

**ESE 546, FALL 2020**

**HOMEWORK 5**

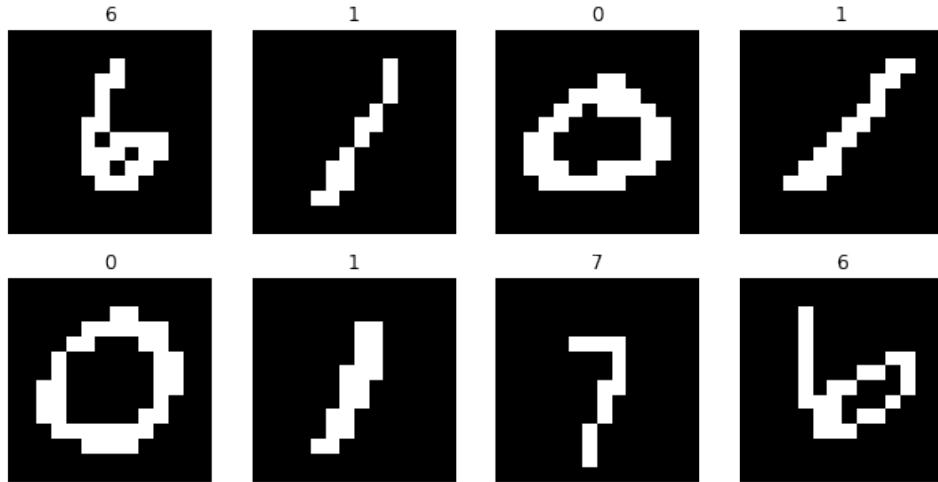
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**Solution 1** (Time spent: 2 hour). (1) To Prove:

$$\text{KL}(q\|p) = \beta \sum_{w \in \mathcal{W}} q(w)\Phi(w) + \sum_{w \in \mathcal{W}} q(w) \log q(w) + \log Z(\beta)$$

**Solution 2** (Time spent: 10 hours). Plots from the Jupyter notebook attached here for reference.

(1) Plot of Binarized and 14\*14 subsampled images of MNIST



(2) Encoder and Decoder classes.

```
class Encoder(nn.Module):
    def __init__(self):
        super(Encoder, self).__init__()
        self.fc1 = nn.Linear(196, 128)
        self.fc2 = nn.Linear(128, 16)
        self.fc3 = nn.Linear(128, 16)

    def forward(self, x):
        reshaped = x.reshape(x.shape[0], -1)
        out = torch.tanh(self.fc1(reshaped))
        fc2_out = self.fc2(out)
        fc3_out = self.fc3(out)

        mu = (fc2_out[:, :8] + fc3_out[:, :8])/2
        logvar = (fc2_out[:, 8:] + fc3_out[:, 8:])/2

        std = logvar.mul(0.5).exp_()
        eps = torch.randn_like(std)
        z = eps.mul(std).add_(mu)
```

```
    return z, mu, logvar
```

```
class Decoder(nn.Module):
    def __init__(self):
        super(Decoder, self).__init__()
        self.fc1 = nn.Linear(8, 128)
        self.fc2 = nn.Linear(128, 196)

    def forward(self, x):
        out = torch.tanh(self.fc1(x))
        out = torch.sigmoid(self.fc2(out))
        return out
```

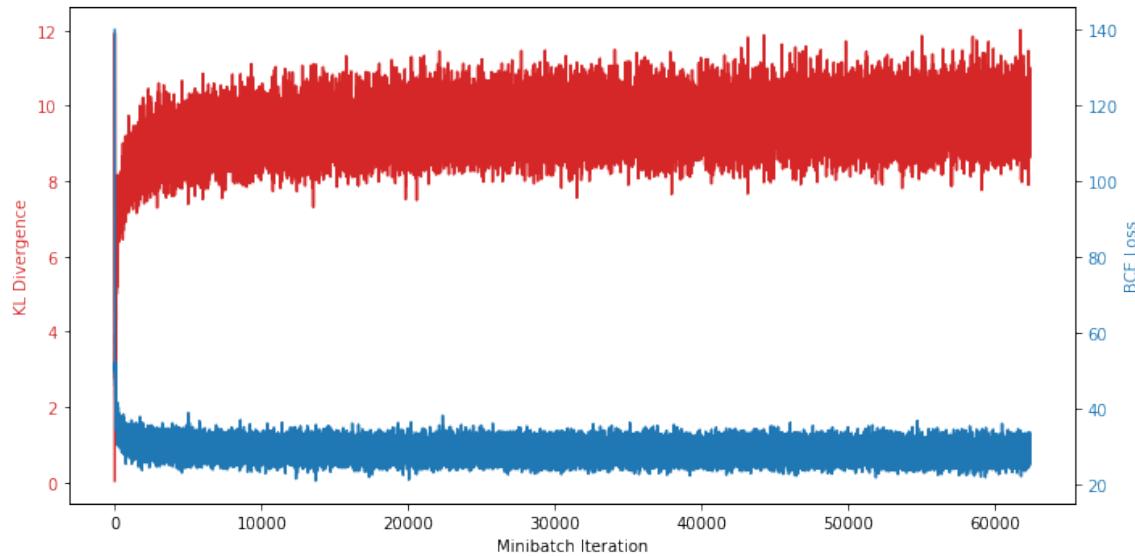
Loss functions.

```
def KL(mu, sigma):
    contribution = 1 + sigma - mu**2 - torch.exp(sigma)
    return (torch.sum(-contribution/2))

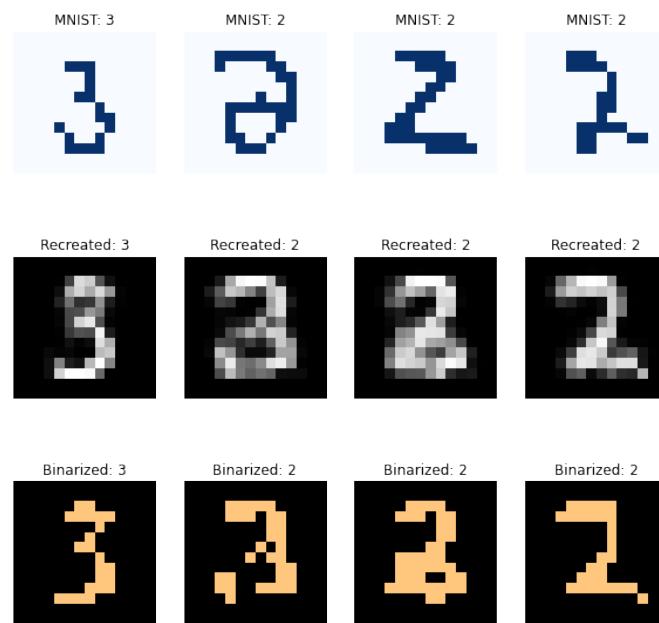
def TotalLoss(x, mu, sigma, decoding):
    kl_loss = KL(mu, sigma)

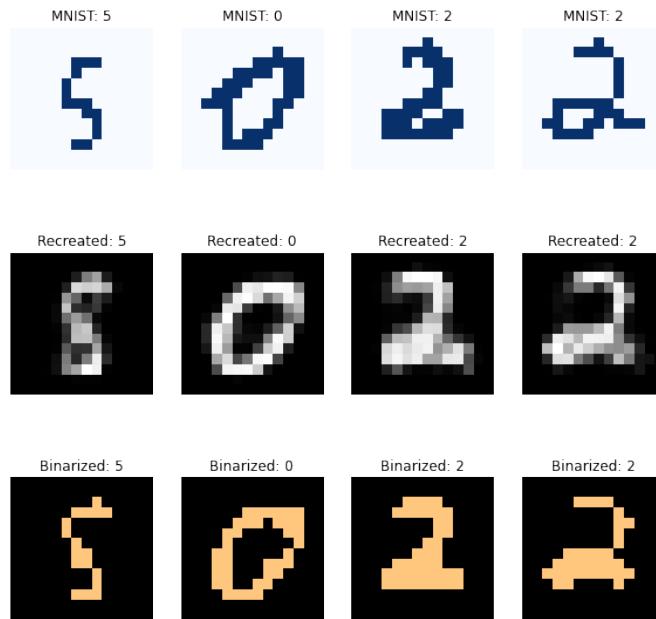
    bce = F.binary_cross_entropy(decoding,
                                 x.view(-1, 196),
                                 reduction='sum')
    return (kl_loss + bce, kl_loss, bce)
```

- (3) Plot of first and second term of ELBO as a function of the number of weight updates.



- (4) Reconstruction of MNIST images using the Autoencoder.





(5) Images created by sampling from the generative model and running the decoder.

