Descriptives - Redux

Mid Semester Check-in

These first 5 weeks have been jam packed with getting you up to speed using R. By now, you should feel comfortable with:

- Importing data
- Manipulating data (getting subsets, using logical operators, knowing the different data classes and when one is more appropriate than another, etc.)
- Plotting data with ggplot2

Where we're going

The next 5 weeks are going to be dedicated in getting you up to speed on statistics. Everyone in this class should have taken Psych 300 (Intro Psych Stats) or equivalent. *If you have not taken this class (or equivalent), you must get in touch with me ASAP.*

What you can expect:

- Refresh your memory about stats. The content presented will hopefully go into slightly more depth (for certain topics) than what you covered in Psych Stats. But it shouldn't be new, per se.
- Applying this theoretical knowledge to practical knowledge in R. You will be expected to know what the outputs mean (e.g., how to interpret them).
- As of now, there will not be any Practice Sets for this unit on statistics. I will update you if there are any changes on this front.
- No HW assignments. Quizzes based on lecture content (10 questions max/quiz). Lecture content longer and denser...but no HW!!

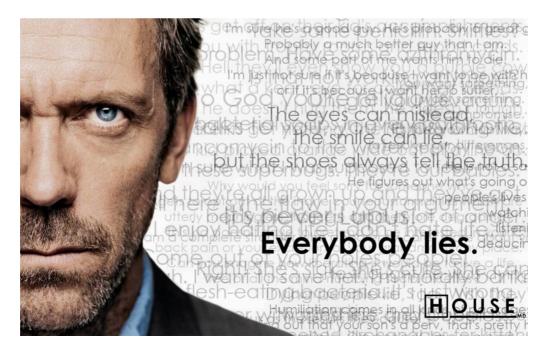
Why are we *not* going to talk about more advanced stats in these few weeks?

This time

- Descriptive Stats
- Bias
- *z*-scores

Why do we describe data?

- Understand your data
 - There's a lot to learn from descriptive statistics
- Find errors in data entry or collection
- Everybody lies...including numbers and data



Happiness

Examples today are based on data from the 2015 World Happiness Report, which is an annual survey part of the Gallup World Poll.

You should be able to download the dataset from 20: Descriptives lecture.

Get in touch with me ASAP if you cannot download this dataset

world Data

Country	Happiness	GDP	Support	Life	Freedom	Generosity	Corrup
Albania	4.606651	9.251464	0.6393561	68.43517	0.7038507	-0.0823377	0.884
Argentina	6.697131	NA	0.9264923	67.28722	0.8812237	NA	0.850
Armenia	4.348319	8.968936	0.7225510	65.30076	0.5510266	-0.1866965	0.901
Australia	7.309061	10.680326	0.9518616	72.56024	0.9218710	0.3157020	0.356
Austria	7.076447	10.691354	0.9281103	70.82256	0.9003052	0.0890886	0.557
Azerbaijan	5.146775	9.730904	0.7857028	61.97585	0.7642895	-0.2226351	0.615

About the world dataset

Happiness: "Please imagine a ladder, with steps numbered from 0 at the bottom to 10 at the top. The top of the ladder represents the best possible life for you and the bottom of the ladder represents the worst possible life for you. On which step of the ladder would you say you personally feel you stand at this time?"

GDP: Log gross domestic product per capita

Support: "If you were in trouble, do you have relatives or friends you can count on to help you whenever you need them, or not?"

Life: Healthy life expectancy at birth

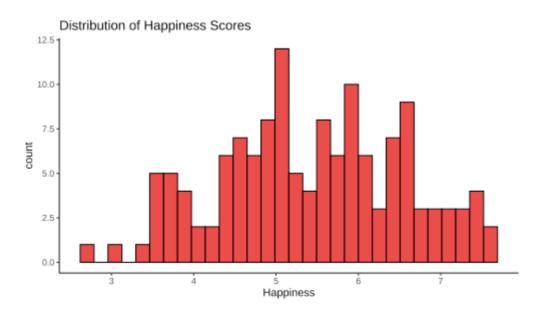
Freedom: "Are you satisfied or dissatisfied with your freedom to choose what you do with your life?"

Corruption: "Is corruption widespread throughout the government or not" and "Is corruption widespread within businesses or not?" (average of 2 questions)

Generosity: "Have you donated money to a charity in the past month?" (residual, adjusting for GDP)

Distributions

A **distribution** often refers to a description of the [relative] number of times a variable X will take each of its unique values.



Central Tendencies

- Mean (average; μ , \bar{X}) -- mean ()
- Median (middle-est) -- median()

##

2

• **Mode** (most) -- No built-in R function for the mode! We can use a different function we've already seen:

```
variable <- c(1,2,3,4,1,1,3,4,3,4,4,1,2,4,4)
table(variable)

## variable
## 1 2 3 4
## 4 2 3 6

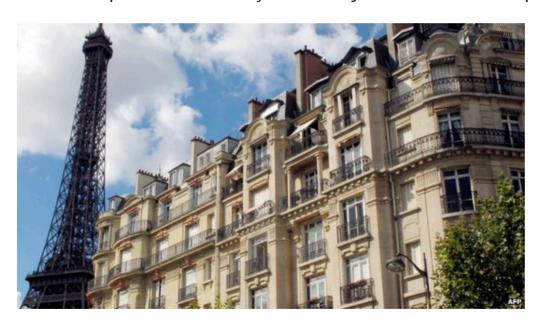
variable <- c("hello", "world", "hello")
table(variable)

## variable
## wariable
## hello world</pre>
```

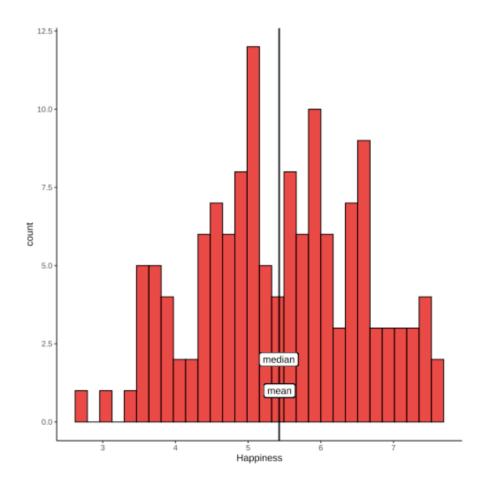
The Mean Can Lie

It's important to remember that the mean of a population (or group) may not represent well some (or any) members of the population.

• Example: André-François Raffray and the French apartment

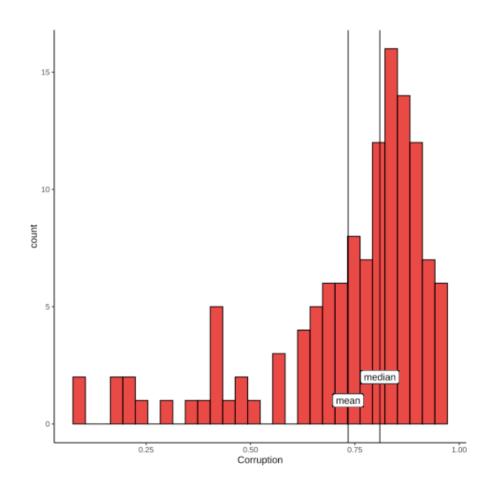


If Normal, All Relatively Equal



If Skewed...

...both the mean and median get pulled away from the mode. The mean is pulled further.



Center and spread

- Distributions are most often described by their mean and variance or standard deviation
- These are both measures of dispersion; how fat or skinny are your distributions?
- The mean represents the average score in a distribution. A good measure of spread will tell us something about how the typical score deviates from the mean.

$$\circ x - \bar{x}$$

Why can't we use the average deviation?

Average deviation

```
x \leftarrow c(7,7,8,3,9,2)
mean(x)
## [1] 6
x - mean(x)
## [1] 1 1 2 -3 3 -4
sum(x - mean(x))
## [1] 0
sum(x - mean(x))/length(x)
## [1] 0
```

Sum of Squares (SS)

Our solution is to square the deviation scores

```
x <- c(7,7,8,3,9,2)
mean(x)

## [1] 6

deviation <- x - mean(x)
deviation^2

## [1] 1 1 4 9 9 16

sum(deviation^2)

## [1] 40</pre>
```

Is there any inherent meaning in the Sum of Squares?

Variance

We calculate the average squared deviation: this is our variance, σ^2 :

```
# nested functions galore!
sum((x - mean(x))^2)/length(x)
```

```
## [1] 6.666667
```

Good things about variance:

- It's additive.
 - \circ Given two variables X and Y, if I create Z=X+Y then Var(Z)=Var(X)+Var(Y)
- Represents all values in a dataset

Bad things about variance:

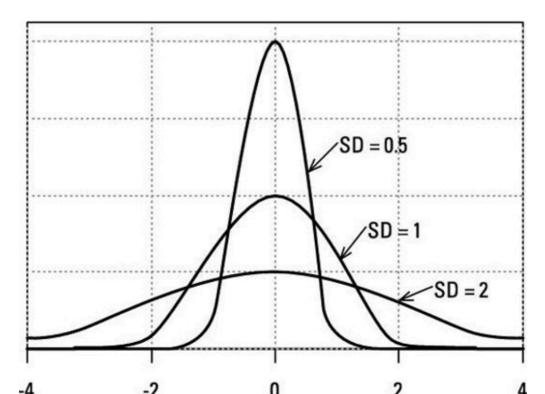
What the heck does it mean?

Standard Deviation

Standard deviation σ is the square root of the variance.

```
sqrt(sum((x - mean(x))^2)/length(x))
```

[1] 2.581989



Bias

Populations versus Samples

Why are these different?

```
# how we calculated variance "by hand" in this lecture
sum((x - mean(x))^2)/length(x)

## [1] 6.666667

# R's default variance function
var(x)

## [1] 8
```

Populations versus Samples

The value that represents the entire *population* is called a **parameter**.

ullet Population parameters are represented with Greek letters (μ , σ)

We collect samples to estimate the properties of populations; the value that represents a *sample* is called a **statistic**.

• Sample statistics are represented with Latin letters (x, \bar{x} , s).

Bias: An estimator is biased if its expected value and the true value of the parameter are different.

- Our estimates of standard deviation & variance (in the formulas up until now) are biased
- They *under*estimate variability in the population

Populations versus Samples

Variance

Population

$$\sigma^2 = rac{\Sigma (X_i - \mu)^2}{N}$$

Sample

$$s^2=\hat{\sigma}^2=rac{\Sigma(X_i-ar{X})^2}{N-1}$$

Standard Deviation

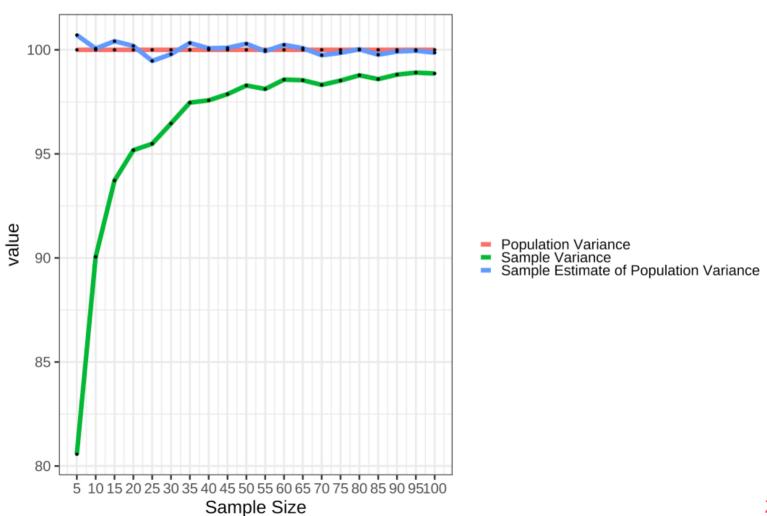
Population

$$\sigma = \sqrt{rac{\Sigma(X_i - \mu)^2}{N}}$$

Sample

$$s = \hat{\sigma} = \sqrt{rac{\Sigma (X_i - ar{X})^2}{N-1}}$$

Simulating Bias



Standardized scores

Why not always use raw scores?

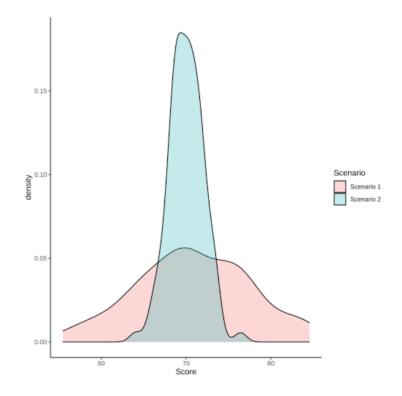
Scenario 1:

- Mean = 70, N = 100
- Range = 0 100
- You get a 71. Good?

Scenario 2:

- Mean = 70, N = 100
- Range = 65 75
- You get a 71. Good?

```
ggplot(full, aes(x = Score)) +
  geom_density(aes(fill = Scenario), alpha = .3) +
  theme_classic()
```



Problem with Raw Scores

- Raw scores are only meaningful in the *context* of the distribution
- What distirbution are you looking at? Patients, controls, patients + controls etc.?
- What does the distribution itself look like? Skinny, fat?
- A raw score can't take all of this into consideration! What does an exam score of 71 mean *in context*?

z-scores

- Raw scores are in the original metric's units (exam points, heigh in inches etc.)
- *z*-scores are in units of standard deviation; aka "standardized scores"
- Interpretation: distance from the mean, in standard deviations.

Formula:

$$z=rac{x_i-ar{x}}{s}$$

R function:

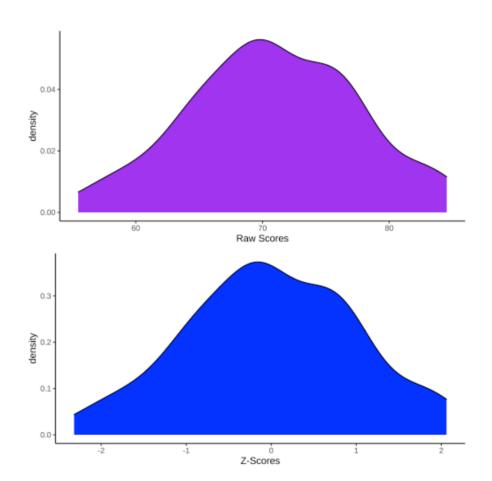
scale() -- but be warned, the output is usually a matrix

z-scores

Step 1: Take an entire set of raw scores (x_i)

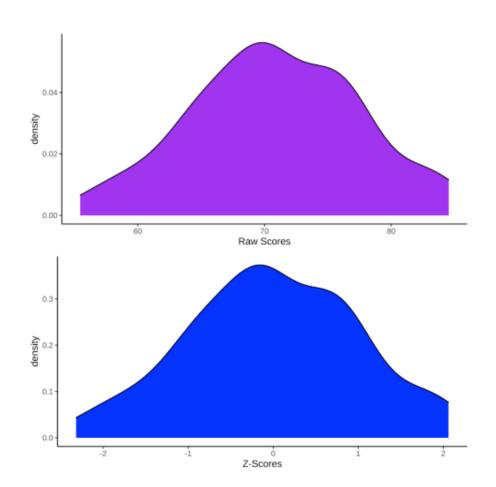
Step 2: Convert them into zscores

Step 3: Now look at the distribution of z-scores



Properties of z-scores

- $\bar{x}=0$
- *s* = 1



z-scores

$$z=rac{x_i-ar{x}}{s}$$

Why is this useful?

- Compare across scales and unit of measures
- More easily identify extreme data

Which variable has outliers?

```
psych::describe(world, fast =T)
```

```
##
                              sd
                                   min
                       mean
                                         max range
                                                     se
             vars
                    n
##
                1 136
                      NaN
                              NA
                                 Inf
                                        -Inf -Inf
                                                     NΑ
  Country
  Happiness
                2 136
                      5.43 1.11
                                 2.70
                                        7.60 4.90 0.10
##
  GDP
                3 121
                       9.22 1.16
                                 6.61 11.43 4.82 0.11
  Support
                4 135
                       0.80 0.12
                                  0.43 0.99 0.55 0.01
##
  Life
                5 135 63.12 7.46 43.74 76.04 32.30 0.64
  Freedom
                      0.75 0.13
                6 132
                                  0.40
                                        0.98 0.58 0.01
  Generosity
                7 120
                      0.00 \ 0.16 \ -0.28
                                        0.46 0.74 0.01
  Corruption
                8 125
                       0.73 0.20
                                        0.96 0.87 0.02
                                 0.09
```

Which variable has outliers?

```
world %>%
  mutate_if(is.numeric, scale) %>%
  psych::describe(., fast =T)
##
                               min
                    n mean sd
                                    max range
                                                se
             vars
                       NaN NA Inf -Inf -Inf
                1 136
                                                NΑ
  Country
  Happiness
                2 136
                         0 1 -2.46 1.96 4.42 0.09
##
  GDP
                3 121
                         0 1 -2.26 1.91 4.17 0.09
                4 135
                         0 1 -2.99 1.51 4.50 0.09
  Support
## Life
                5 135
                         0 1 -2.60 1.73 4.33 0.09
## Freedom
                6 132
                         0 1 -2.64 1.71 4.34 0.09
                         0 1 -1.80 2.90 4.70 0.09
## Generosity
             7 120
                         0 1 -3.20 1.14 4.34 0.09
## Corruption
                8 125
```