

## Op Amp Circuits

### Measurement of Offset Voltage, Bias Currents, and Open-loop Gain

#### Input offset voltage

In an ideal op amp, we assume that the  $V_o$  versus  $V_i$  curve goes through  $(0,0)$ , i.e., for an input voltage of  $V_i = 0$  V, the output voltage  $V_o$  is also 0 V, as shown in Fig. 1 (a). This condition is valid if the transistors in the op amp (see Fig. 2) such as  $Q_1$  and  $Q_2$  which are supposed to be identical are indeed identical in all respects. In reality, there are always some small differences between them, e.g., their  $\beta$  values could be slightly different. As a result of this mismatch, the  $V_o$  versus  $V_i$  relationship of a real op amp exhibits a shift along the  $V_i$  axis, as shown in Fig. 1 (b).

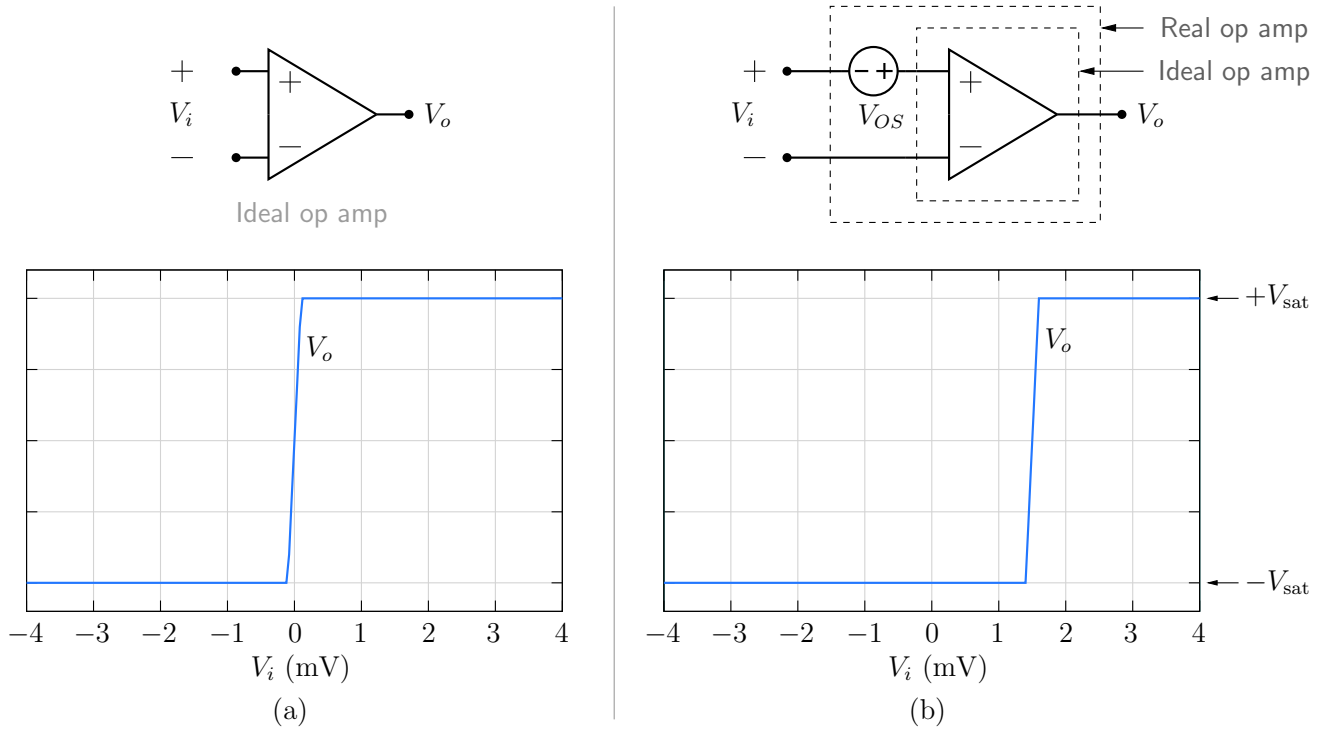


Figure 1:  $V_o$  versus  $V_i$  relationship for (a) ideal op amp, (b) op amp with an input offset voltage  $V_{OS} = -1.5$  mV.

The effect of the offset voltage can be incorporated with a voltage source  $V_{OS}$  (called the input offset voltage), as shown in Fig. 1 (b). In other words, if we apply  $V_i = V_+ - V_- = -V_{OS}$ , we get an output voltage  $V_o = 0$  V. For Op Amp 741, the offset voltage is typically in the range  $-5$  mV to  $+5$  mV.

#### Input bias currents

The transistors of the input stage ( $Q_1$  and  $Q_2$  in Fig. 2) of Op Amp 741 draw small but non-zero base currents  $I_B^+$  and  $I_B^-$ . Since  $Q_1$  and  $Q_2$  may not be perfectly matched,  $I_B^+$  and  $I_B^-$

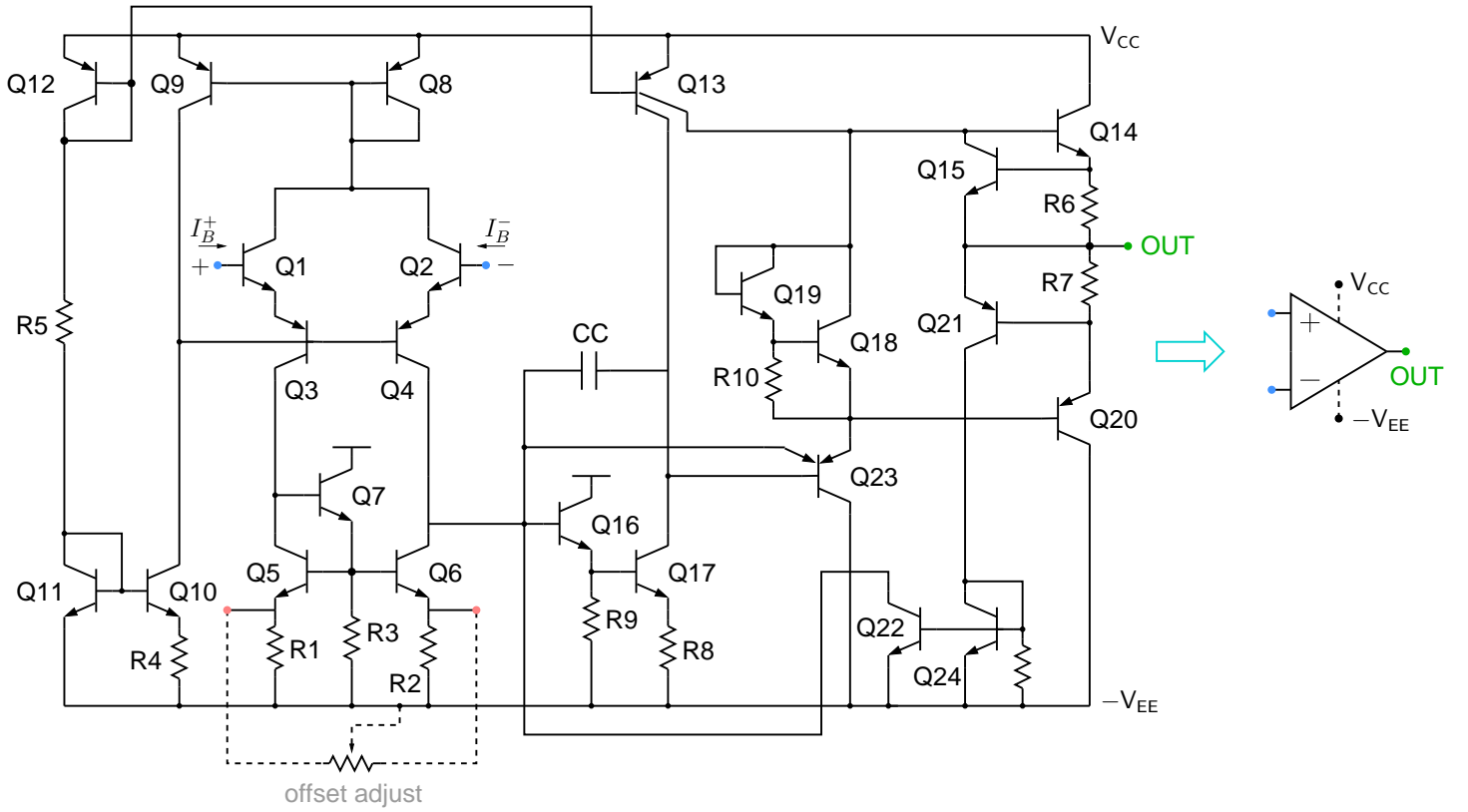


Figure 2: Internal circuit of Op Amp 741.

would be generally different. The average of the two currents is called the input bias current  $I_B$ , and the difference between the two is called the input offset current  $I_{OS}$ , i.e.,

$$I_B = \frac{I_B^+ + I_B^-}{2}, \quad I_{OS} = |I_B^+ - I_B^-|. \quad (1)$$

For Op Amp 741,  $I_B$  is typically 100 nA, and  $I_{OS}$  is 10 nA at 25 °C.

The effect of the bias currents can be represented by the equivalent circuit shown in Fig. 3 (a), and the overall op amp model showing bias currents as well as offset voltage is shown in Fig. 3 (b).

### Measurement of offset voltage and bias currents [1]

When an op amp is used in a circuit, the bias currents  $I_B^+$  and  $I_B^-$  as well as the input offset voltage  $V_{OS}$  would generally affect the output voltage. In order to measure these quantities, we require circuits which enhance the contributions of one of these parameters while keeping the other two contributions small.

Fig. 4 (a) shows a circuit which can be used for measurement of  $V_{OS}$ . Fig. 4 (b) shows the same circuit re-drawn using the op amp equivalent circuit of Fig. 3 (b) which accounts for the op-amp non-idealities, viz.,  $V_{OS}$ ,  $I_B^+$ , and  $I_B^-$ . Using superposition, we can show that

$$V_o = V_{OS} \left( 1 + \frac{R_2}{R_1} \right) + R_2 I_B^-. \quad (2)$$

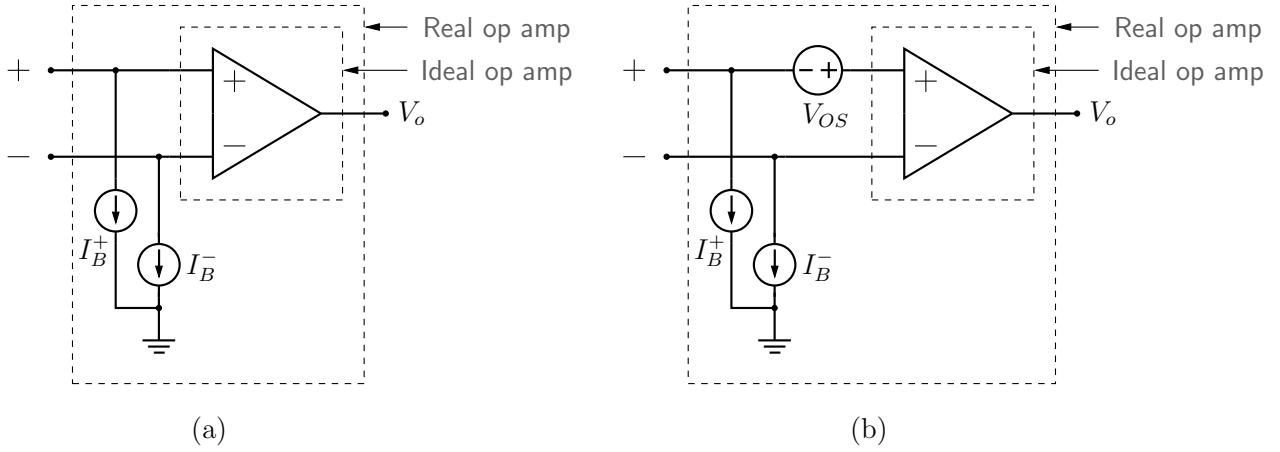


Figure 3: (a) Representation of bias currents of an op amp, (b) representation of bias currents and offset voltage of an op amp.

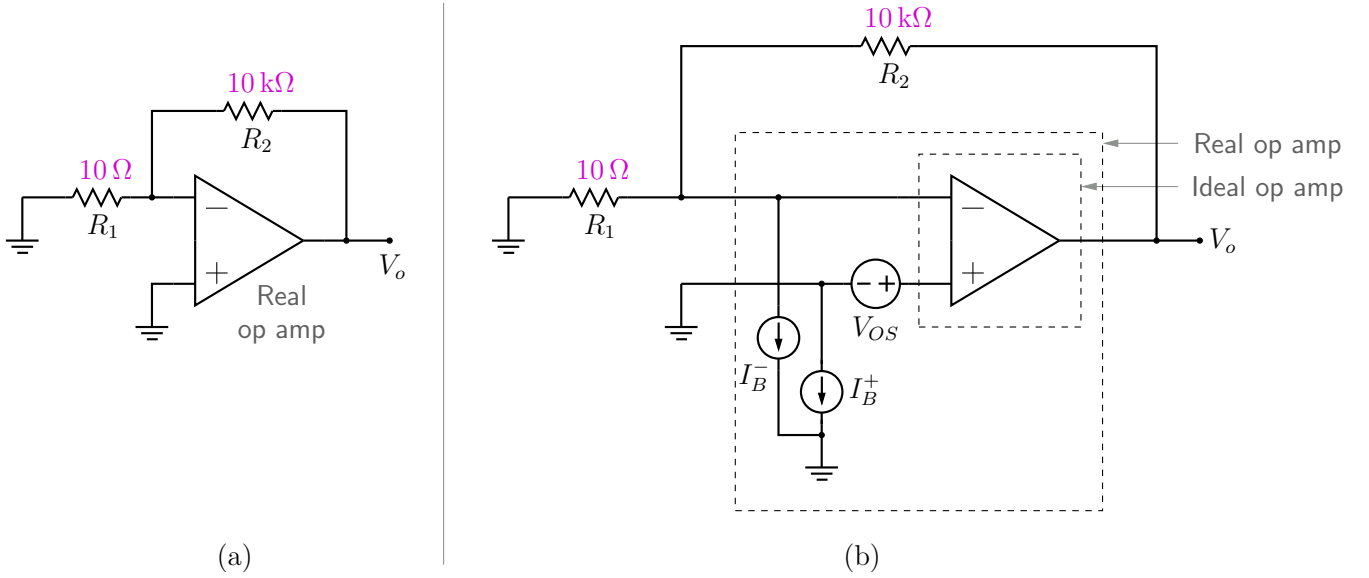


Figure 4: (a) Circuit for measurement of  $V_{OS}$ , (b) equivalent circuit.

For  $V_{OS} \approx 5\ \text{mV}$  and  $I_B^- \approx 100\ \text{nA}$ , the contributions from the two terms for  $R_1 = 10\ \Omega$  and  $R_2 = 10\ \text{k}\Omega$  are about  $5\ \text{V}$  and  $1\ \text{mV}$ , respectively. Clearly,  $I_B^-$  has a negligible effect on the output voltage, and we can write

$$V_{OS} = \frac{V_o}{1 + R_2/R_1} \approx \frac{V_o}{R_2/R_1}. \quad (3)$$

A circuit for measurement of the bias current  $I_B^-$  is shown in Fig. 5 (a), and the corresponding equivalent circuit is shown in Fig. 5 (b). Since the op amp in Fig. 5 (b) is ideal, we have  $V_- = V_+ = V_{OS}$ , and the output voltage is

$$V_o = V_- + I_B^- R = V_{OS} + I_B^- R. \quad (4)$$

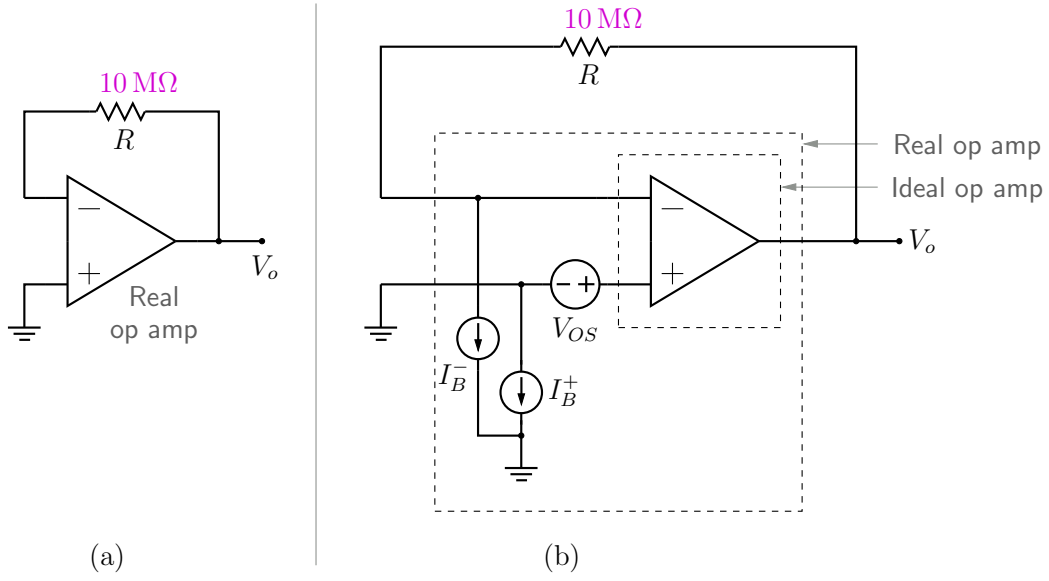


Figure 5: (a) Circuit for measurement of  $I_B^-$ , (b) equivalent circuit.

As an example, let  $V_{OS} = 5\text{ mV}$  and  $I_B^- = 100\text{ nA}$ . With  $R = 10\text{ M}\Omega$ , the second term is  $1\text{ V}$  which is much larger than  $V_{OS}$ , and therefore we get

$$I_B^- = V_o/R. \quad (5)$$

The circuit shown in Fig. 6 (a), with the corresponding equivalent circuit shown in Fig. 6 (b), can be used for measurement of  $I_B^+$ . Since the input current for the ideal op amp of Fig. 6 (b)

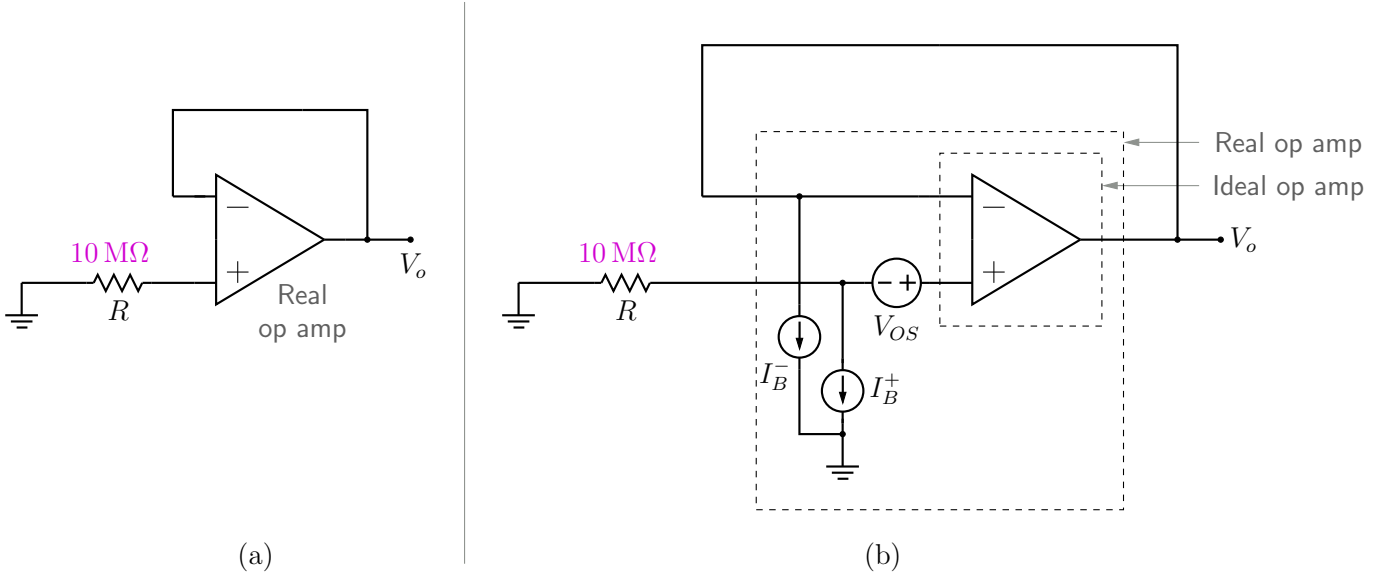


Figure 6: (a) Circuit for measurement of  $I_B^+$ , (b) equivalent circuit.

is zero, the current  $I_B^+$  must go through  $R$ , causing  $V_+ = I_B^+ R + V_{OS}$ , and

$$V_o = V_- = V_+ = I_B^+ R + V_{OS}. \quad (6)$$

For typical values of  $I_B^+$  and  $V_{OS}$ , with  $R = 10\text{ M}\Omega$ , the first term dominates, giving

$$I_B^+ = V_o/R. \quad (7)$$

### Measurement of DC open-loop gain

One of the most important features of an op amp is a high open-loop gain  $A_{OL}$  which is typically in the range  $10^5$  to  $10^6$ . Measurement of  $A_{OL}$  with a simple scheme shown in Fig. 7 does not work for the following reasons:

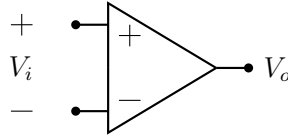


Figure 7: An op amp operated in the open-loop configuration.

- (a) With a large gain of  $10^5$  or more, the op amp is likely to be driven to saturation on account of the input offset voltage  $V_{OS}$  which is typically in the range  $-5\text{ mV}$  to  $+5\text{ mV}$  for Op Amp 741.
- (b) Even if we had a magical op amp with  $V_{OS} = 0\text{ V}$  (or we compensated for the effect of  $V_{OS}$  by some means), measurement of  $A_{OL}$  is still a challenge. Suppose  $A_{OL} = 2 \times 10^5$ , and we want an output voltage of  $1\text{ V}$ , for example. This would require  $V_i = 1\text{ V} / 2 \times 10^5 = 5\text{ }\mu\text{V}$ , a very small voltage to apply or measure in the lab.

Given the above difficulties, how to we reliably measure  $V_{OL}$ ? The trick is to use the op amp in a “servo loop” which ensures that its input voltage remains small enough to keep it in the linear region. Fig. 8 shows the circuit diagram [2]. The op amp for which we want to measure  $A_{OL}$

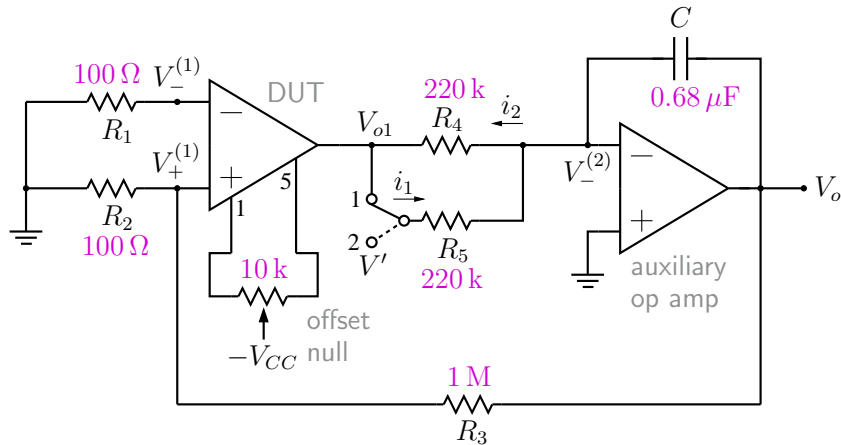


Figure 8: Measurement of DC open-loop gain  $A_{OL}$ .

is marked in the figure as the Device Under Test (DUT). The circuit has a high overall gain,

but because of the negative feedback provided by  $R_3$ , it is stable. The capacitor  $C$  prevents the circuit from oscillating. We can measure the open-loop gain  $A_{OL}$  of the DUT using the following steps.

- (a) Using the 10k pot, we first nullify the effect of the offset voltage of the DUT to the extent possible, i.e., we adjust the pot, with the switch in position 1 (or simply open), to make  $V_o$  as small as possible. Let us use  $V_o^A$  and  $V_{o1}^A$  to denote the values of  $V_o$  and  $V_{o1}$ , respectively, in this situation. Because of the large gain of the auxiliary op amp, we can say that  $V_{o1}^A = 0$  V.
- (b) We now change the switch to position 2. With  $V_-^{(2)} \approx V_+^{(2)} = 0$  V and with the capacitor behaving like an open circuit in the DC condition, we have  $i_1 = i_2$ , and

$$V_{o1} = V_-^{(2)} - i_2 R_4 = 0 - \frac{V'}{R_5} R_4 = -V'. \quad (8)$$

In this situation, let  $V_o$  be denoted by  $V_o^B$  and  $V_{o1}$  by  $V_{o1}^B$ . We can attribute the difference  $(V_o^B - V_o^A)$  to the change in  $V_{o1}$ , i.e.,  $\Delta V_{o1} = V_{o1}^B - V_{o1}^A = -V' - 0 = -V'$ .

For the DUT, its output  $V_{o1}$  has undergone a change of  $-V'$ , and it is a result of a change in  $(V_+^{(1)} - V_-^{(1)})$  which is equal to  $\frac{R_2}{R_2 + R_3} \times (V_o^B - V_o^A)$ . In other words,

$$\frac{R_2}{R_2 + R_3} (V_o^B - V_o^A) \times A_{OL} = -V', \quad (9)$$

which can be used to obtain  $A_{OL}$  for the DUT.

## References

1. Texas Instruments, "Understanding Op Amp parameters," <http://www.ti.com/lit/ml/sloa083/sloa083.pdf>
2. James Bryant, "Simple Op Amp measurement," [http://www.analog.com/library/analogDialogue/archives/45-04/op\\_amp\\_measurements.html](http://www.analog.com/library/analogDialogue/archives/45-04/op_amp_measurements.html)