



RESTORING DIVISION

- 1) Let Q register hold the divided, M register holds the divisor and A register is 0.
- 2) On completion of the algorithm, Q will get the quotient and A will get the remainder.

Algorithm:

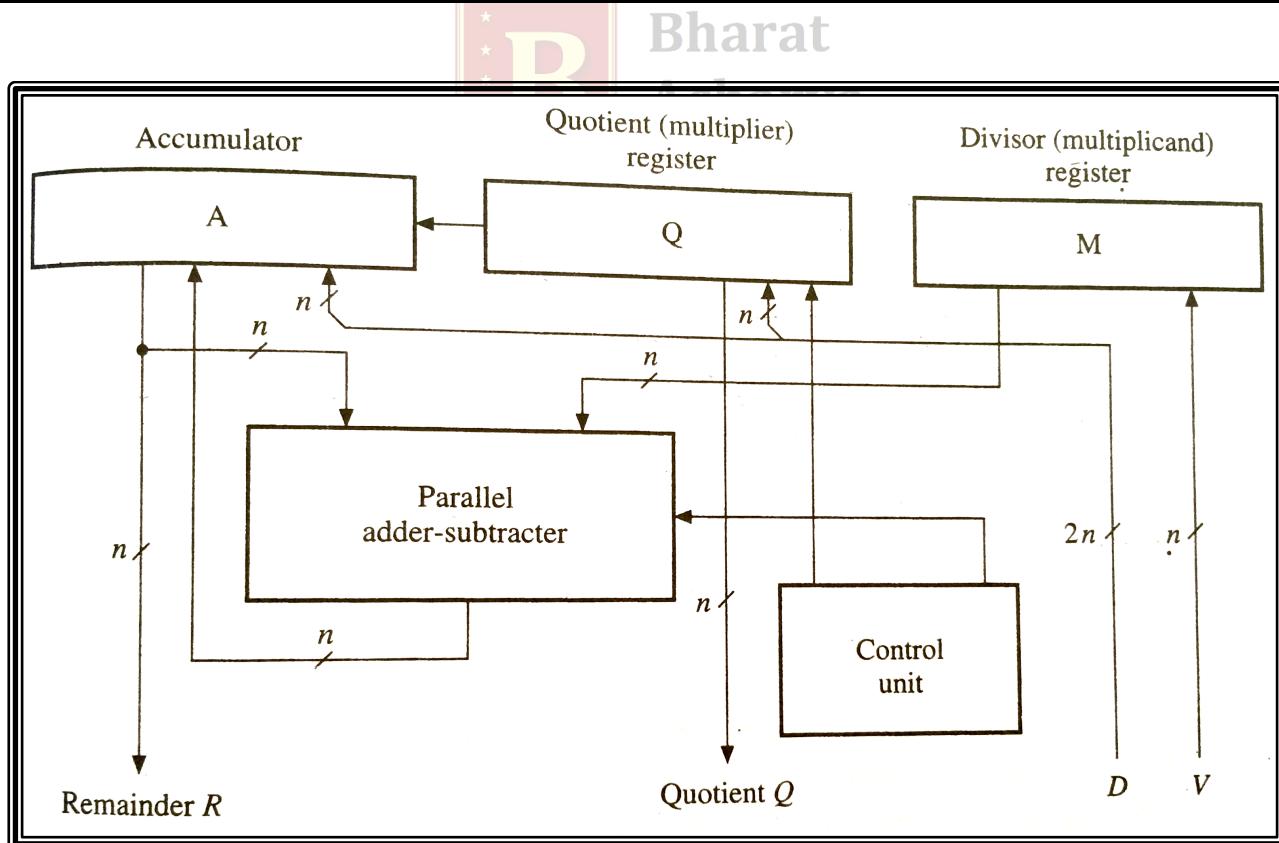
The **number of steps** required is equal to the **number of bits in the Dividend**.

- 1) At each step, **left shift the dividend by 1 position**.
- 2) **Subtract the divisor from A** (perform $A - M$).
- 3) If the **result is positive** then the step is said to be "**Successful**".
In this case **quotient bit will be "1"** and **Restoration is NOT Required**.
- 4) If the **result is negative** then the step is said to be "**Unsuccessful**".
In this case **quotient bit will be "0"**.

Here Restoration is performed by adding back the divisor.

Hence the method is called Restoring Division.

Repeat steps 1 to 4 for **all bits** of the Dividend.





Example: (6) / (4)

Dividend (Q) = 6

Divisor (M) = 4

Accumulator (A) = 0

$$\begin{array}{r} 6 = 0110 \\ -6 = 1010 \end{array} \quad \begin{array}{r} 4 = 0100 \\ -4 = 1100 \end{array}$$

In case of doubts, Call #BharatSir @ 98204 08217	ACCUMULATOR	DIVIDEND	DIVISOR
	A (0)	Q (6)	M (4)
Initial Values	0 0 0 0	0 1 1 0	0 1 0 0
Step 1:			
Left-Shift	0 0 0 0	1 1 0 _	
A - M	+ 1 1 0 0		
Unsuccessful (-ve)	1 1 0 0		
Restoration	0 0 0 0	1 1 0 0	
Step 2:			
Left-Shift	0 0 0 1	1 0 0 _	
A - M	+ 1 1 0 0		
Unsuccessful (-ve)	1 1 0 1	Education ★★★★☆	
Restoration	0 0 0 1	1 0 0 0	
Step 3:			
Left-Shift	0 0 1 1	0 0 0 _	
A - M	+ 1 1 0 0		
Unsuccessful (-ve)	1 1 1 1		
Restoration	0 0 1 1	0 0 0 0	
Step 4:			
Left-Shift	0 1 1 0	0 0 0 _	
A - M	+ 1 1 0 0		
Successful (+ve)	0 0 1 0		
No Restoration	0 0 0 0	0 0 0 1	
	Remainder (0)	Quotient (1)	



Example: (19) / (7)

Dividend (Q) = 19 Divisor (M) = 7 Accumulator (A) = 0

$$\begin{array}{ll} 19 = 010011 & 7 = 000111 \\ -19 = 101101 & -7 = 111001 \end{array}$$

In case of doubts, Call #BharatSir @ 98204 08217	ACCUMULATOR	DIVIDEND	DIVISOR
	A (0)	Q (19)	M (7)
Initial Values	000000	010011	000111
Step 1:			
Left-Shift	000000	10011_	
A - M	+111001		
Unsuccessful (-ve)	111001		
Restoration	000000	100110	
Step 2:			
Left-Shift	000001	00110_	
A - M	+111001		
Unsuccessful (-ve)	111010		
Restoration	000001	001100	
Step 3:			
Left-Shift	000010	01100_	
A - M	+111001		
Unsuccessful (-ve)	111011		
Restoration	000010	011000	
Step 4:			
Left-Shift	000100	11000_	
A - M	+111001		
Unsuccessful (-ve)	111101		
Restoration	000100	110000	
Step 5:			
Left-Shift	001001	10000_	
A - M	+111001		
Successful (+ve)	000010		
No Restoration	000010	100001	
Step 6:			
Left-Shift	000101	00001_	
A - M	+111001		
Unsuccessful (-ve)	111110		
Restoration	000101	000010	
	Remainder (5)	Quotient (2)	



Example: (23) / (3)

Dividend (Q) = 23 Divisor (M) = 3 Accumulator (A) = 0

$$\begin{array}{r} 23 = 010111 \\ -23 = 101001 \end{array} \quad \begin{array}{r} 3 = 000011 \\ -3 = 111101 \end{array}$$

In case of doubts, Call #BharatSir @ 98204 08217	ACCUMULATOR	DIVIDEND	DIVISOR
	A (0)	Q (23)	M (3)
Initial Values	0 0 0 0 0 0	0 1 0 1 1 1	0 0 0 0 1 1
Step 1:			
Step 2:			
Step 3:			
Step 4:			
Step 5:			
Step 6:			
	Remainder (2)	Quotient (7)	



NON-RESTORING DIVISION

- 1) Let Q register hold the divided, M register holds the divisor and A register is 0.
- 2) On completion of the algorithm, Q will get the quotient and A will get the remainder.

Algorithm:

The **number of steps** required is equal to the **number of bits in the Dividend**.

- 1) At each step, **left shift the dividend by 1 position**.
 - 2) **Subtract the divisor from A** (perform $A - M$).
 - 3) If the **result is positive** then the step is said to be "**Successful**".
In this case **quotient bit will be "1"** and **Restoration is NOT Required**.
The **Next Step** will also be **Subtraction**.
 - 4) If the **result is negative** then the step is said to be "**Unsuccessful**".
In this case **quotient bit will be "0"**.
Here Restoration is NOT Performed.
Instead the next step will be ADDITION in place of subtraction.
- As restoration is not performed, the method is called Non-Restoring Division.

Repeat steps 1 to 4 for **all bits** of the Dividend.

*Note: Restoration may only be performed in the FINAL step, if it is unsuccessful, as there is no next step thereafter.
In such a case, restoration is performed by adding back the divisor.*



Example: (7) / (5)

Dividend (Q) = 7

Divisor (M) = 5

Accumulator (A) = 0

$$\begin{array}{r} 7 = 0111 \\ -7 = 1001 \end{array} \quad \begin{array}{r} 5 = 0101 \\ -5 = 1011 \end{array}$$

In case of doubts, Call #BharatSir @ 98204 08217	ACCUMULATOR		DIVIDEND	DIVISOR
	A (0)	Q (7)	M (5)	
Initial Values	0 0 0 0	0 1 1 1	0 1 0 1	
Step 1:				
Left-Shift	0 0 0 0	1 1 1 _		
A - M	+ 1 0 1 1			
Unsuccessful (-ve)	1 0 1 1	1 1 1 0		
Next Step: "Add"	*			
Step 2:				
Left-Shift	* 0 1 1 1	1 1 0 _		
A + M	+ 0 1 0 1			
Unsuccessful (-ve)	* 1 1 0 0	1 1 0 0		
Next Step: "Add"				
Step 3:				
Left-Shift	1 0 0 1	1 0 0 _		
A + M	+ 0 1 0 1			
Unsuccessful (-ve)	1 1 1 0	1 0 0 0		
Next Step: "Add"				
Step 4:				
Left-Shift	1 1 0 1	0 0 0 _		
A + M	+ 0 1 0 1			
Successful (+ve)	0 0 1 0	0 0 0 1		
	Remainder (2)	Quotient (1)		



Example: (7) / (3)

Dividend (Q) = 7

Divisor (M) = 3

Accumulator (A) = 0

$$\begin{array}{r} 7 = 0111 \\ -7 = 1001 \end{array} \quad \begin{array}{r} 3 = 0011 \\ -3 = 1101 \end{array}$$

In case of doubts, Call #BharatSir @ 98204 08217	ACCUMULATOR		DIVIDEND	DIVISOR
	A (0)	Q (7)	M (3)	
Initial Values	0 0 0 0	0 1 1 1	0 0 1 1	
Step 1:				
Left-Shift	0 0 0 0	1 1 1 _		
A - M	+ 1 1 0 1			
Unsuccessful (-ve)	1 1 0 1	1 1 1 0		
Next Step: "Add"	*			
Step 2:				
Left-Shift	1 0 1 1	1 1 0 _		
A + M	+ 0 0 1 1			
Unsuccessful (-ve)	1 1 1 0	1 1 0 0		
Next Step: "Add"				
Step 3:				
Left-Shift	1 1 0 1	1 0 0 _		
A + M	+ 0 0 1 1			
Successful (+ve)	0 0 0 0	1 0 0 1		
Next Step: "Sub"				
Step 4:				
Left-Shift	0 0 0 1	0 0 1 _		
A - M	+ 1 1 0 1			
Unsuccessful (-ve)	1 1 1 0			
Restore: (Add back divisor)	0 0 0 1	0 0 1 0		
	Remainder (1)	Quotient (2)		



Example: (19) / (4)

Dividend (Q) = 19 Divisor (M) = 4 Accumulator (A) = 0

$$\begin{array}{r} 19 = 010011 \\ -19 = 101101 \end{array} \quad \begin{array}{r} 4 = 000100 \\ -4 = 111100 \end{array}$$

In case of doubts, Call #BharatSir @ 98204 08217	ACCUMULATOR	DIVIDEND	DIVISOR
	A (0)	Q (19)	M (4)
Initial Values	000000	010011	000100
Step 1:			
Left-Shift	000000	10011_	
A - M	+111100		
Unsuccessful (-ve)	111100	100110	
Next Step: "Add"			
Step 2:			
Left-Shift	111001	00110_	
A + M	+000100		
Unsuccessful (-ve)	111101	001100	
Next Step: "Add"			
Step 3:			
Left-Shift	111010	01100_	
A + M	+000100		
Unsuccessful (-ve)	111110	011000	
Next Step: "Add"			
Step 4:			
Left-Shift	111100	11000_	
A + M	+000100		
Successful (+ve)	000000	110001	
Next Step: "Sub"			
Step 5:			
Left-Shift	000001	10001_	
A - M	+111100		
Unsuccessful (-ve)	111101	100010	
Next Step: "Add"			
Step 6:			
Left-Shift	111011	00010_	
A + M	+000100		
Unsuccessful (-ve)	111111		
Restore: (Add back divisor)	000011	000100	
	Remainder (3)	Quotient (4)	



Example: (23) / (3)

Dividend (Q) = 23 Divisor (M) = 3 Accumulator (A) = 0

$$\begin{array}{ll} 23 = 010111 & 3 = 000011 \\ -23 = 101001 & -3 = 111101 \end{array}$$

In case of doubts, Call #BharatSir @ 98204 08217	ACCUMULATOR	DIVIDEND	DIVISOR
	A (0)	Q (23)	M (3)
Initial Values	0 0 0 0 0 0	0 1 0 1 1 1	0 0 0 0 1 1
Step 1:			
Step 2:			
Step 3:			
Step 4:			
Step 5:			
Step 6:			
	Remainder (2)	Quotient (7)	



RESTORING DIVISION FOR SIGNED NUMBERS

- 1) Let M register hold the divisor, Q register hold the dividend.
- 2) A register should be the signed extension of Q.
- 3) On completion of the algorithm, Q will get the quotient and A will get the remainder.

Algorithm:

The **number of steps** required is equal to the **number of bits in the Dividend**.

- 1) At each step, **left shift the dividend by 1 position**.
- 2) If Sign of A and M is the same then **Subtract the divisor from A** (perform $A - M$),
Else **Add M to A**
- 3) After the operation,
If **Sign of A remains the same** or the **dividend** (in A and Q) **becomes zero**,
then the step is said to be "**Successful**".
In this case **quotient bit will be "1"** and **Restoration is NOT Required**.
- 4) If **Sign of A changes**, then the step is said to be "**Unsuccessful**".
In this case **quotient bit will be "0"**.
Here Restoration is Performed.
Hence, the method is called Restoring Division.

Repeat steps 1 to 4 for **all bits** of the Dividend.

Note: The result of this algorithm is such that, the quotient will always be positive and the remainder will get the same sign as the dividend.



Example: (5) / (3)

$$5 = 0101 \quad 3 = 0011$$

$$-5 = 1011 \quad -3 = 1101$$

In case of doubts, Call #BharatSir @ 98204 08217	ACCUMULATOR	DIVIDEND	DIVISOR
	A (Sign Extension)	Q (5)	M (3)
Initial Values	0000	0101	0011
Step 1:			
Left-Shift	0000	101_	
Sign (A, M) Same: A - M	+1101		
Sign Changes: Unsuccessful	1101		
Restore	0000	1010	
Step 2:			
Left-Shift	0001	010_	
Sign (A, M) Same: A - M	+1101		
Sign Changes: Unsuccessful	1110		
Restore	0001	0100	
Step 3:			
Left-Shift	0010	100_	
Sign (A, M) Same: A - M	+1101		
Sign Changes: Unsuccessful	1111		
Restore	0010	1000	
Step 4:			
Left-Shift	0101	000_	
Sign (A, M) Same: A - M	+1101		
Sign still Same: Successful	0010		
Restore not required	0010	0001	
	Remainder (2)	Quotient (1)	



Example: (-19) / (7)

$$19 = 010011 \quad 7 = 000111$$

$$-19 = 101101 \quad -7 = 111001$$

In case of doubts, Call #BharatSir @ 98204 08217	ACCUMULATOR	DIVIDEND	DIVISOR
	A (Sign Extension)	Q (-19)	M (7)
Initial Values	1 1 1 1 1 1	1 0 1 1 0 1	0 0 0 1 1 1
Step 1:			
Left-Shift	1 1 1 1 1 1	0 1 1 0 1 _	
Sign (A, M) Different: A + M	+ 0 0 0 1 1 1		
Sign Changes: Unsuccessful	0 0 0 1 1 0		
Restore	1 1 1 1 1 1	0 1 1 0 1 0	
Step 2:			
Left-Shift	1 1 1 1 1 0	1 1 0 1 0 _	
Sign (A, M) Different: A + M	+ 0 0 0 1 1 1		
Sign Changes: Unsuccessful	0 0 0 1 0 1		
Restore	1 1 1 1 1 0	1 1 0 1 0 0	
Step 3:			
Left-Shift	1 1 1 1 0 1	1 0 1 0 0 _	
Sign (A, M) Different: A + M	+ 0 0 0 1 1 1		
Sign Changes: Unsuccessful	0 0 0 1 0 0		
Restore	1 1 1 1 0 1	1 0 1 0 0 0	
Step 4:			
Left-Shift	1 1 1 0 1 1	0 1 0 0 0 _	
Sign (A, M) Different: A + M	+ 0 0 0 1 1 1		
Sign Changes: Unsuccessful	0 0 0 0 1 0		
Restore	1 1 1 0 1 1	0 1 0 0 0 0	
Step 5:			
Left-Shift	1 1 0 1 1 0	1 0 0 0 0 _	
Sign (A, M) Different: A + M	+ 0 0 0 1 1 1		
Sign still Same: Successful	1 1 1 1 0 1		
Restore not required	1 1 1 1 0 1	1 0 0 0 0 1	
Step 6:			
Left-Shift	1 1 1 0 1 1	0 0 0 0 1 _	
Sign (A, M) Different: A + M	+ 0 0 0 1 1 1		
Sign Changes: Unsuccessful	0 0 0 0 1 0		
Restore	1 1 1 0 1 1	0 0 0 0 1 0	
	Remainder (-5)	Quotient (2)	



Example: (-8) / (-4)

$$\begin{array}{ll} 8 = 01000 & 4 = 00100 \\ -8 = 11000 & -4 = 11100 \end{array}$$

In case of doubts, Call #BharatSir @ 98204 08217	ACCUMULATOR	DIVIDEND	DIVISOR
	A (Sign Extension)	Q (-8)	M (-4)
Initial Values	1 1 1 1 1	1 1 0 0 0	1 1 1 0 0
Step 1:			
Left-Shift	1 1 1 1 1	1 0 0 0 _	
Sign (A, M) Same: A - M	+ 0 0 1 0 0		
Sign Changes: Unsuccessful	0 0 0 1 1		
Restore	1 1 1 1 1	1 0 0 0 0	
Step 2:			
Left-Shift	1 1 1 1 1	0 0 0 0 _	
Sign (A, M) Same: A - M	+ 0 0 1 0 0		
Sign Changes: Unsuccessful	0 0 0 1 1		
Restore	1 1 1 1 1	0 0 0 0 0	
Step 3:			
Left-Shift	1 1 1 1 0	0 0 0 0 _	
Sign (A, M) Same: A - M	+ 0 0 1 0 0		
Sign Changes: Unsuccessful	* 0 0 0 1 0		
Restore	* 1 1 1 1 0	0 0 0 0 0	
Step 4:			
Left-Shift	1 1 1 0 0	0 0 0 0 _	
Sign (A, M) Same: A - M	+ 0 0 1 0 0		
Dividend(A,Q)=0: Successful	0 0 0 0 0		
Restore not required	0 0 0 0 0	0 0 0 0 1	
Step 5:			
Left-Shift	0 0 0 0 0	0 0 0 1 _	
Sign (A, M) Different: A + M	+ 1 1 1 0 0		
Sign Changes: Unsuccessful	1 1 1 0 0		
Restore	0 0 0 0 0	0 0 0 1 0	
	Remainder (0)	Quotient (2)	



Example: (-14) / (2)

$$14 = 01110 \quad 2 = 00010$$

$$-14 = 10010 \quad -2 = 11110$$

In case of doubts, Call #BharatSir @ 98204 08217	ACCUMULATOR	DIVIDEND	DIVISOR
	A (Sign Extension)	Q (-14)	M (2)
Initial Values	1 1 1 1 1	1 0 0 1 0	0 0 0 1 0
Step 1:			
Left-Shift	1 1 1 1 1	0 0 1 0 _	
Sign (A, M) Different: A + M	+ 0 0 0 1 0		
Sign Changes: Unsuccessful	0 0 0 0 1		
Restore	1 1 1 1 1	0 0 1 0 0	
Step 2:			
Left-Shift	1 1 1 1 0	0 1 0 0 _	
Sign (A, M) Different: A + M	+ 0 0 0 1 0		
Sign Changes: Unsuccessful	0 0 0 0 0	Note that dividend part in (A, Q) is not zero	
Restore	1 1 1 1 0	0 1 0 0	
Step 3:		In case of doubts, call #BharatSir @ 98204 08217	
Left-Shift	1 1 1 0 0	1 0 0 0 _	
Sign (A, M) Different: A + M	+ 0 0 0 1 0		
Sign still Same: Successful	1 1 1 1 0		
Restore not required	1 1 1 1 0	1 0 0 0 1	
Step 4:			
Left-Shift	1 1 1 0 1	0 0 0 1 _	
Sign (A, M) Different: A + M	+ 0 0 0 1 0		
Sign still Same: Successful	1 1 1 1 1		
Restore not required	1 1 1 1 1	0 0 0 1 1	
Step 5:			
Left-Shift	1 1 1 1 0	0 0 1 1 _	
Sign (A, M) Different: A + M	+ 0 0 0 1 0		
Dividend(A,Q)=0: Successful	0 0 0 0 0	Note that dividend part in (A, Q) is Zero!	
Restore not required	0 0 0 0 0	0 0 1 1 1	
	Remainder (0)	Quotient (7)	



Example: (14) / (-2)

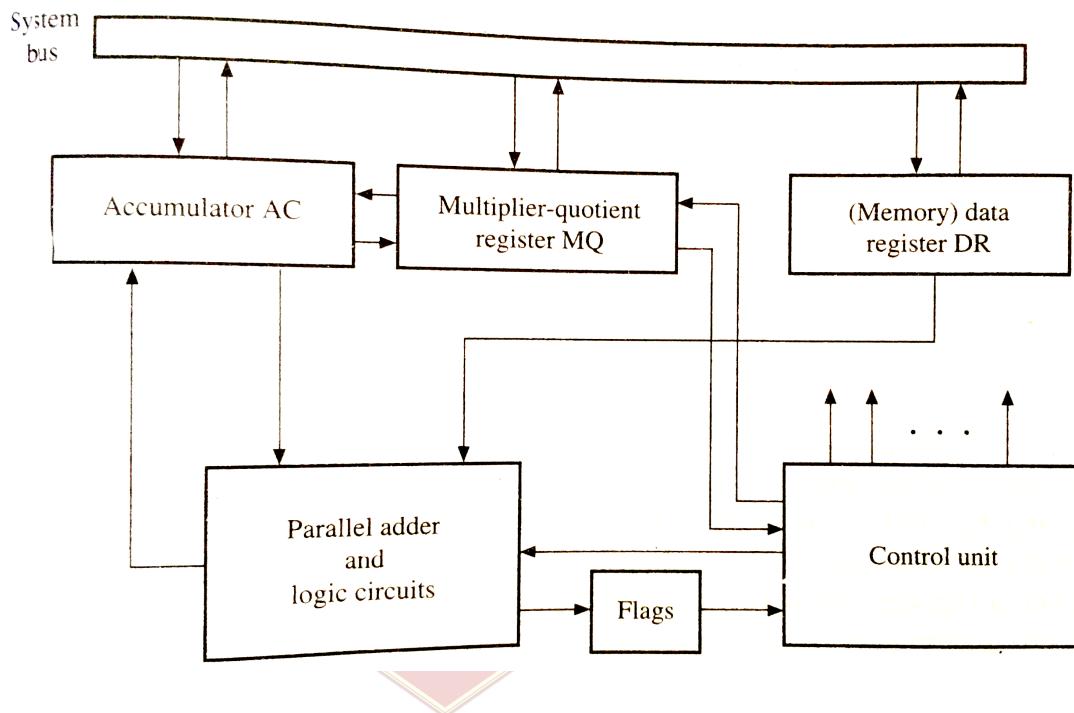
$$14 = 01110 \quad 2 = 00010$$

$$-14 = 10010 \quad -2 = 11110$$

In case of doubts, Call #BharatSir @ 98204 08217	ACCUMULATOR	DIVIDEND	DIVISOR
	A (Sign Extension)	Q (-14)	M (-2)
Initial Values	0 0 0 0 0	0 1 1 1 0	1 1 1 1 0
Step 1:			
Step 2:			
Step 3:	<i>In case of doubts, call #BharatSir @ 98204 08217</i>		
	<i>In case of doubts, call #BharatSir @ 98204 08217</i>		
	<i>In case of doubts, call #BharatSir @ 98204 08217</i>		
	<i>In case of doubts, call #BharatSir @ 98204 08217</i>		
Step 4:			
Step 5:			
	Remainder (0)	Quotient (7)	



TYPICAL ALU DESIGN



Addition

$$AC := AC + DR$$

Subtraction

$$AC := AC - DR$$

Multiplication

$$AC \cdot MQ := DR \times MQ$$

Division

$$AC \cdot MQ := MQ/DR$$

AND

$$AC := AC \text{ and } DR$$

OR

$$AC := AC \text{ or } DR$$

EXCLUSIVE-OR

$$AC := AC \text{ xor } DR$$

NOT

$$AC := \text{not}(AC)$$