

Homework 14: Multirate Signal Processing

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[»] Problem 12.21: Resampling downsampled sequences

Using the `downsample` function, resample the following sequences using the given parameters D and the offset k . Using the `stem` function, plot the original and downsampled signals.

(a) $x[n] = \sin(0.2\pi n)$, $0 \leq n \leq 50$, $D = 4$, $k = 0$, and $k = 2$.

(b) $x[n] = \cos(0.3\pi n)$, $0 \leq n \leq 60$, $D = 3$, $k = 0$, and $k = 1$.

[»] Problem 12.22: Resample decimated sequences

Using the `decimate` function, resample the following sequences using the given parameters D . Using the `stem` function, plot the original and decimated signals. Obtain results using both the default IIR and FIR decimation filters and comment on the results.

(a) $x[n] = \cos(0.4\pi n)$, $0 \leq n \leq 100$, $D = 2$.

(b) $x[n] = \sin(0.15\pi n)$, $0 \leq n \leq 100$, $D = 3$.

[✓] Problem 12.26: Interpolation using MATLAB's interp function

```
clear variables;
```

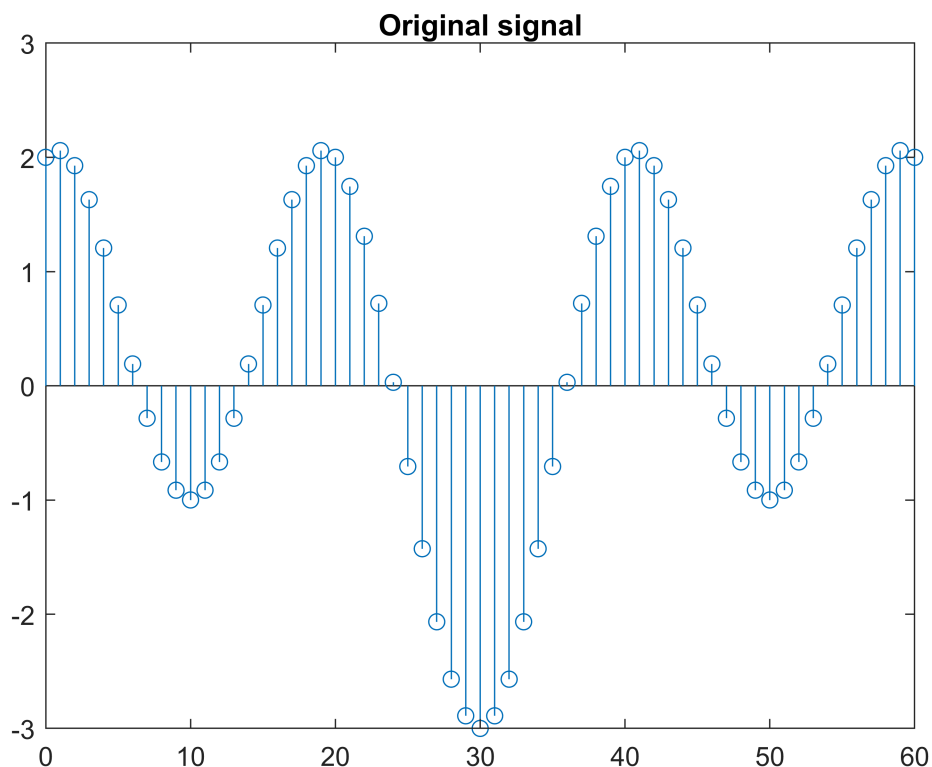
Let $x[n] = 2 \cos(0.1\pi n) + \sin(0.05\pi n)$, $0 \leq n \leq 60$.

- (a) Using the `interp` function, interpolate using $I = 3$, $I = 6$, and $I = 9$. Stem plot the original and interpolated signals.
- (b) Using the second output argument of the `interp` function, plot the frequency response of the lowpass filter used in each of the above interpolations.

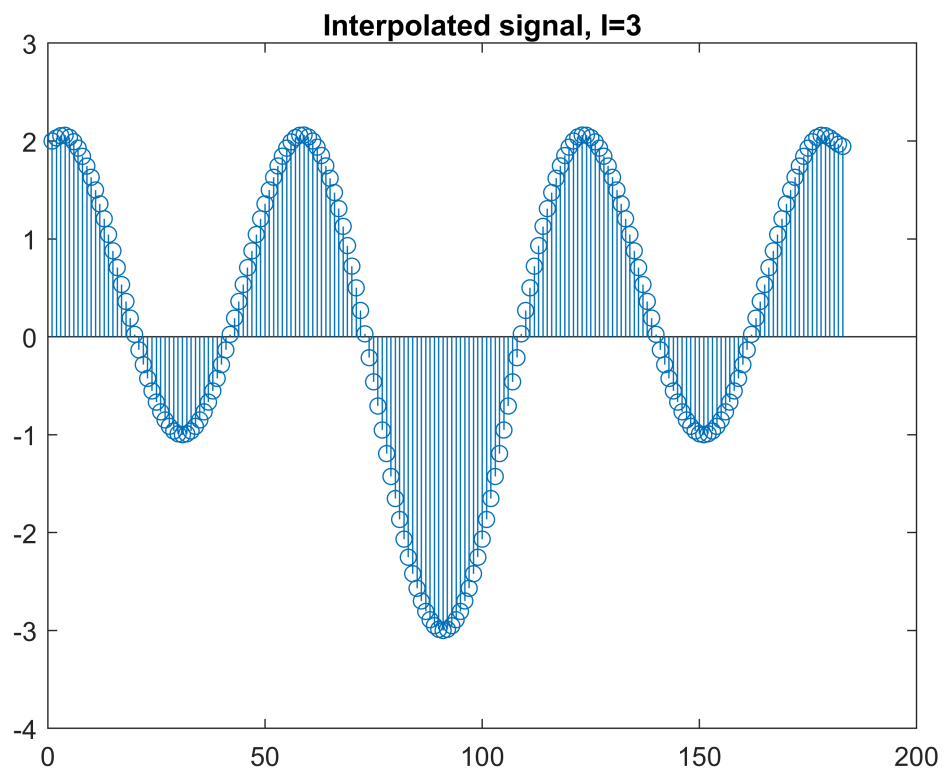
a) Interpolate signal using MATLAB's interp function

- (a) Using the `interp` function, interpolate using $I = 3$, $I = 6$, and $I = 9$. Stem plot the original and interpolated signals.

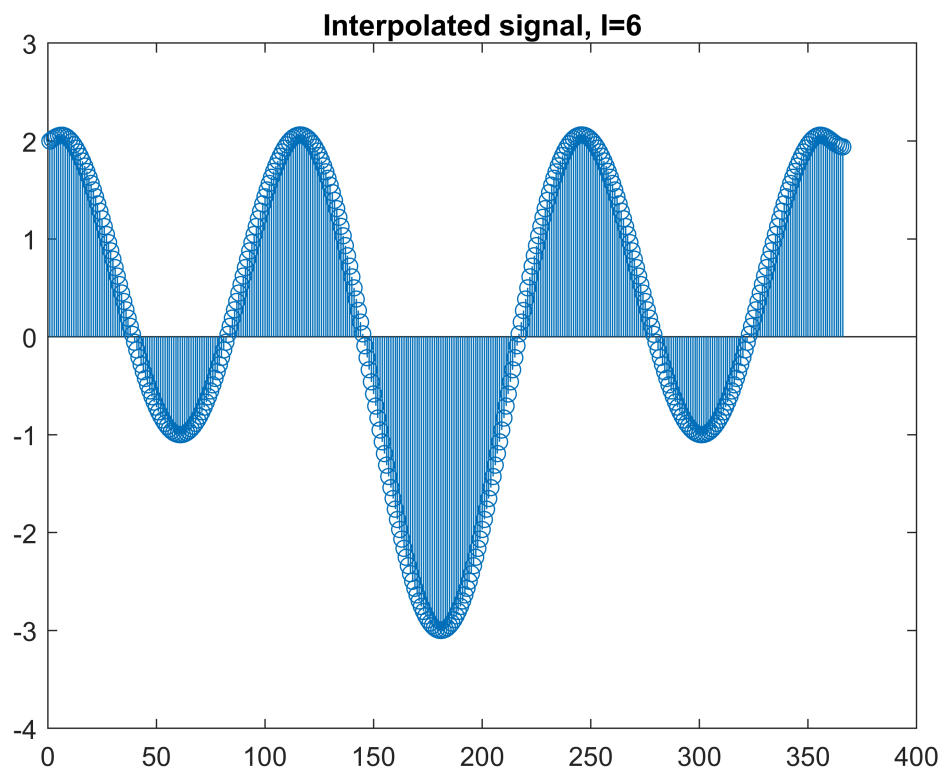
```
n = 0:60;  
x = 2*cos(0.1*pi*n) + sin(0.05*pi*n);  
  
stem(n, x)  
title('Original signal')
```



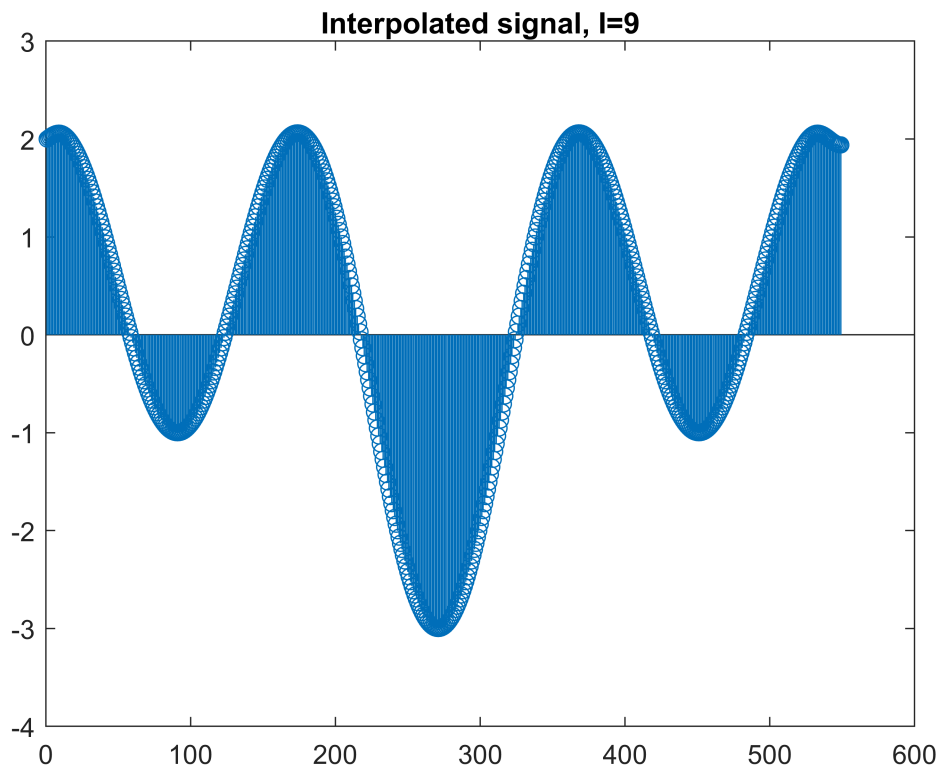
```
stem(interp(x, 3))  
title('Interpolated signal, I=3')
```



```
stem(interp(x, 6))  
title('Interpolated signal, l=6')
```



```
stem(interp(x, 9))  
title('Interpolated signal, I=9')
```

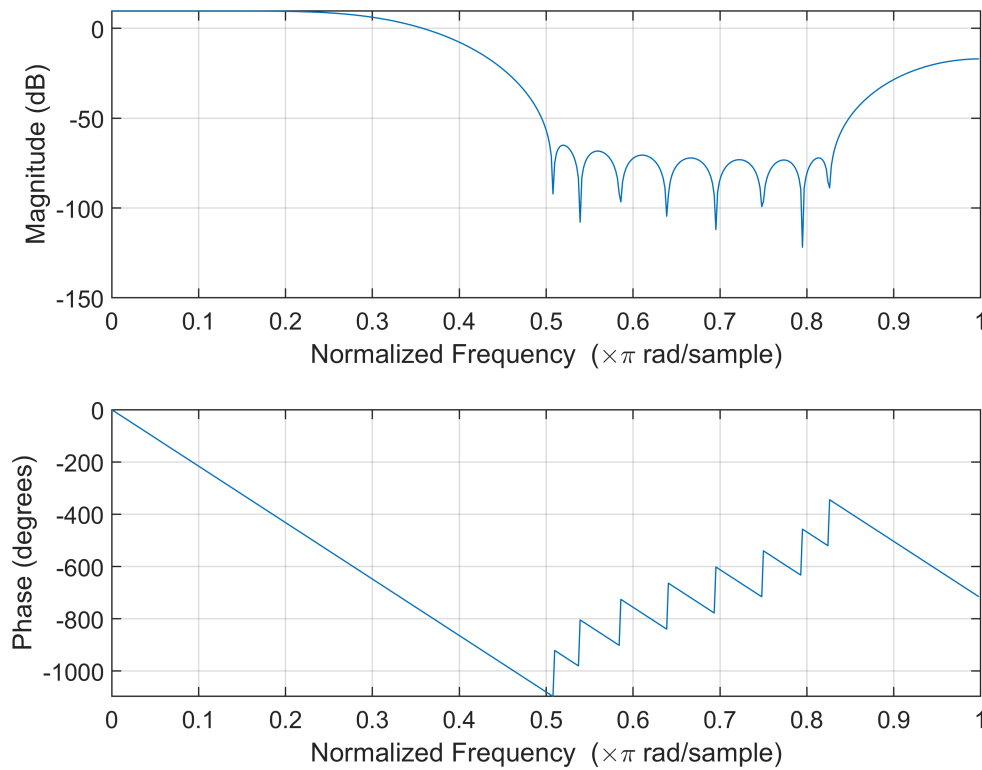


b) Plot the frequency response of the lowpass filter

(b) Using the second output argument of the `interp` function, plot the frequency response of the lowpass filter used in each of the above interpolations.

`[y,b] = interp(x,r,n,cutoff)` returns a vector, `b`, with the filter coefficients used for the interpolation.

```
[y, b] = interp(x, 3);
freqz(b, 1)
```



[»] Problem 12.19: Compare spectrum of a downsampled signal with the original

```
clear variables;
```

Consider the signal $x[n] = 0.9^n u[n]$. It is to be downsampled by a factor of $D = 3$ to obtain $x_D[n]$.

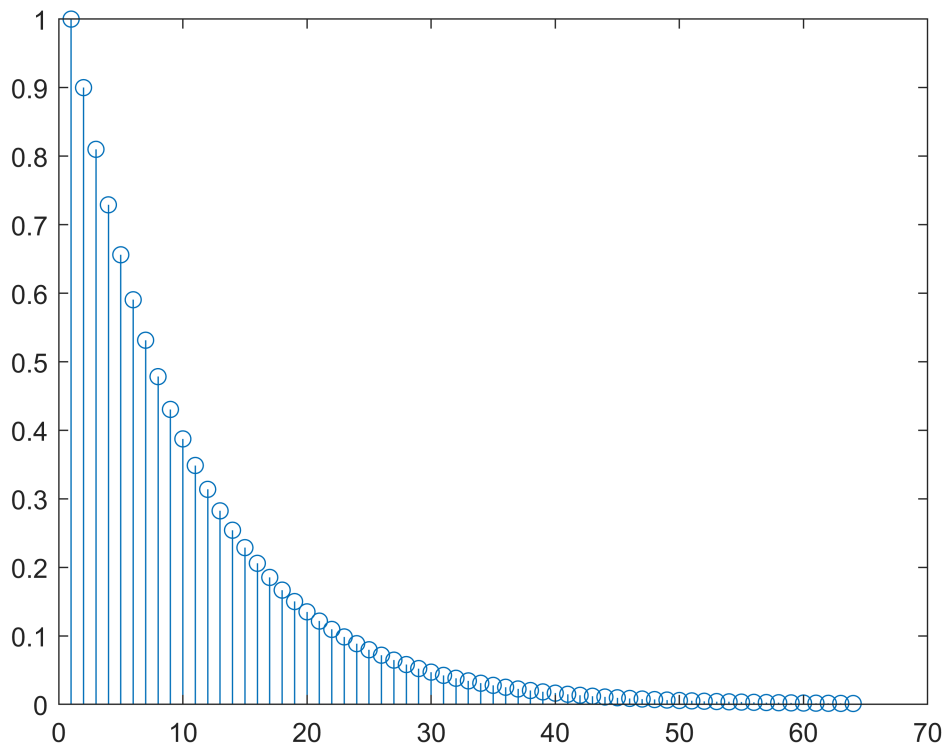
- (a) Compute the spectrum of $x[n]$ and plot its magnitude.
- (b) Compute the spectrum of $x_D[n]$ and plot its magnitude.
- (c) Compare the two spectra.

The *unit step* sequence is given by

$$u[n] \triangleq \begin{cases} 1, & n \geq 0 \\ 0, & n < 0 \end{cases}$$

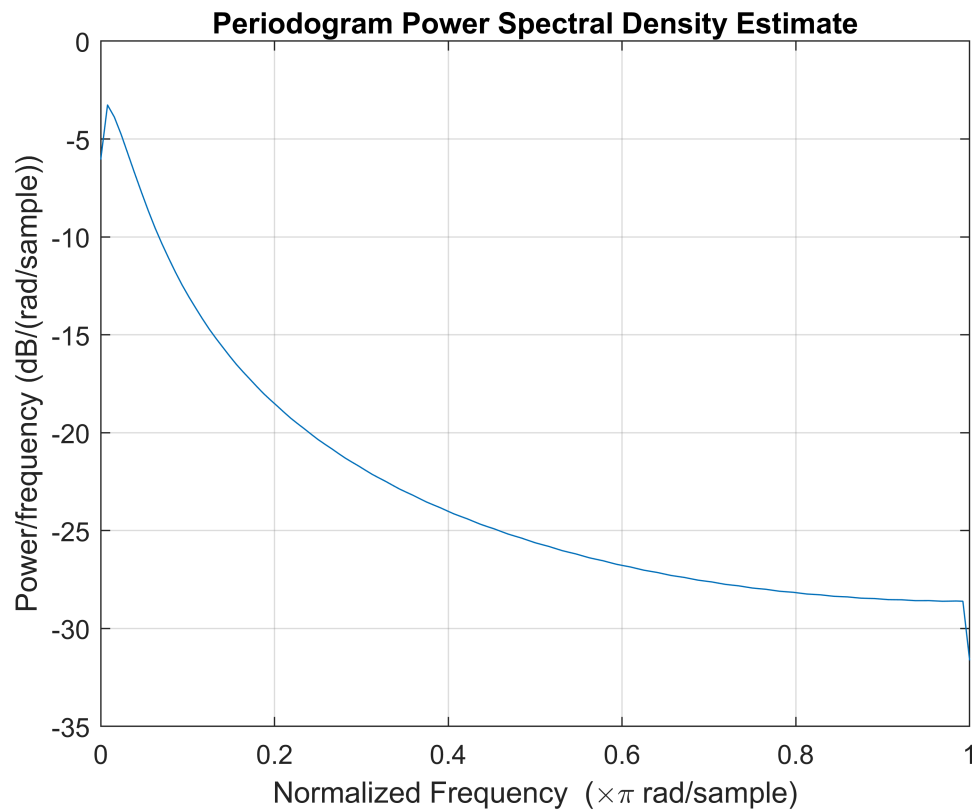
a) Compute the spectrum of the original signal and plot its magnitude

```
N = 64;  
n = 0:N-1;  
x = 0.9.^n;  
% x = exp(-n);  
stem(x)
```



[?] How do you compute the spectrum of the signal?

```
periodogram(x)
```



- a) Compute the spectrum of the signal and plot its magnitude
- b) Compute the spectrum of the downsampled signal and plot its magnitude
- c) Compare the two spectra

ADSI Problem 8.1: Upsampling with linear interpolation

```
clear variables;
```

Consider a signal given by:

$$x[n] = \begin{cases} -1 & n = 1 \\ 3 & n = 2 \\ 0 & \text{elsewhere} \end{cases}$$

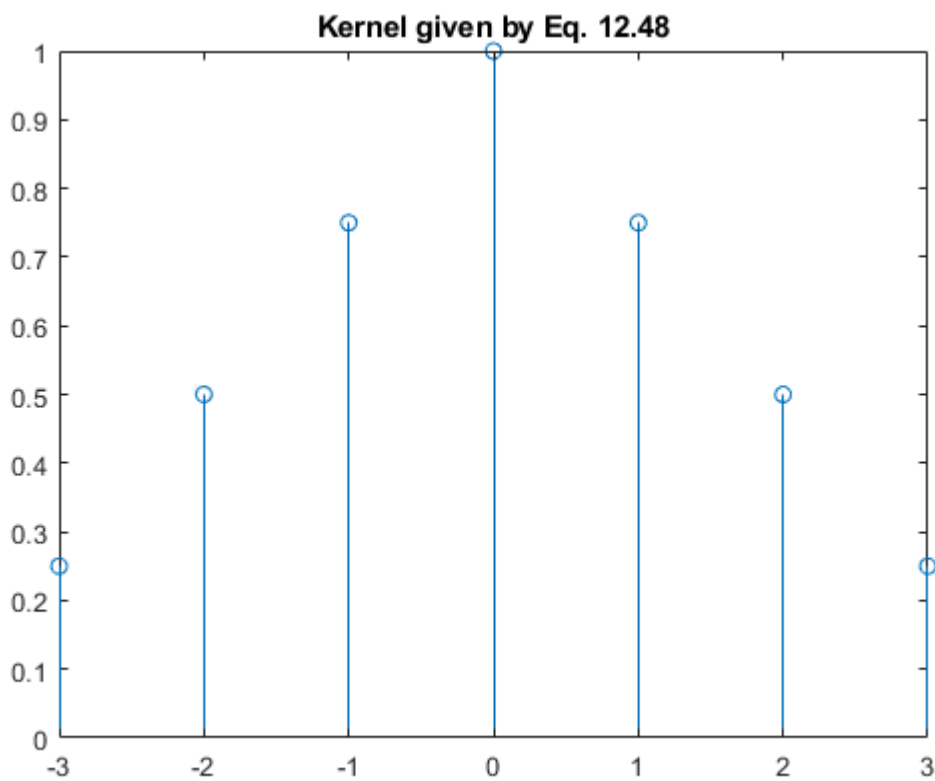
```
N = 10;
n = 1:N;
x = zeros(N,1);
x(1) = -1;
x(2) = 3;
```

1. Upsample the signal using $I = 4$ and the linear interpolation kernel given by Eq. 12.48.

$$g_{\text{lin}}[n] \triangleq \begin{cases} 1 - \frac{|n|}{I}, & -I < n < I \\ 0, & \text{otherwise} \end{cases} \quad (12.48)$$

```
I = 4;
gn = -I+1:1:I-1;
g = 1 - abs(gn)/I; % g = triang(I*2-1)

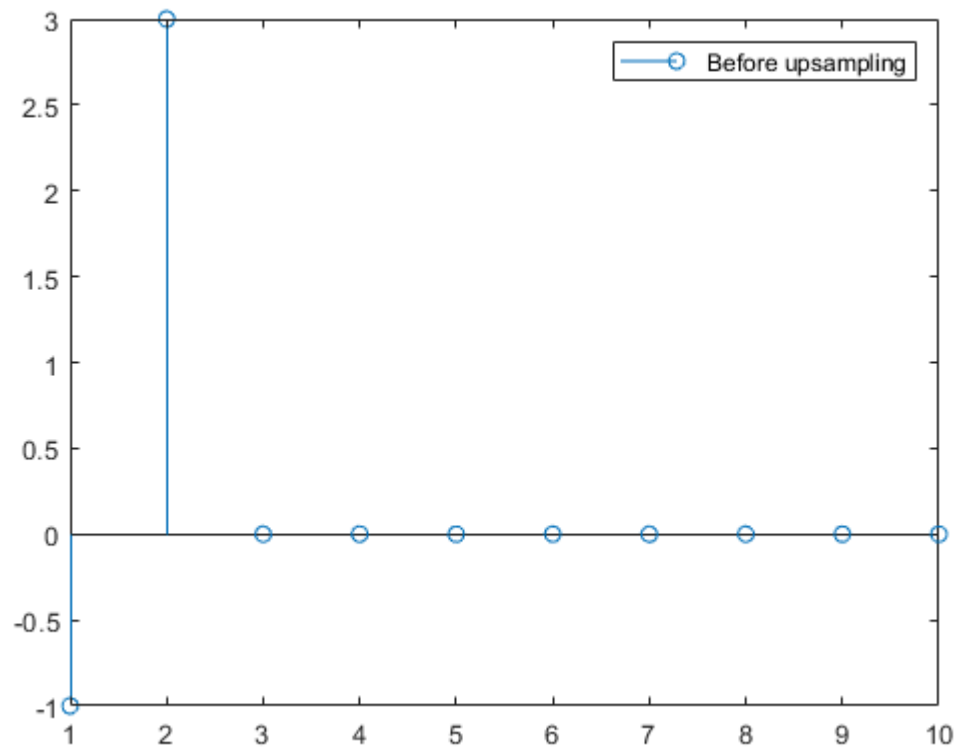
stem(gn, g);
title('Kernel given by Eq. 12.48')
```



```
x_upsampled = conv(x, g);
```

2. Sketch the signal before and after the upsampling and interpolation.

```
stem(n, x)  
legend('Before upsampling')
```



```
stem(x_upsampled)  
legend('Upsampled')
```

