

Logic Synthesis

2 Level Exact Synthesis

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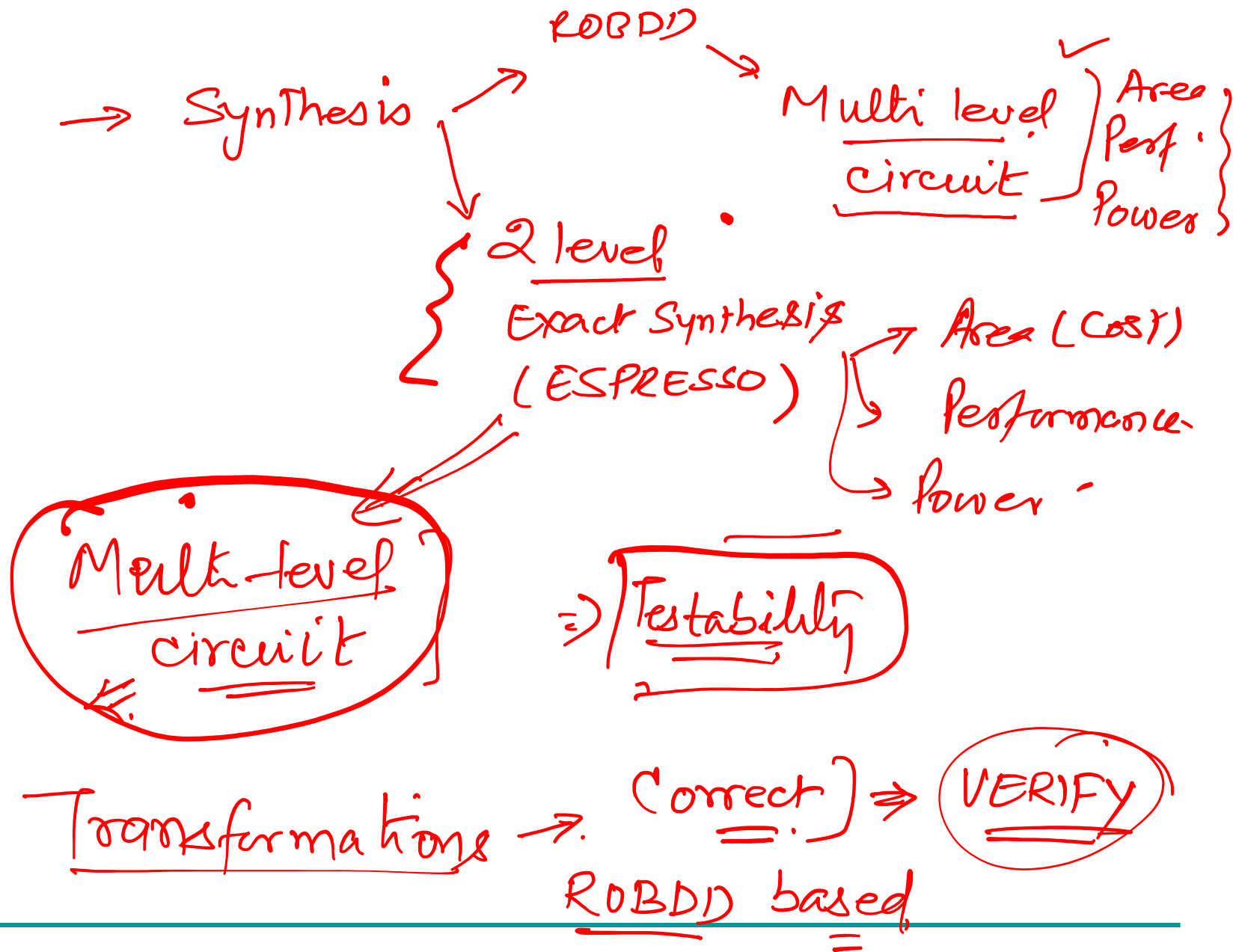


EE-677: Foundations of VLSI CAD



Lecture 21 on 28 Sep 2021

CADSL



SAT based
Satisfiability

$$\underbrace{(a+b)}_{C_1} \underbrace{(b+\bar{a}+c)}_{C_2} \underbrace{(a+c+d)}_{C_3} = 1$$

SAT { Under what assignments to variables (literals)
a, b, c, d. the expression evaluates to true }

$$\{ a=1 \quad b=1 \quad c=1 \quad d=1 \}$$

$$\underline{C_1 \cdot C_2 \cdot C_3} = 1 \Rightarrow$$

$$\left. \begin{array}{l} C_1=1 \\ C_2=1 \\ C_3=1 \end{array} \right\}$$

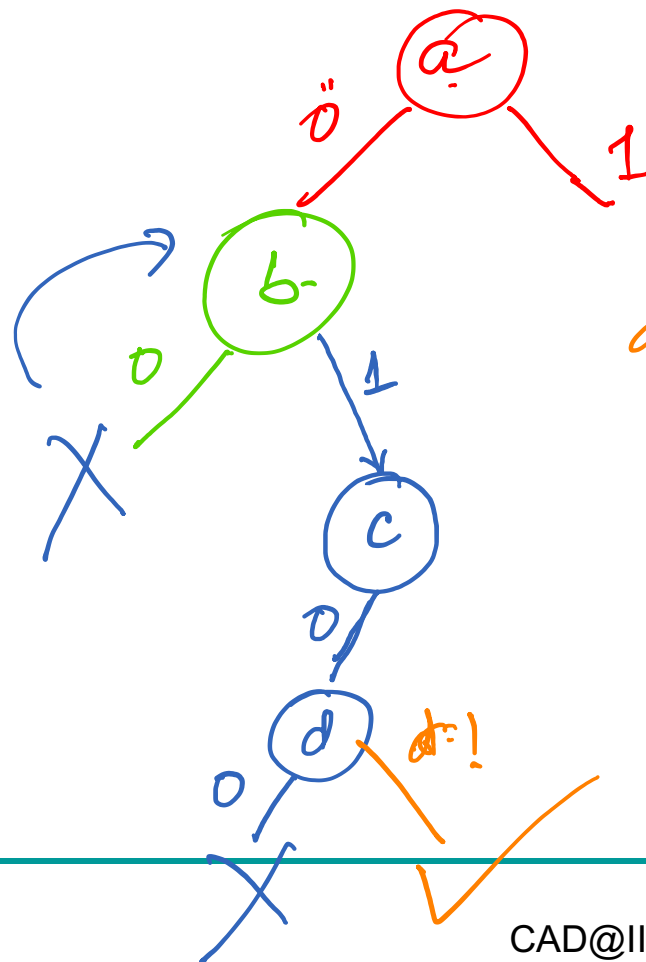
$$C_1=1, C_2=0, C_3=1$$



How to find the assignments?

$(a+b)$ ✓
 $(\bar{a}+b+c)$ ✓
 $(a+c+d)$ ✓
 $(a < b < c < d)$ ✓
Decision Tree

$c_1 = 0$



$a=0$
 $b=1$
 $c=0$
 $d=1$

1960.

DPLL

$b=1$ c_2 ✓
 c_1 ✓
 c_3

$c \geq 1$ c_3 ✓
 c_1 ✓
 c_3

$d=0$ c_2 ✓
 c_1 ✓
 c_3 X

$d=1$ c_2 ✓
 c_1 ✓
 c_3 ✓



Fast ✓

Unit clause rule;

$$\frac{a(b+c) \cdot (d+e) (a+b)}{a(b+c) \cdot (d+e) (a+b)} \downarrow \begin{matrix} \uparrow b=0 \\ \downarrow \end{matrix} \begin{matrix} \rightarrow [c] \\ (b) \end{matrix}$$

Boolean Constraint
Propagation

BCP

x0 (a)

a=1

Stall Marks
method

Recursive
Learning!

Learning

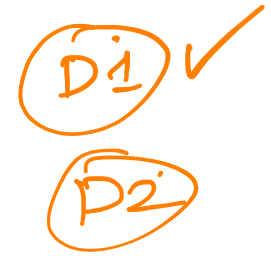
Consensus theorem

$$(a+b)(b+c)(a+c) \equiv (a+b)(b+c)(a+c)$$

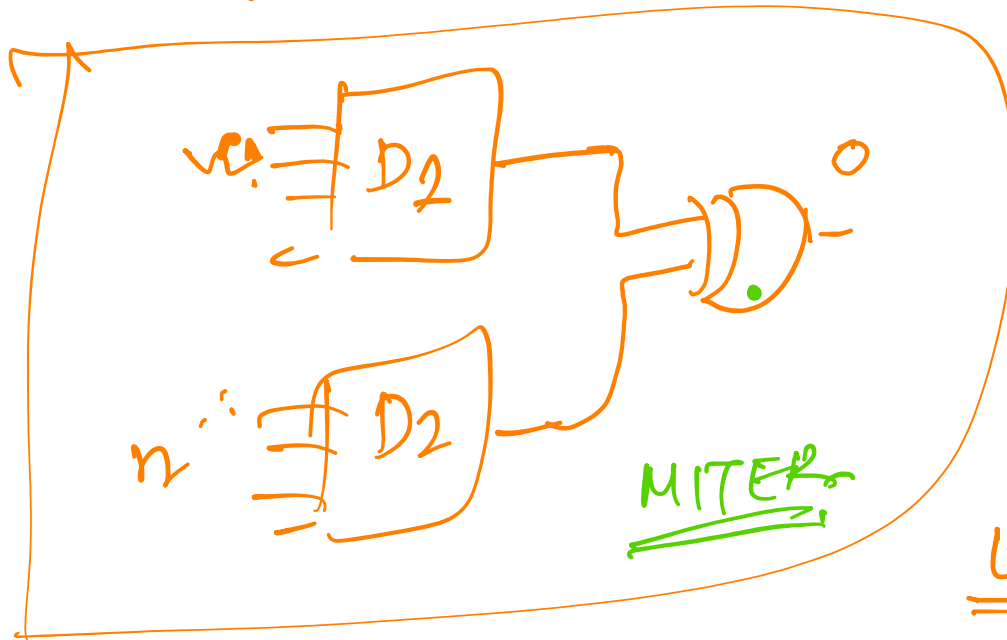
Millions - clauses



VERIFICATION.



$$D1 \equiv D2$$



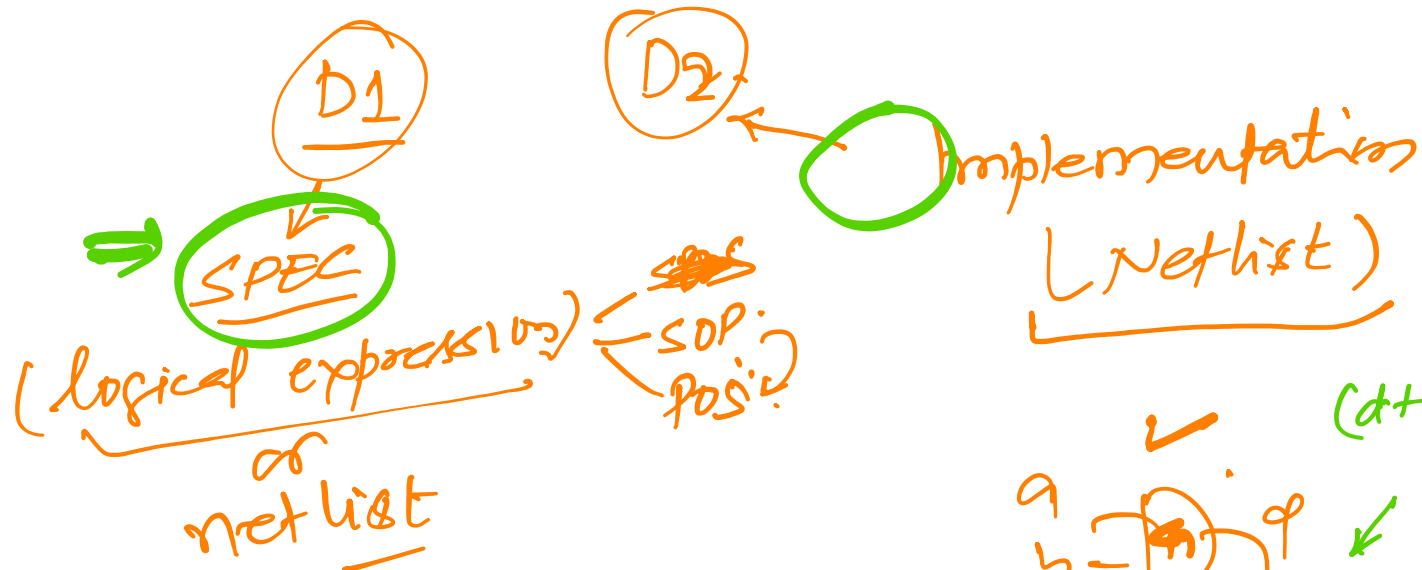
SAT expression

Should never
satisfy
if $D1 \equiv D2$

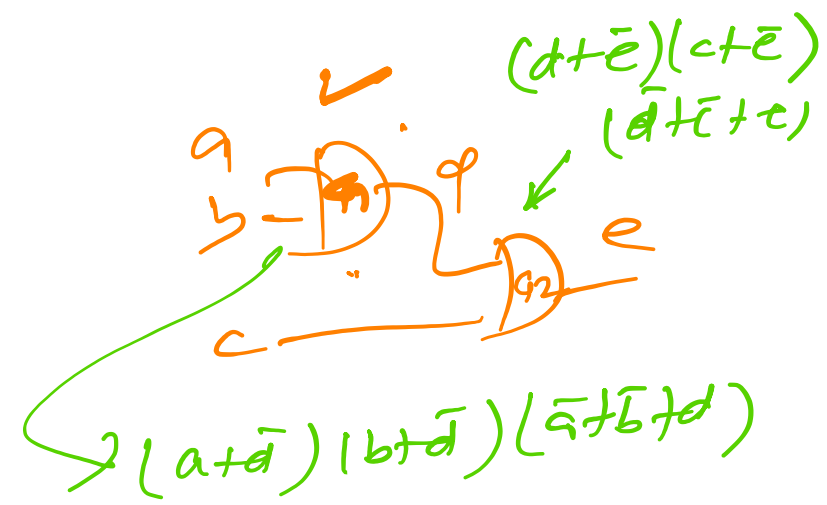
UNSAT problem

if any assignment exists $\Rightarrow D1 \neq D2$

a=1 b=2 c=3 d=4 ← Counter Example.



0	0	0	$a=0 \rightarrow d=0$
0	1	0	$b=0 \rightarrow d=0$
1	0	0	$a=1 \wedge b=1 \rightarrow d=1$
1	1	1	



AND

$$\bar{a} \rightarrow \bar{d} \Rightarrow (\bar{a} + \bar{d}) \Rightarrow (a + \bar{d})$$

$$\bar{b} \rightarrow \bar{d} \Rightarrow (b + \bar{d})$$

$$(a \cdot b \rightarrow d) \Rightarrow (\bar{a} \cdot \bar{b} + d) \Rightarrow (\bar{a} + \bar{b} + d)$$



{ Equivalence checking.
SAT. }

Thank You

