back into the medium will not be an exact time-reversed copy of the fields in the forward stage.

¹One can use a finite number of transducers located at distances of $\lambda_{\min}/2$, from one another, λ_{\min} being the minimum wavelength associated with the source excitation. Still, the number of transducers can be quite significant for high-frequency sources, and the measured waveforms can be affected by cross-coupling between adjacent transducers.

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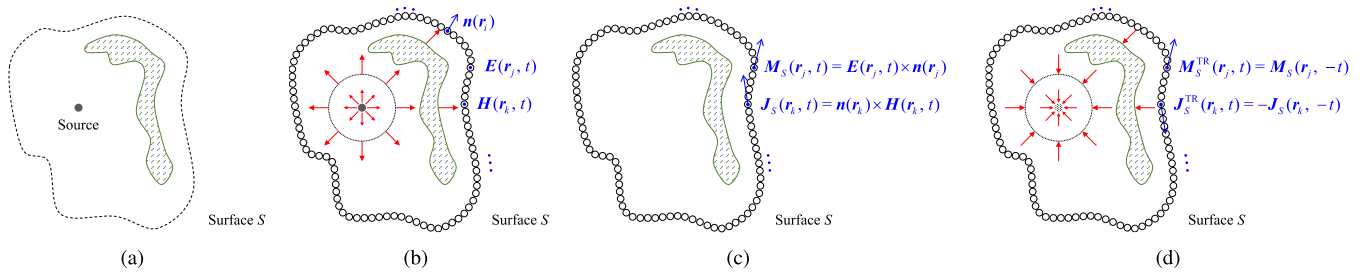


Fig. 1. Schematic of a closed TR cavity. (a) Assume a closed, 3-D surface S surrounding a source and its ambient inhomogeneous medium. (b) Tangential fields generated by the source at any point on the surface S are determined. (c) Source is replaced by equivalent electric and magnetic current sources J_s and M_s . (d) Time reversing the equivalent sources on the surface results in time reversing the electromagnetic fields within that surface.

In this article, we demonstrate that a closed TR cavity can, in fact, be realized using a transmission line network. Such a TR cavity requires a finite number of observation points located at the network terminals.

This article is structured as follows. Section II describes the realization of a closed TR cavity for electromagnetic waves in transmission line networks. Section III illustrates the concept with a Y-shaped coaxial-cable network, and it includes a derivation of the forward- and backward-prorogation stages' wave equations. In Section IV, a numerical and experimental validation of the proposed TR cavity is presented. A discussion is given in Section V on the effects of the backward-stage diverging process and an active realization of a TR sink. Lastly, Section VI concludes this article with final remarks.

II. REALIZATION OF A CLOSED TIME-REVERSAL CAVITY USING A NETWORK OF TRANSMISSION LINES

Consider a transmission line network formed by coaxial shielded cables with an arbitrary topology as shown in Fig. 2(a). Such networks can be found in various applications, e.g., in electronic and communications circuits, and in underground power networks. Let the transmission line network be excited by an impulsive voltage or current source located at an arbitrary point along one of the line branches [see the red dot along branch 1 in Fig. 2(b)]. Consider also a closed surface S (dotted line in Fig. 2) that surrounds the network passing through each one of its terminals. Note that the network can be inhomogeneous and nonuniform in the sense that the transmission lines that form the network can have different characteristics, such as propagation speed and cross-sectional dimension. Note also that the network can have any number of branches and nodes, and any number of sources, either voltage or current.

Applying the concept of the closed TR cavity to Fig. 2 implies considering a matched load at each line terminal in such a way that electromagnetic energy is only going outward from the cavity.

The electromagnetic field propagation in such a system is confined within the cable (i.e., in the space between the inner conductor and the sheath). Furthermore, as long as the transverse dimensions of the cables forming the network are electrically small², the wave propagation along the conducting

²For example, a communication cable of about 1 cm diameter is electrically small for signals with a frequency content of up to a few GHz.

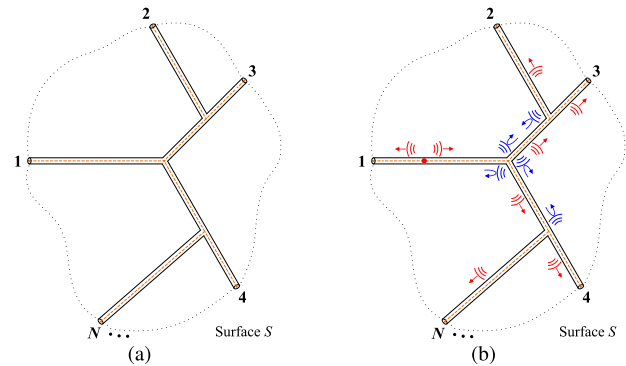


Fig. 2. Closed TR cavity in a transmission line network composed of coaxial shielded cables. The network can have any arbitrary topology with any number of junctions and nodes. (a) Closed surface S represented by a dotted line surrounds the network passing through each terminal of the network (labeled 1 to N). (b) Transmission line network is excited by a voltage or current pulse source (represented by the red dot). The transmitted electromagnetic waves (red color) propagate along the network. At the inner nodes, parts of the waves are transmitted to connected branches and parts of them, shown in blue, are reflected back.

cables is transverse electromagnetic (TEM) [21]. Therefore, the field characteristics at every terminal are totally determined by the measured output signal (either current or voltage).

Furthermore, the only locations on the surface S at which electromagnetic fields are nonzero are at the line terminals. In other words, the considered system allows realizing a closed TR cavity using a finite number of measurements equal to the number of network terminals. The current or voltage distribution along the network, resulting from the back-injection of the time-reversed signals from all terminals, will be an exact time-reversed copy of its distribution in the forward-propagation stage.

III. ILLUSTRATION OF THE CONCEPT OF A CLOSED TIME-REVERSAL CAVITY USING A Y-SHAPED TRANSMISSION LINE NETWORK

A. Closed Time-Reversal Cavity in a Y-Shaped Transmission Line Network

The proposed closed TR cavity in a transmission line cable network is a general concept and it applies to any arbitrary multiterminal, multinode topology. To illustrate the concept, we will consider here an inhomogeneous Y-shaped network (see Fig. 3), for which the solutions of the wave equations in the forward and the backward stages can be found analytically.

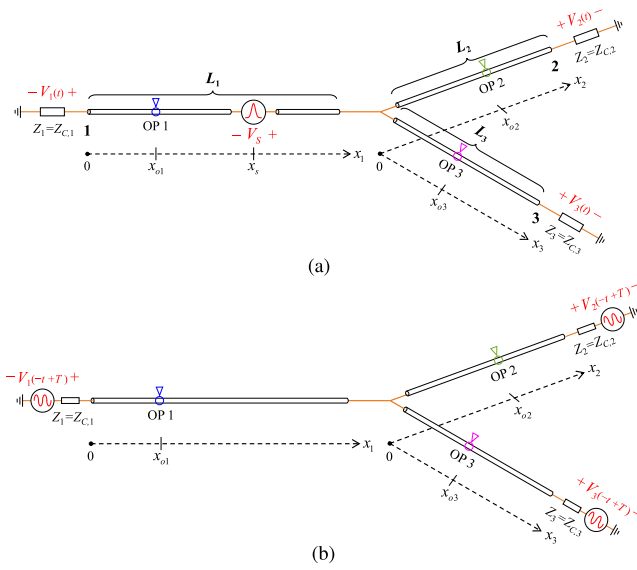


Fig. 3. Realization of a closed TR cavity in a Y-shaped inhomogeneous coaxial-cable network. (a) Forward-propagation stage: DT. (b) Backward-propagation stage: RT.

As illustrated in Fig. 3(a), in the forward-propagation stage, a voltage pulse is injected into the inner conductor of the coaxial cable at a given location along Line branch 1 (along the x_1 axis) and induced voltage responses are observed at the three network terminals (labeled 1 to 3). In the backward-propagation stage [see Fig. 3(b)], the recorded voltages are time reversed and synchronously back injected into the network from the respective line terminals. In order to show that the temporal and spatial signal distribution along the entire network can be reproduced in reverse sequence, three arbitrary observation points (identified as OP 1–3 in Fig. 3) are considered.

B. Wave Equations in the Closed Time-Reversal Cavity

In this section, wave equations are derived to describe the TR forward- and backward-propagation processes in the Y-shaped cable network of Fig. 3. Without loss of generality, the derivation focuses on the voltage wave. To ensure the TR invariance of the wave equations, let us assume for now a lossless medium.

We use voltage reflection coefficients in the transmission line theory to describe the boundary conditions at the network terminals and at the junction of the three line branches. Taking into account directionality, the instantaneous voltage reflection coefficient at the junction can be defined as

$$\rho_{j,k}^i = \frac{Z_{j,k} - Z_{C,i}}{Z_{j,k} + Z_{C,i}}, \quad i \in U = \{1, 2, 3\}, \quad j, k \in \mathbb{C}_U \quad (1)$$

where the superscript i corresponds to the number of the line branch, along which incident voltage waves propagate, and the subscript pair j, k combines the numbers of the other two lines connected to the junction. $Z_{C,i}$ refers to the line characteristic impedance and $Z_{j,k}$ is the input impedance of the other two line branches seen from the junction. The input impedance for a matched transmission line being equal to its characteristic

impedance, $Z_{j,k}$ can be thus calculated as

$$Z_{j,k} = \frac{Z_{C,j} \cdot Z_{C,k}}{Z_{C,j} + Z_{C,k}}. \quad (2)$$

In the forward-propagation stage [see Fig. 3(a)], responding to the series voltage source $V_s(t)$ exciting the coaxial-cable network at $x_1 = x_s$, the voltage waves recorded at the terminals (representing the cavity surface) read

$$V_1(t) = -\frac{1}{2}V_s\left(t - \frac{x_s}{v_1}\right) + \rho_{2,3}^1 \cdot \frac{1}{2}V_s\left(t - \frac{L_1 - x_s}{v_1} - \frac{L_1}{v_1}\right) \quad (3)$$

$$V_2(t) = (1 + \rho_{2,3}^1) \cdot \frac{1}{2}V_s\left(t - \frac{L_1 - x_s}{v_1} - \frac{L_2}{v_2}\right) \quad (4)$$

$$V_3(t) = (1 + \rho_{2,3}^1) \cdot \frac{1}{2}V_s\left(t - \frac{L_1 - x_s}{v_1} - \frac{L_3}{v_3}\right) \quad (5)$$

which are obtained considering the matched boundary conditions at the network terminals. v_i refers to the wave propagation speed along the corresponding line branch.

We now take the voltage wave at the observation point OP1 $x_1 = x_{o1}$ located between $x_1 = 0$ and the source point $x_1 = x_s$ as an example³

$$V_{x_{o1}}^{\text{DT}}(t) = -\frac{1}{2}V_s(t - \tau_1') + \rho_{2,3}^1 \cdot \frac{1}{2}V_s(t - \tau_1''), \quad (x_{o1} < x_s) \quad (6)$$

with the propagation delays respectively being

$$\tau_1' = \frac{x_s - x_{o1}}{v_1} \quad (7)$$

and

$$\tau_1'' = \frac{2L_1 - x_s - x_{o1}}{v_1}. \quad (8)$$

We denote the time-reversed copy of $V_i(t)$ as

$$V_i^{\text{tr}}(t) = V_i(T - t) \quad (9)$$

where, to ensure causality, the TR operation is given by the transformation

$$t \Rightarrow T - t \quad (10)$$

with T being the length of the time window over which the terminal voltage responses are recorded.

In the backward-propagation stage [see Fig. 3(b)], the synchronous excitation of the time-reversed sources [also named secondary sources relative to the original source $V_s(t)$] generates the voltage wave at $x_1 = x_{o1}$ through

$$V_{x_{o1}}^{\text{RT}}(t) = \sum_{i=1}^3 V_{x_{o1}}^{\text{RT}; V_i^{\text{tr}}}(t) \quad (11)$$

where V_i^{tr} in the superscript indicates the individual contribution from the time-reversed voltage $V_i^{\text{tr}}(t)$ being separately

³The superscripts DT and RT are used to indicate, respectively, that the signals are evaluated in the forward- and backward-propagation stage (i.e., DT and RT) of the closed TR cavity.

back injected at its corresponding terminal. The contributions can be readily obtained as⁴

$$V_{x_{o1}}^{\text{RT};V_1^{\text{tr}}}(t) = \frac{1}{2} \cdot 2V_1^{\text{tr}}\left(t - \frac{x_{o1}}{v_1}\right) + \rho_{2,3}^1 \cdot \frac{1}{2} \cdot 2V_1^{\text{tr}}\left(t - \frac{L_1}{v_1} - \frac{L_1 - x_{o1}}{v_1}\right) \quad (12)$$

$$V_{x_{o1}}^{\text{RT};V_2^{\text{tr}}}(t) = (1 + \rho_{1,3}^2) \cdot \frac{1}{2} \cdot 2V_2^{\text{tr}}\left(t - \frac{L_2}{v_2} - \frac{L_1 - x_{o1}}{v_1}\right) \quad (13)$$

$$V_{x_{o1}}^{\text{RT};V_3^{\text{tr}}}(t) = (1 + \rho_{1,2}^3) \cdot \frac{1}{2} \cdot 2V_3^{\text{tr}}\left(t - \frac{L_3}{v_3} - \frac{L_1 - x_{o1}}{v_1}\right). \quad (14)$$

Substituting (12)–(14) into (11) yields (15), as shown at the bottom of the page.

According to the boundary condition at the junction,

$$\rho_{2,3}^1 + \rho_{1,3}^2 + \rho_{1,2}^3 = -1. \quad (16)$$

Using (16), $V_{x_{o1}}^{\text{RT}}(t)$ is simplified as (17), as shown at the bottom of the page.

Following a similar approach, we can derive the solutions for the voltage waves observed along Line branch 2 (i.e., at $x_2 = x_{o2}$) in the forward- and backward-stages

$$V_{x_{o2}}^{\text{DT}}(t) = (1 + \rho_{2,3}^1) \cdot \frac{1}{2} V_S(t - \tau_2) \quad (18)$$

with

$$\tau_2 = \frac{L_1 - x_s}{v_1} + \frac{x_{o2}}{v_2} \quad (19)$$

and

$$V_{x_{o2}}^{\text{RT}}(t) = \underbrace{(1 + \rho_{2,3}^1) \cdot \frac{1}{2} V_S(T - t - \tau_2)}_{\text{Converging}} - \underbrace{(1 + \rho_{2,3}^1) \cdot \frac{1}{2} V_S(T - t + \tau_2)}_{\text{Diverging}}. \quad (20)$$

The voltage wave expression obtained at the observation point $x_3 = x_{o3}$ along Line branch 3 has a similar form as that at $x_2 = x_{o2}$

$$V_{x_{o3}}^{\text{DT}}(t) = (1 + \rho_{2,3}^1) \cdot \frac{1}{2} V_S(t - \tau_3) \quad (21)$$

⁴When $V_i^{\text{tr}}(t)$ is back injected as the secondary source, a voltage division ratio of 1/2 caused by the matched boundary condition at the network terminal is introduced. As seen in (12)–(14), $V_i^{\text{tr}}(t)$ is multiplied by 2 to offset the dividing effect, to be consistent with the generic definition of the closed TR cavity.

$$V_{x_{o3}}^{\text{RT}}(t) = \underbrace{(1 + \rho_{2,3}^1) \cdot \frac{1}{2} V_S(T - t - \tau_3)}_{\text{Converging}} - \underbrace{(1 + \rho_{2,3}^1) \cdot \frac{1}{2} V_S(T - t + \tau_3)}_{\text{Diverging}} \quad (22)$$

where

$$\tau_3 = \frac{L_1 - x_s}{v_1} + \frac{x_{o3}}{v_3}. \quad (23)$$

We now use the expressions (21) and (22) of $x_3 = x_{o3}$ as an example to interpret the properties of the voltage wave propagation in the forward- and backward-propagation stages.

Basically, the voltage wave observed in the backward stage consists of two components, which arrive at the observation point one after the other. The later-arriving component [i.e., the second term in (22)] is an inverted and time-delayed copy of the first wave. The two components are respectively generated by the processes of the time-reversed terminal responses (back injected by the secondary sources) converging to and diverging from the original source location. For this reason, the two components are referred to, respectively, as the “converging” and “diverging” terms in (22), in agreement with the terminology used in [1]–[3].

It is important to note that only the converging wave in the backward stage behaves as a time-reversed copy of the voltage wave in the forward stage, whereas the diverging component does not have any counterpart in the forward stage. This can be clearly seen by comparing equations (17), (20) and (22) with their forward-stage counterparts, namely equations (6), (18) and (21), respectively. In other words, the earlier-arriving converging component is a mirror image of the voltage wave observed in the forward stage with respect to the recording time-window length T .

We now discuss the interfering effect⁵ caused by the diverging wave for observation points located in the region near the source location.

For ease of explanation, the components of $V_{x_{o1}}^{\text{RT}}$ in (17) are arranged in chronological order according to the instants when they arrive at the observation point $x_1 = x_{o1}$. It can be seen that the difference (denoted by τ) between the instants of the converging and diverging components, respectively, arriving at $x_1 = x_{o1}$ is twice the prorogation delay τ_1' . An immediate consequence of this fact is that the diverging voltage wave

⁵Note that Fink *et al.* [1]–[3] used the term “distortion” in their articles. We preferred to use here instead the term interfering to avoid any confusion with the concept of distortion in communication systems.

$$2V_{x_{o1}}^{\text{RT}}(t) = -V_S(T - t - \tau_1') + \rho_{2,3}^1 \cdot V_S(T - t - \tau_1'') - \rho_{2,3}^1 \cdot V_S(T - t + \tau_1') + (\rho_{2,3}^1)^2 \cdot V_S(T - t + \tau_1') \\ + (1 + \rho_{1,3}^2) \cdot (1 + \rho_{2,3}^1) \cdot V_S(T - t + \tau_1') + (1 + \rho_{1,2}^3) \cdot (1 + \rho_{2,3}^1) \cdot V_S(T - t + \tau_1') \quad (15)$$

$$V_{x_{o1}}^{\text{RT}}(t) = \underbrace{\rho_{2,3}^1 \cdot \frac{1}{2} V_S(T - t - \tau_1'') - \frac{1}{2} V_S(T - t - \tau_1') + \frac{1}{2} V_S(T - t + \tau_1')}_{\text{Converging}} - \underbrace{\rho_{2,3}^1 \cdot \frac{1}{2} V_S(T - t + \tau_1')}_{\text{Diverging}} \quad (17)$$

overlaps the converging one at the region near the source location that is characterized by a relatively small τ'_1 . The two voltage waves can be completely separated in time if τ is greater than the temporal duration T_S of the voltage source $V_S(t)$. Thus, this interference would affect only the observation point that is located around the source and is characterized by the abscissa $x_1 = x_{o1}$ satisfying

$$|x_{o1} - x_s| \leq \frac{1}{2} v_1 \cdot T_S. \quad (24)$$

Here, without loss of generality, we assume that Line branch 1 is long enough so that the interfering region is confined along the line branch where the source excitation is originally injected.

This conclusion is also analogous to that of the TR cavity for acoustic waves in free space [1]–[3].

In summary, the closed TR cavity is realized for the observation points that satisfy the following condition:

$$V^{\text{RT},c.}(x, t) = V^{\text{DT}}(x, T - t), \quad \left(x > x_s \pm \frac{1}{2} v_1 \cdot T_S \right) \quad (25)$$

where $V^{\text{RT},c.}(x, t)$ represents the converging component of the voltage wave at a generic location x along the network.

IV. NUMERICAL AND EXPERIMENTAL VALIDATION

The preceding analysis demonstrated the realization of a closed TR cavity for electromagnetic waves in transmission line networks. It was shown that the voltage wave resulting from the converging process in the backward stage is a time-reversed copy of the voltage wave that was originally generated by the source in the forward stage. This section presents numerical and experimental validation of the proposed closed TR cavity. To this end, the generic Y-shaped inhomogeneous cable network of Fig. 3 is experimentally realized using the setup described in Fig. 4.

The proposed network is composed of three line branches and five segments of coaxial cables. As detailed in Table I, Line branches 1 and 2 are RG-58 coaxial cables, which are, respectively, 45 and 26 m in length. Note that Line branch 3 contains a mix of three line sections comprising RG-59 and RG-179 coaxial cables. The main parameters of the adopted RG-58, RG-59, and RG-179 standard coaxial cables are summarized in Table II. The three types of cables feature different characteristic impedances, wave propagation speeds and cross-sectional dimensions. As a result, the considered cable network is characterized by a high degree of inhomogeneity.

Matching the coaxial-cable network under study consists of terminating RG-58 and -59 cables with lumped resistors of 50 and 75 Ω , respectively. Note that matched impedances are only required at the external terminations.

Fig. 5 illustrates the profile of a modified Gaussian pulse that was adopted as the source signal of the series voltage source $V_S(t)$ to excite the network in the forward-propagation stage. The $1/e$ pulsewidth of the injected Gaussian pulse is 38 ns. In this respect, the width is sufficiently small in the light of the propagation delays of the line branches.

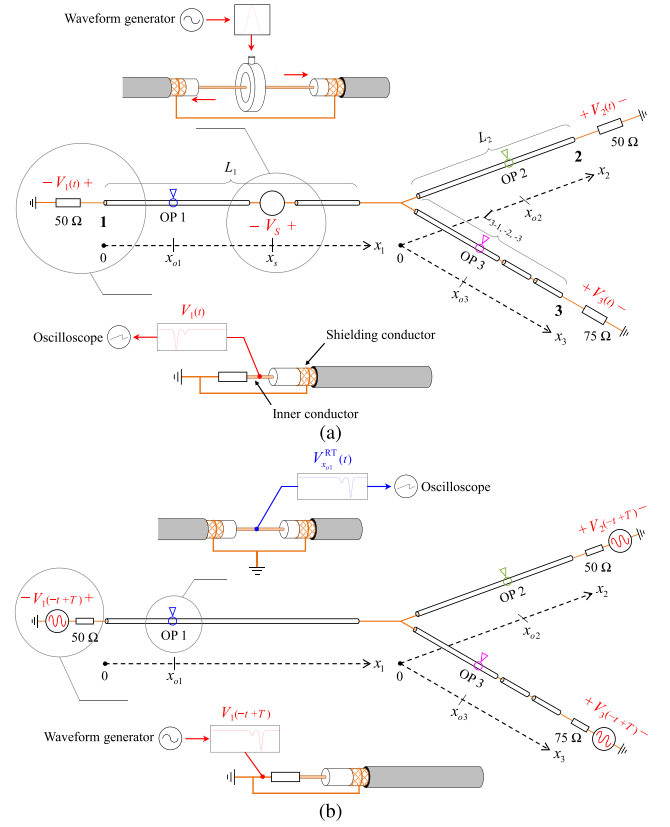


Fig. 4. Experimental setups realizing a TR cavity in a Y-shaped transmission line network. (a) Forward-propagation stage: DT . (b) Backward-propagation stage: RT .

TABLE I
CONFIGURATION OF THE SETUP DESCRIBED IN FIG. 4

Line branch	Cable	Length
1 (along the x_1 axis)	RG-58	L_1 45 m
2 (along the x_2 axis)	RG-58	L_2 26 m
3 (along the x_3 axis)	RG-59	L_{3-1} 14 m
	RG-179	L_{3-2} 4 m
	RG-59	L_{3-3} 4 m

TABLE II
MAIN PARAMETERS OF RG-58/59/179 COAXIAL CABLE

	RG-58	RG-59	RG-179
Characteristic impedance (Ω)	50	75	75
Propagation speed (% of the speed of light)	66	65.8	69
Nom. attenuation (dB/m) ($f \leq 35$ MHz)	0.07	0.06	0.14
Diameter of inner/shielding conductor (mm/mm)	0.9/3.6	0.58/4.5	0.31/2

A. Numerical Validation

The voltage wave propagation along the cable network representing a closed TR cavity was first numerically simulated within the EMTP-RV environment [22], [23]. In the numerical simulations, losses in the coaxial cables were disregarded as in the foregoing derivation. This way, the TR invariance of the underlying telegrapher's equations is strictly satisfied.

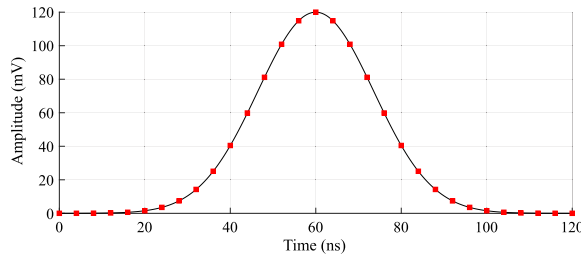


Fig. 5. Modified Gaussian pulse as the excitation signal of the series voltage source $V_S(t)$. The red squares show the sampling points which correspond to the 250 MS/s sampling rate of the adopted arbitrary waveform generator.

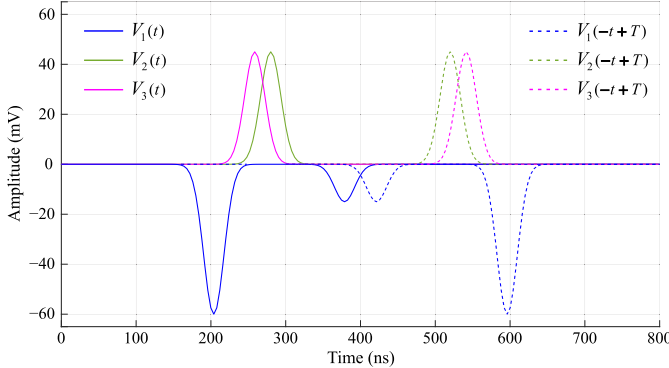


Fig. 6. Simulated terminal voltage waveforms $V_i(t)$ in the forward-propagation stage of the closed TR cavity. The terminal responses are time reversed as $V_i(T - t)$ and plotted in dashed lines.

In accordance with the setup described in Fig. 4(a), Fig. 6 presents the terminal voltages $V_i(t)$ (i being 1–3) simulated in the forward-propagation stage of the TR cavity. The series voltage source $V_S(t)$ injected the Gaussian pulse at $x_1 = x_s = 28$ m, giving rise to the voltage wave propagating toward the network terminals. The voltage responses at the terminals were observed in a time window T of 800 ns. The voltages $V_i(t)$ were then time reversed and shifted in time by T as $V_i(T - t)$. The two sets of waveforms are superimposed in Fig. 6. The original waveforms $V_i(t)$ and their time-reversed images $V_i(T - t)$ are symmetrical with respect to the middle point of the time window T (i.e., $t = 400$ ns).

For simulating the backward propagation, the time-reversed voltages $V_i(T - t)$ were synchronously back injected into the network. In view of the line parameters reported in Tables I and II, the interfering effect caused by the diverging process in the Y-shaped cable network can be eliminated by considering the observation points with a coordinate satisfying either $x_1 \leq 16$ m or $x_1 \geq 40$ m. Fig. 7 presents the simulated voltage waves in the forward-propagation stage (solid lines) and the backward-propagation stage (dashed lines) at the three observation points, which are located along the three line branches with the coordinates $x_1 = x_{o1} = 4$ m, $x_2 = x_{o2} = 17$ m and $x_3 = x_{o3} = 12$ m, respectively. As analyzed previously, the observed voltage waves contributed by the converging process in the backward stage are exact time-reversed copies of the voltage waves propagating in the forward stage.

B. Experimental Validation

The proposed Y-shaped coaxial-cable network realizing a closed TR cavity was validated experimentally. The expanded

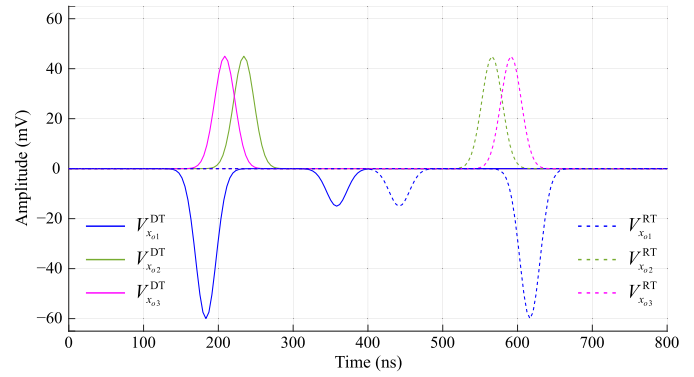


Fig. 7. Simulated voltage waveforms at the considered observation points. Solid lines: forward-stage voltages. Dashed lines: backward-stage voltages.

TABLE III
MAIN CHARACTERISTICS OF THE EXPERIMENTAL DEVICES

	CP ^a	AWG ^b	Osc. ^c
Bandwidth	200 MHz	125 MHz	350 MHz
Sampling rate	–	250 MS/s	2.5 GS/s
Vertical resolution	–	16 bit	14 bit

^aCurrent probe, ^bArbitrary waveform generator and ^cOscilloscope

views included in Fig. 4 describe the involved experimental devices and approaches. The main specifications of the devices used in the experiment are summarized in Table III. Note that the spectrum of the Gaussian pulse of Fig. 5 extends to significant frequencies of up to 10 MHz.

In the forward-propagation stage, an arbitrary waveform generator was used in combination with a Pearson 1 V/A (50 turns) broadband current transformer for the generation and injection of a voltage pulse into the inner conductor of the coaxial cable [see Fig 4(a)]. Corresponding to the simulation scenario, the current probe was positioned along Line branch 1 at $x_1 = x_s = 28$ m. With the injection of a signal from the secondary coil, the current probe behaves as a voltage transformer with a transformation ratio of 50:1. Therefore, the same Gaussian pulse shown in Fig. 5 was applied to the secondary coil of the current probe but with a peak value of 6 V. This way, the generated voltage pulse, which is equivalent to the excitation of the series voltage source $V_S(t)$ in the inner conductor in Fig. 4(a), has a peak value of 120 mV. At the matched line terminals, the induced voltage responses were recorded by means of an oscilloscope.

The measured terminal voltages are shown in Fig. 8. In the same figure, the simulated counterparts are also presented in black lines for the sake of comparison. It can be seen that, except for the peak values that are attenuated in the measured signals, the overall simulated and measured waveforms are in high-grade agreement. The attenuation is essentially due to the losses in the cables, which were not considered in the simulations.

As described in Fig. 4(b), in the backward stage, the responses acquired in the forward stage at the network terminals were reversed in time and synchronously back injected into the network from the respective terminals using an arbitrary waveform generator.

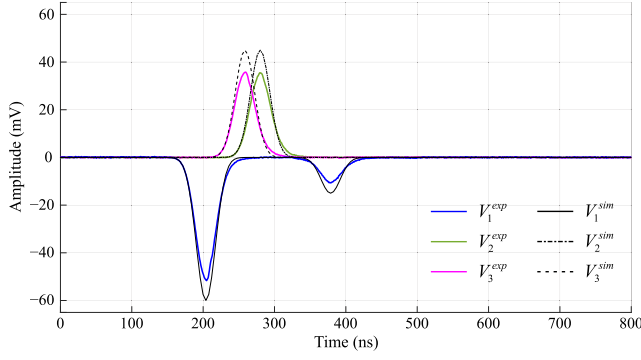


Fig. 8. Experimentally recorded terminal voltage waveforms $V_i(t)$ (indicated by the superscript *exp* in the legend) in the forward stage. The simulated waveforms (indicated by the superscript *sim*) are shown in black (solid for V_1 , dash-dotted for V_2 and dashed for V_3).

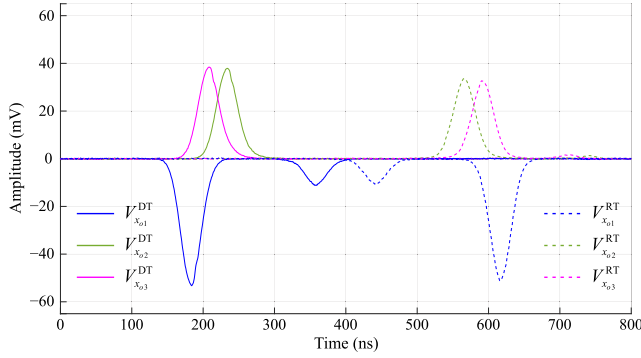


Fig. 9. Experimentally recorded voltage waveforms at the considered observation points. Solid lines: forward-stage voltages. Dashed lines: backward-stage voltages.

Fig. 9 presents the voltages measured in the forward stage (solid lines) and in the backward stage (dashed lines) at the three considered observation points. It is evident that the observed signals in the backward stage (more precisely of the converging process) are nearly perfect time-reversed copies of the ones originally present in the forward stage. The difference between the two stages' voltages is the slight attenuation in amplitude, which stems from losses in the cables. Note that by considering an inverted-loss medium in the backward stage [24], the attenuation effect can be compensated.

V. DISCUSSION

The preceding results have validated the wave propagation property of the closed TR cavity realized by the Y-shaped cable network. The observation refers to the locations that are out of the interfering region. The discussion in this subsection focuses on the locations neighboring the original source location $x_1 = x_s$.

A. Interfering Effect of Diverging Voltage Waves

Given the previous analysis, the interfering region for the proposed TR cavity is bounded at $x_1 = x_s \pm 12$ m. Figs. 10(a) and (b) depict the voltage waves measured at the locations $x_1 = x_s \pm \Delta x$ with Δx being 1, 2 and 5 m, respectively. As formulated previously, if the observation point is within the interfering region, the backward-stage voltage wave is not any more a time-reversed copy of its counterpart in the forward stage.

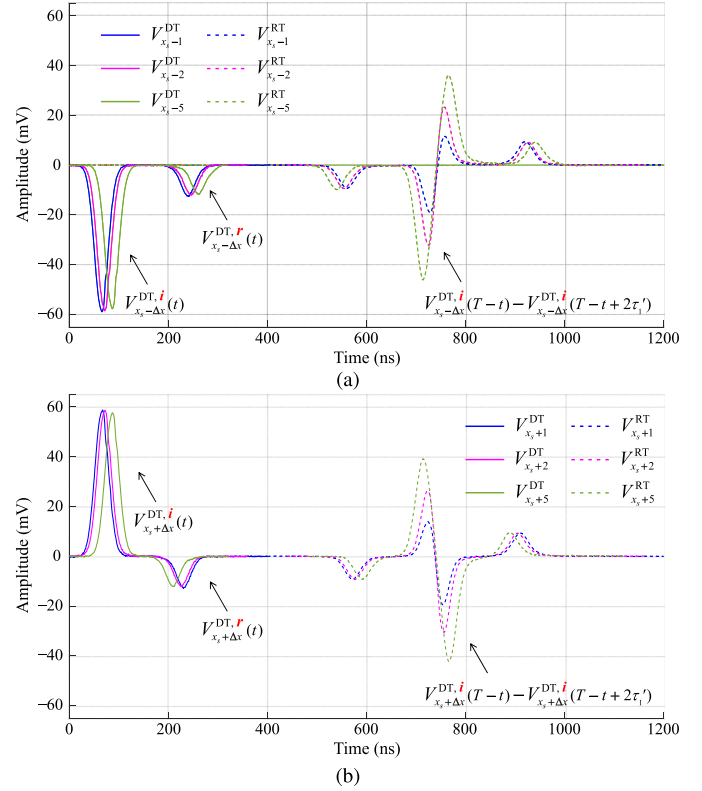


Fig. 10. Experimentally recorded voltage waveforms at the points neighboring the source location $x_1 = x_s$. Solid lines: voltages in the forward stage. Dashed lines: voltages in the backward stage. The observation points are on (a) side $x_1 < x_s$ and (b) side $x_1 > x_s$.

The forward-stage voltage wave can be decomposed into two terms (see the waveforms of solid lines in Fig. 10): 1) the incident voltage wave generated by the source denoted by the superscript “*i*” and 2) the reflected voltage wave from the junction point denoted by the superscript “*r*.” The incident voltage wave has the same shape as the series excitation source $V_s(t)$ but with an amplitude reduced by a factor 2 due to the division of the excitation voltage. As can be seen in Figs. 10(a) and 10(b), the incident voltage wave has either a positive or negative polarity depending on whether the observation point is located on the right side (i.e., $x_1 > x_s$) or on the left side (i.e., $x_1 < x_s$) of the series voltage source.

In the backward-propagation stage, the interfering effect results from the time-reversed incident waves $V_{x_s \pm \Delta x}^{DT,i}(T-t)$, namely the converging waves, overlapping with their respective inverted and time-shifted copies (i.e., the diverging waves). It is also demonstrated by the results that only the incident component that is originally generated by the source itself is distorted by the diverging voltage wave in the backward stage.

It is worth noting that in spite of the overlap between the converging and diverging voltage waves, it is still possible to locate the position of the source. Thanks to the TR temporal-spatial correlation property, $V_{x_s}^{DT,i}(T-t)$ and its inverted copy inherently arrive in phase at the source location $x_1 = x_s$, resulting in a complete offset. This way, the original source point can be exclusively distinguished from its neighboring locations, for example, by means of an algorithm assessing the energy of the voltage wave along the network.

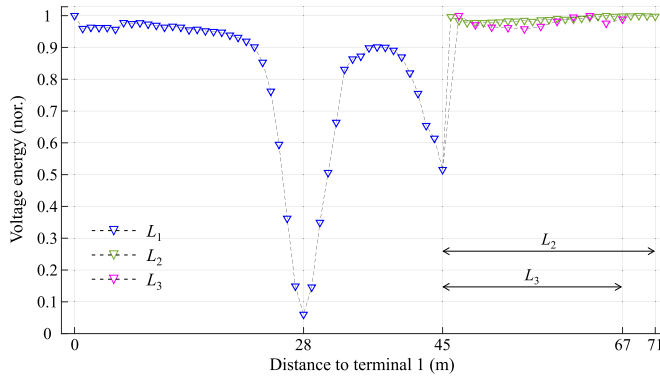


Fig. 11. Normalized energy of the voltage experimentally recorded along the network. The spacings of the observation points are, respectively, 1 m along Line branches 1 and 2, and 2 m along Line branch 3. The normalization is based on the maximal voltage energies calculated for the respective line branches.

Fig. 11 shows the normalized voltage energy as a function of the distance to the network terminal $x_1 = 0$. Obviously, the source location ($x_1 = 28$ m) is characterized by the global minimum voltage energy among the observation points distributed along the network.

B. Closed Time-Reversal Cavity in Transmission Line Networks With a Time-Reversal Sink

Rosny and Fink have proposed in acoustics the concept of a *TR sink* to overcome the interfering effect caused by the diverging waves in the region near the source location [25]. According to this concept, during the backward-propagation stage of the TR process, the source is replaced by a sink that absorbs the incident wave.

Both active and passive realizations of a TR sink are possible. For the case of a single transmission line, a passive TR sink can be straightforwardly designed as a simple two-port passive circuit at the source location. However, when it comes to a topologically complex transmission line network (characterized by multiple junctions and terminals), the realization of a passive sink would be quite challenging and it would require dedicated time-varied switch operations.

However, if the source excitation is known, the sink can be experimentally realized by an active source that generates an additive inverse of the diverging wave in the backward stage, compensating therefore the interfering effect caused by the diverging process.

Assume that the original source remains active in the backward-propagation stage but with a time-reversed waveform, namely $V_S(T - t)$ for the proposed case of the TR cavity in transmission line networks. Mathematically, solving the wave equation taking into account the active TR sink in the backward stage, it can readily be shown that the voltage wave generated by the time-reversed source is identical to the diverging term in (17) but with opposite polarity.

Fig. 12 compares the distorted voltage wave experimentally recorded at the location $x_1 = x_s - 1$ as an example with the one measured in presence of the active source $V_S(T - t)$ representing a TR sink. As can be observed, even the voltage wave is recorded at a location quite adjacent to the source

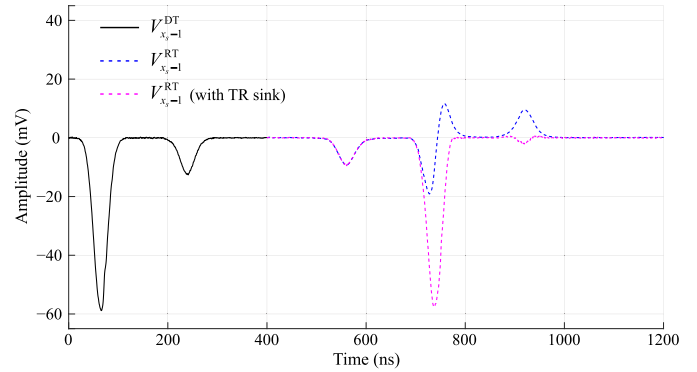


Fig. 12. Experimentally recorded voltage waveforms at the location $x_1 = x_s - 1$ in the forward-propagation stage (i.e., with the black solid line) and the backward-propagation stage (with and without a TR sink).

point, its waveform in the backward-propagation stage is nearly a time-reversed copy of the voltage wave in the forward-propagation stage, as the diverging voltage wave has been compensated.

Thus, the so-called time reversal sink applies the additional source generated wave to interfere destructively with the backward-stage diverging wave, keeping intact the converging component.

VI. CONCLUSION

We demonstrated that a closed time reversal cavity can be realized using a transmission line network. Such a time reversal cavity requires a finite number of observation points located at the terminals of the network. A time-reversed copy of the system state (e.g., voltage wave distributions) originated by a source in the forward-propagation stage can be obtained by time-reversing the response at the terminals and back injecting them into the network.

In the experimental realization of the time reversal cavity, the resulting distribution was affected by an attenuation resulting from losses in the coaxial cables. Indeed, the wave equations in transmission lines are time reversal invariant for lossless lines. When the network is lossy, the time reversal invariance will hold when an inverted-loss medium is considered in the back-propagation model [24]. An inverted-loss medium can be considered in a straightforward way in numerical simulations as long as the line losses are well characterized.

We showed in this study that the past behavior of signals along a transmission line network can be reproduced in the future. To achieve this, only a finite number of responses need to be monitored at the network terminals. We also discussed the interfering effect of the so-called diverging wave for observation points in the vicinity of the source. We proposed an active realization of a time reversal sink, using the time-reversed source generated wave to interfere destructively with the backward-stage diverging wave.

The proposed closed time reversal cavity in transmission lines can find useful applications, for instance in online monitoring of communication networks, which work generally under matched conditions. Such networks can also include point-to-point wireless communication systems, which can

be represented by their equivalent models in the backward stage. The synchronized measurement of signals at each network terminal would allow detecting anomalies and locating their source. The technique can also be used in various other applications such as: 1) preventive maintenance and monitoring of cables to detect and locate incipient faults, before their occurrence; 2) detecting and locating intentional electromagnetic interference (IEMI) attacks; and 3) facilitating the investigation of incidents in flight data recorders.

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