Interactions (V)

Last time...

Factorial ANOVA

- Estimated marginal means
- Estimated cell means
- Sums of squares

Power

- Omnibus test
- Coefficients

ANOVA vs Regression

Factorial ANOVA

Interaction tests whether there are differences in differences.

Simple main effect -the effect of Factor A
at a specific level of
Factor B

Regression

Interaction tests whether slope changes.

Simple slopes -- the slope of Variable A at a specific level of Variable B

Power

The likelihood of finding an effect *if the effect* actually exists.

When calculating power for the omnibus test, use the expected multiple R^2 value to calculate an effect size: $f^2=\frac{R^2}{1-R^2}$

To estimate power for a single coefficient, you need to consider (1) how much variance is accounted for by just the variable and (2) how much variance you'll account for in Y overall.

$$f^2=rac{R_Y^2-R_{Y.X}^2}{1-R_Y^2}$$

Effect sizes (interactions)

To start our discussion on powering interaction terms, we need to first consider the effect size of an interaction.

How big can we reasonably expect an interaction to be?

• Interactions are always partialled effects; that is, we examine the relationship between the product of variables X and Z only after we have controlled for X and controlled for Z. How does this affect the size of the relationship between XZ and Y?

Effect sizes (interactions)

The effect of XZ and Y will get **smaller** as X or Z (or both) is related to the product

The semi-partial correlation is always smaller than or equal to the zero-order correlation.

McClelland and Judd (1993)

Is it more difficult to find interaction effects in experimental studies or observational studies?

What factors make it relatively easier to find interactions in experimental work?

Influencing power in experimental studies

- No measurement error of IV
 - don't have to guess what condition a participant is in
 - measurement error is exacerbated when two variables measured with error are multiplied by each other
- Experimentalists are more likely to find cross-over interactions; observational studies may be restricted to fan interactions
 - cross-over interactions are easier to detect than fan interactions

Influencing power in experimental studies

- Experimentalists can concentrate scores on extreme ends on both X and Z
 - in observational studies, data tends to cluster around the mean
 - increases variability in both X and Z, and in XZ
- Experimentalists can also force orthognality in X and Z
- Experimentalists can study the full range of X in an experiment

McClelland and Judd's simulation

For the experiment simulations, we used 2 X 2 factorial designs, with values of X and Z equal to +1 and —1 and an equal number of observations at each of the four combinations of X and Z values.

```
X = rep(c(-1,1), each = 50)

Z = rep(c(-1,1), times = 50)

table(X,Z)
```

```
## Z
## X -1 1
## -1 25 25
## 1 25 25
```

McClelland and Judd's simulation

For the field study simulations, they used values of X and Z that varied between the extreme values of +1 and —1. More specifically, in the field study simulations, values of X and Z were each sampled independently from a normal distribution with a mean of 0 and a standard deviation of 0.5. Values of X and Z were rounded to create equally spaced 9-point scales ranging from -1 to +1 because ranges in field studies are always finite and because ratings are often on scales with discrete intervals.

McClelland and Judd's simulation

For field studies

```
X = rnorm(n = 100, mean = 0, sd = .5)
Z = rnorm(n = 100, mean = 0, sd = .5)
X = round(X/.2)*.2
Z = round(Z/.2)*.2
psych::describe(data.frame(X,Z), fast = T)
```

```
## vars n mean sd min max range se
## X 1 100 -0.05 0.5 -1.2 1.2 2.4 0.05
## Z 2 100 0.03 0.5 -1.6 1.2 2.8 0.05
```

For both: $eta_0=0, eta_X=eta_Z=eta_{XZ}=1.$ N=100 , and randomly sampled normally distributed errors ($\mu=0,\sigma=4$)

Y = 0 + 1*X + 1*Z + 1*X*Z + rnorm(n = 100, mean = 0, sd = 4)

```
summarv(lm(Y \sim X*Z))
##
## Call:
## lm(formula = Y \sim X * Z)
##
## Residuals:
##
      Min 10 Median 30
                                     Max
## -11.2002 -3.2569 -0.4427 3.1085 10.0917
##
## Coefficients:
            Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 0.7331
                    0.4710 1.557 0.123
## X
    1.3502 0.9430 1.432 0.155
## Z 1.3674 0.9615 1.422 0.158
             -2.8471 2.0902 -1.362 0.176
## X:Z
##
## Residual standard error: 4.679 on 96 degrees of freedom
```

set.seed(0305)

```
# for experimental studies
sim = 100
ebeta_xz = numeric(length = )
et_xz = numeric(length = 100
for(i in 1:sim){
 # simulate data
 X = rep(c(-1,1), each = 50)
  Z = rep(c(-1,1), times = 50)
   Y = 0 + 1*X + 1*Z + 1*X*Z
    rnorm(n = 100, mean = 0,
  #run model
  model = lm(Y \sim X*Z)
  coef = coef(summary(model))
  #extract coefficients
  beta = coef["X:Z", "Estima"]
  t_val = coef["X:Z", "t value"
  #save to vectors
  ebeta_xz[i] = beta
  et xz[i] = t_val
```

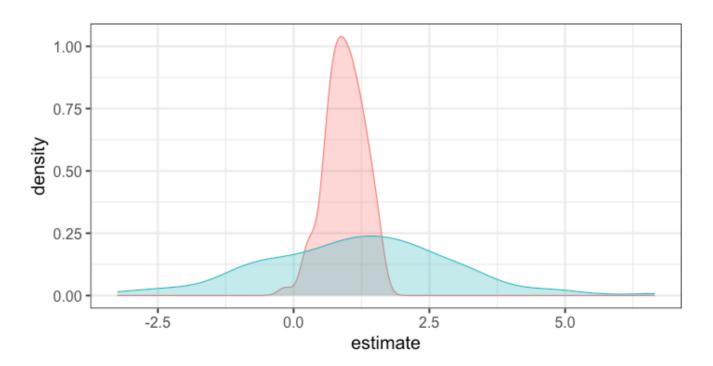
```
# for observational studies
obeta_xz = numeric(length = 1
ot_xz = numeric(length = 100
for(i in 1:sim){
  # simulate data
 X = rnorm(n = 100, mean=0,
 Z = rnorm(n = 100, mean=0,
 X = round(X/.2)*.2
  Z = round(Z/.2)*.2
  Y = 0 + 1*X + 1*Z + 1*X*Z
    rnorm(n = 100, mean = 0,
  #run model
  model = lm(Y \sim X*Z)
  coef = coef(summary(model)
  #extract coefficients
  beta = coef["X:Z", "Estima"
  t_val = coef["X:Z", "t val
  #save to vectors
  obeta_xz[i] = beta
  ot_xz[i] = t_val
```

mean(ebeta_xz)

[1] 0.9440304

mean(obeta_xz)

[1] 1.175444

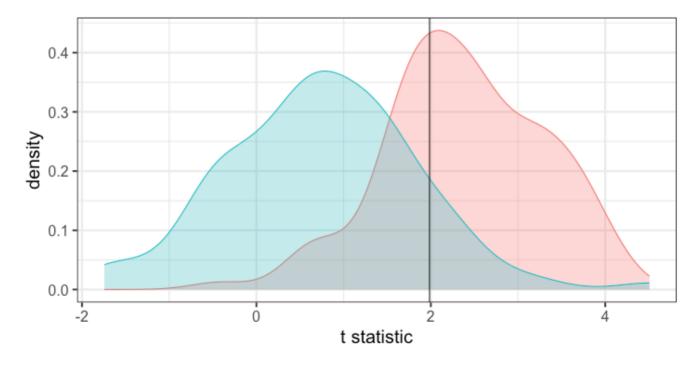


mean(et_xz)

[1] 2.383435

mean(ot_xz)

[1] 0.7411209



```
cv = qt(p = .975, df = 100-3-1)
esig = et_xz > cv
sum(esig)

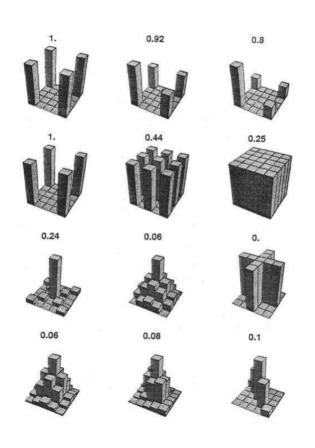
## [1] 66

osig = ot_xz > cv
sum(osig)

## [1] 12
```

In our simulation, 66% of experimental studies were statistically significant, whereas only 12% of observational studies were significant. Remember, we built our simulation based on data where there really is an interaction effect (i.e., the null is false).

Efficiency



Efficiency = the ratio of the variance of X7 (controlling for X and Z) of a design to the best possible design (upper left corner). High efficiency is better; best efficiency is 1.

Efficiency

If the optimal design has N observations, then to have the same power, any other design needs to have N*(1/efficiency).

So a design with .06 efficiency needs $\frac{1}{.06} = 16.67$ times the sample size to detect the effect.

0.06



Efficiency

This particular point has been "rediscovered" as recently as 2018:

- you need 16 times the sample size to detect an interaction as you need for a main effect of the same size.
- This generalizes to higher-order interactions as well. If you have a three-way interaction, you need 16*16 (256 times the number of people).

Observational studies: What NOT to do

Re-code X and Z into more extreme values (e.g., median splits)

 while this increases variance in X and Z, it also increases measurement error

Collect a random sample and then only perform analyses on the sub sample with extreme values

reduces sample size and also generalizability

Observational studies: What NOT to do

What can be done?

M&J suggest oversampling extremes and using weighted and unweighted samples

Experimental studies: What NOT to do

Be mean to field researchers

Forget about lack of external validity and generalizability

Ignore power when comparing interaction between covariate and experimental predictors (ANCOVA or multiple regression with categorical and continuous predictors)

Polynomials

Non-linear relationships

Linear lines often make bad predictions -- very few processes that we study actually have linear relationships. For example, effort had diminishing returns (e.g., log functions), or small advantages early in life can have significant effects on mid-life outcones (e.g., exponentional functions). In cases where the direction of the effect is constant but changing in magnitude, the best way to handle the data is to transform a variable (usually the outcome) and run linear analyses.

Other processes represent changes in the direction of relationship -- a small amount of anxiety is beneficial for performance on some tasks but too much is detrimental. When the shape of the effect includes change(s) in direction, then a **polynomial** term(s) may be more appropriate.

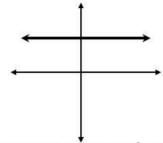
Polynomials are often a poor approx. for a non-linear effect. Correctly testing for non-linear effects usually requires (a) a lot of data and (b) making a number of assumptions about the data. Polynomial regression can be a useful tool for *exploratory* analysis and in cases when data are limited in terms of quantity and/or

Polynomial regression

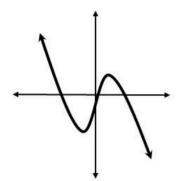
Polynomial regression is most often a form of hierarchical regression that systematically tests a series of higher order functions for a single variable.

$$egin{aligned} \mathbf{Linear:} \ \hat{Y} &= b_0 + b_1 X \ \mathbf{Quadtratic:} \ \hat{Y} &= b_0 + b_1 X + b_2 X^2 \ \mathbf{Cubic:} \ \hat{Y} &= b_0 + b_1 X + b_2 X^2 + b_3 X^3 \end{aligned}$$

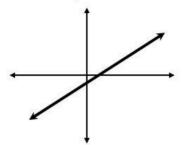
Graphs of Polynomial Functions:



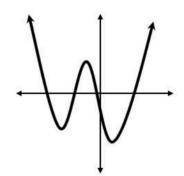
Constant Function (degree = 0)



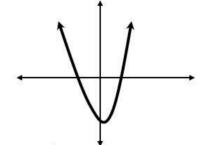
Cubic Function (deg. = 3)



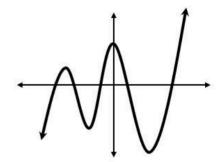
Linear Function (degree = 1)



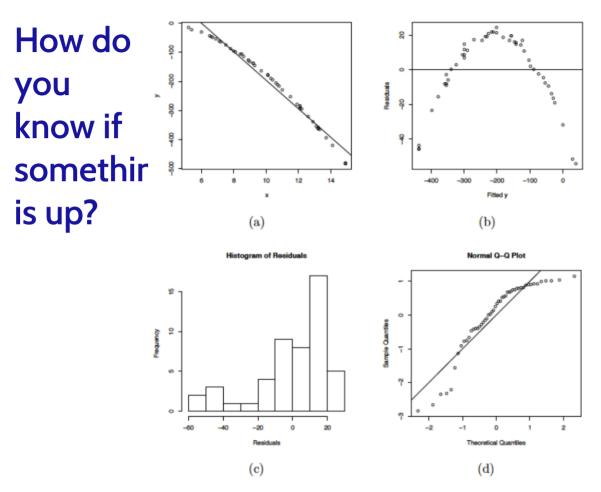
Quartic Function (deg. = 4)



Quadratic Function (degree = 2)



Quintic Function (deg. = 5)



- (a) Scatterplot of the quadratic data with the OLS line. (b) Residual plot for the OLS fit.
- (c) Histogram of the residuals. (d) NPP for the Studentized residuals.

Can a team have too much talent?

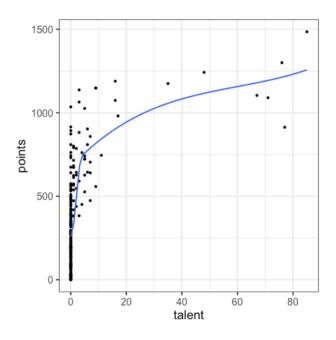
Researchers hypothesized that teams with too many talented players have poor intra-team coordination and perform worse than teams with a moderate amount of talent. They looked at 208 international football teams. Talent was the percentage of players during the 2010 and 2014 World Cup Qualifications phases who also had contracts with elite club teams. Performance was the number of points the team earned during these same qualification phases.

Swaab, R.I., Schaerer, M, Anicich, E.M., Ronay, R., and Galinsky, A.D. (2014). The too-much-talent effect: Team

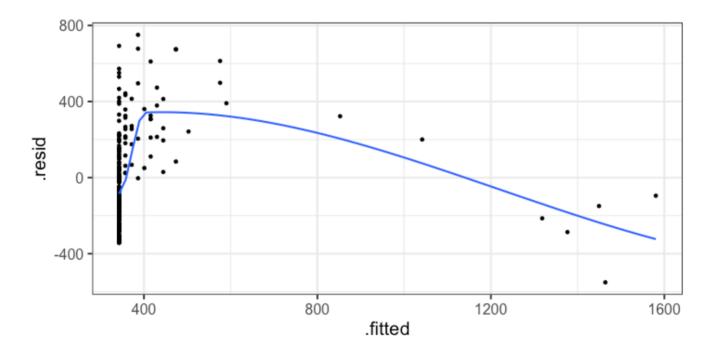
head(football)

```
##
         country points talent
           Spain
## 1
                    1485
                             85
## 2
         Germany
                   1300
                             76
## 3
          Brazil
                   1242
                             48
        Portugal
## 4
                   1189
                             16
## 5
       Argentina
                   1175
                             35
   6 Switzerland
                              9
##
                   1149
```

```
ggplot(football, aes(x = tale
  geom_point() +
  geom_smooth(se = F) +
  theme_bw(base_size = 20)
```



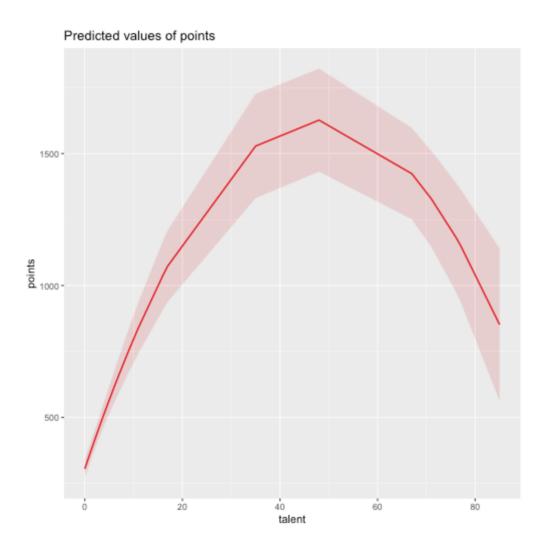
```
mod1 = lm(points ~ talent, data = football)
library(broom)
aug1 = augment(mod1)
ggplot(aug1, aes(x = .fitted, y = .resid)) +
  geom_point() +
  geom_smooth(se = F) +
  theme_bw(base_size = 20)
```



```
mod2 = lm(points ~ talent + I(talent^2), data = football)
summary(mod2)
```

```
##
## Call:
## lm(formula = points ~ talent + I(talent^2), data = football)
##
## Residuals:
      Min
               10 Median 30
##
                                     Max
## -384.66 -193.82 -35.34 152.11 729.66
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 305.34402 17.62668 17.323 < 2e-16 ***
## talent 54.89787 5.46864 10.039 < 2e-16 ***
## I(talent^2) -0.57022 0.07499 -7.604 1.01e-12 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 236.3 on 205 degrees of freedom
## Multiple R-squared: 0.4644, Adjusted R-squared: 0.4592
## F-statistic: 88.87 on 2 and 205 DF, p-value: < 2.2e-16
```

```
library(sjPlot)
plot_model(mod2, type = "pred", terms = "talent")
```



Interpretation

The intercept is the predicted value of Y when X=0

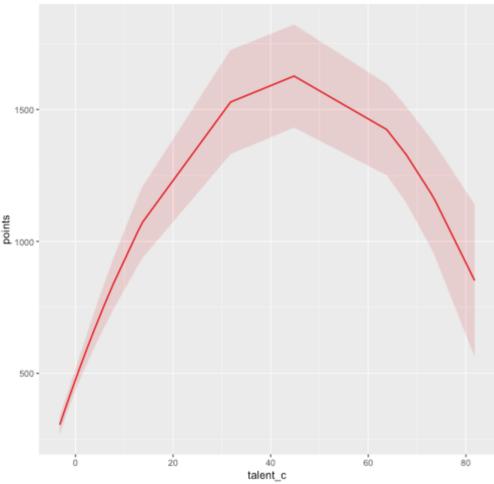
 b_1 coefficient is the *tangent to the curve* when X=0. In other words, this is the rate of change when X is equal to 0. If 0 is not a meaningful value on your X, you may want to center, as this will tell you the rate of change at the mean of X.

```
football$talent_c = football$talent - mean(football$talent)
mod2_c = lm(points ~ talent_c + I(talent_c^2), data = footbal
```

summary(mod2_c)

```
##
## Call:
## lm(formula = points ~ talent_c + I(talent_c^2), data = football)
##
## Residuals:
##
      Min
               10 Median 30
                                     Max
## -384.66 -193.82 -35.34 152.11 729.66
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) 476.01572 19.94656 23.865 < 2e-16 ***
## talent_c 51.22982 5.00212 10.242 < 2e-16 ***
## I(talent c^2) -0.57022 0.07499 -7.604 1.01e-12 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 236.3 on 205 degrees of freedom
## Multiple R-squared: 0.4644, Adjusted R-squared: 0.4592
## F-statistic: 88.87 on 2 and 205 DF, p-value: < 2.2e-16
```

Predicted values of points

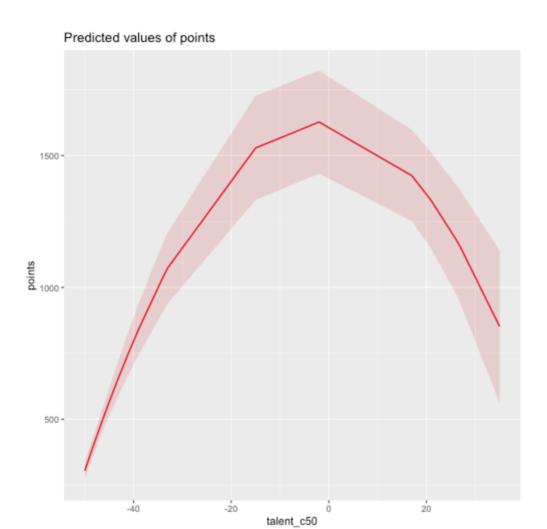


Or you can choose another value to center your predictor on, if there's a value that has a particular meaning or interpretation.

```
football$talent_c50 = football$talent - 50
mod2_50 = lm(points ~ talent_c50 + I(talent_c50^2), data = fo
```

summary(mod2_50)

```
##
## Call:
## lm(formula = points ~ talent_c50 + I(talent_c50^2), data = football)
##
## Residuals:
##
      Min
               10 Median 30
                                    Max
## -384.66 -193.82 -35.34 152.11 729.66
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1624.68872 97.18998 16.717 < 2e-16 ***
## talent c50 -2.12408 2.56568 -0.828 0.409
## I(talent c50^2) -0.57022 0.07499 -7.604 1.01e-12 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 236.3 on 205 degrees of freedom
## Multiple R-squared: 0.4644, Adjusted R-squared: 0.4592
## F-statistic: 88.87 on 2 and 205 DF, p-value: < 2.2e-16
```



Interpretation

The b_2 coefficient indexes the acceleration, which is how much the slope is going to change. More specifically, $2 \times b_2$ is the acceleration: the rate of change in b_1 for a 1-unit change in X.

You can use this to calculate the slope of the tangent line at any value of X you're interested in:

$$b_1 + (2 imes b_2 imes X)$$

tidy(mod2)

At X = 10

At X = 70

Polynomials are interactions

An term for X^2 is a term for $X \times X$ or the multiplication of two independent variables holding the same values.

```
football$talent_2 = football$talent*football$talent
tidy(lm(points ~ talent + talent_2, data = football))
```

Polynomials are interactions

Put another way:

$$\hat{Y}=b_0+b_1X+b_2X^2$$

$$\hat{Y} = b_0 + rac{b_1}{2}X + rac{b_1}{2}X + b_2(X imes X)$$

The interaction term in another model would be interpreted as "how does the slope of X change as I move up in Z?" -- here, we ask "how does the slope of X change as we move up in X?"

When should you use polynomial terms?

You may choose to fit a polynomial term after looking at a scatterplot of the data or looking at residual plots. A U-shaped curve may be indicative that you need to fit a quadratic form -- although, as we discussed before, you may actually be measuring a different kind of non-linear relationship.

Polynomial terms should mostly be dictated by theory -- if you don't have a good reason for thinking there will be a change in sign, then a polynomial is not right for you.

Three-way interactions and beyond

Three-way interactions (regression)

Regression equation

$$\hat{Y} = b_0 + b_1 X + b_2 Z + b_3 W + b_4 X Z + b_5 X W + b_6 Z W + b_7 X Z W$$

The three-way interaction qualifies the three main effects (and any two-way interactions).

Like a two-way interaction, the three-way interaction is a conditional effect. And it is symmetrical, meaning there are several equally correct ways of interpreting it.

How do we describe a 3-way ANOVA?

A two-way (A x B) interaction means that the magnitude of one main effect (e.g., A main effect) depends on levels of the other variable (B). But, it is equally correct to say that the magnitude of the B main effect depends on levels of A. In regression, we refer to these as **conditional effects** and in ANOVA, they are called **simple main effects**.

A three-way interaction means that the magnitude of one two-way interaction (e.g., A x B) **depends** on the levels of the remaining variable (C).

A three-way interaction means that the magnitude of one two-way interaction (e.g., A x B) **depends** on the levels of the remaining variable (C).

It is equally correct to say that the magnitude of the A x C interaction depend on levels of B. Or, that the magnitude of the B x C interaction depends on levels of A. These are known as **simple interaction effects**.

```
psych::describe(stress_data, fast = T)
## Warning in FUN(newX[, i], ...): no non-missing arguments to min; retur
## Warning in FUN(newX[, i], ...): no non-missing arguments to max; retur
##
       vars n mean sd min max range se
           1 150 NaN NA Inf -Inf NA
## gender
## bad_day 2 150 2.95 1.29 1 5
                                      4 0.11
## talk 3 150 2.57 1.20 1 5 4 0.10
## stress 4 150 30.15 10.00 1 51 50 0.82
table(stress_data$gender)
##
## female
         male
##
      67
            83
```

```
mod_stress = lm(stress ~ bad_day*talk*gender, data = stress_d
summary(mod_stress)
```

```
##
## Call:
## lm(formula = stress ~ bad_day * talk * gender, data = stress_data)
##
## Residuals:
##
       Min
                      Median
                 10
                                   30
                                           Max
## -10.6126 -3.2974
                      0.0671
                               3.1129
                                       10.7774
##
## Coefficients:
##
                          Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                           20.3385
                                       4.5181 4.502 1.39e-05 ***
## bad_day
                            2.5273
                                       1.6596 1.523 0.13003
## talk
                                                      0.06227 .
                            2.4870
                                       1.3234 1.879
## gendermale
                           -0.1035
                                       5.7548 - 0.018
                                                      0.98568
## bad_day:talk
                                       0.4564 - 3.116
                           -1.4220
                                                      0.00222 **
## bad_day:gendermale
                           -0.1244
                                       2.0069
                                               -0.062
                                                      0.95067
## talk:gendermale
                                       2.2823 0.867
                                                      0.38718
                           1.9797
## bad_day:talk:gendermale 1.5260
                                       0.7336
                                               2.080
                                                      0.03931 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.733 on 142 degrees of freedom
```

Adjusted R-squared:

Multiple R-squared: 0.7865,

51 / 67

0.776

```
library(reghelper)
simple_slopes(mod_stress)
```

1.661455 1.365903 sstest

2.953333 1.365903 sstest

sstest 3.767431

bad day

##

1

2

21

```
## 3
     4.245211 1.365903 sstest
                                     10.9214
                                                 2.5606 4.2651 142 3.627
## 4
     1.661455 2.566667 sstest
                                     11.2788
                                                 1.4571 7.7406 142 1.687
## 5
     2.953333 2.566667 sstest
                                                 1.0985 14.7274 142 < 2.2
                                     16.1781
                                                 1.6775 12.5647 142 < 2.2
## 6
     4.245211 2.566667 sstest
                                     21.0775
     1.661455 3.767431 sstest
                                     16.7004
                                                        6.9912 142 9.806
## 7
                                                 2.3888
                                                 1.4830 16.1608 142 < 2.2
## 8
     2.953333 3.767431 sstest
                                     23.9670
                                                 2.0578 15.1784 142 < 2.2
## 9
     4.245211 3.767431 sstest
                                     31.2335
## 10 1.661455
               sstest female
                                      0.1245
                                                        0.1724 142 0.863
                                                 0.7221
## 11 2.953333 sstest female
                                                 0.5996 -2.8558 142 0.004
                                     -1.7125
                                                 0.9450 -3.7561 142 0.000
## 12 4.245211 sstest female
                                     -3.5495
## 13
        sstest 1.365903 female
                                      0.5850
                                                 1.0725
                                                        0.5455 142 0.586
       sstest 2.566667 female
                                                 0.6181 -1.8160 142 0.071
                                     -1.1224
## 14
        sstest 3.767431 female
                                                 0.4630 -6.1115 142 9.006
## 15
                                     -2.8299
## 16 1.661455
                 sstest
                          male
                                                 1.0195 4.5510 142 1.137
                                      4.6396
                          male
                                                 0.6463 7.3862 142 1.177
## 17 2.953333
                 sstest
                                      4.7741
                                                 0.9474 5.1813 142 7.418
## 18 4.245211
                sstest
                          male
                                      4.9085
                          male
                                                         5.0533 142 1.315
## 19
        sstest 1.365903
                                      2.5451
                                                 0.5036
                          male
## 20
        sstest 2.566667
                                      2.6700
                                                 0.6116
                                                        4.3655 142 2.427
```

male

talk gender Test Estimate Std. Error t value

5.8571

8.3892

2.7950

1.2025

df

2.3244 142 9 6 9 2 1

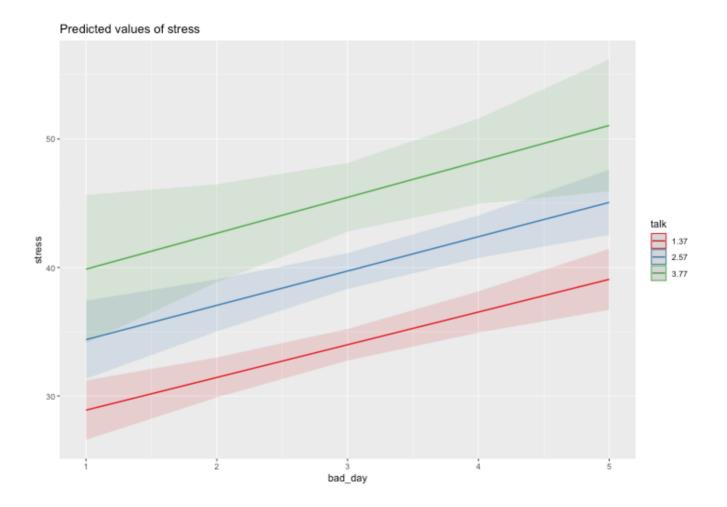
1.7437 3.3590 142 0.001

1.5671 5.3535 142 3.386

Pr(>

plot_model(mod_stress, type = "int", mdrt.values = "meansd")

[[1]]



As a reminder, centering will change all but the highest-order terms in a model.

tidy(mod_stress)

```
## # A tibble: 8 × 5
##
    term
                           estimate std.error statistic
                                                         p.value
    <chr>
                              <dbl>
                                       <dbl>
                                                 <dbl>
                                                           <dbl>
##
                                                4.50
## 1 (Intercept)
                             20.3
                                       4.52
                                                       0.0000139
## 2 bad_day
                                       1.66
                              2.53
                                                1.52 0.130
## 3 talk
                              2.49
                                       1.32
                                                1.88
                                                       0.0623
## 4 gendermale
                             -0.104
                                       5.75
                                               -0.0180 0.986
## 5 bad_day:talk
                             -1.42
                                       0.456
                                               -3.12
                                                       0.00222
## 6 bad_day:gendermale
                                       2.01
                                               -0.0620 0.951
                             -0.124
## 7 talk:gendermale
                             1.98
                                       2.28 0.867
                                                      0.387
## 8 bad_day:talk:gendermale
                              1.53
                                       0.734
                                                2.08
                                                       0.0393
```

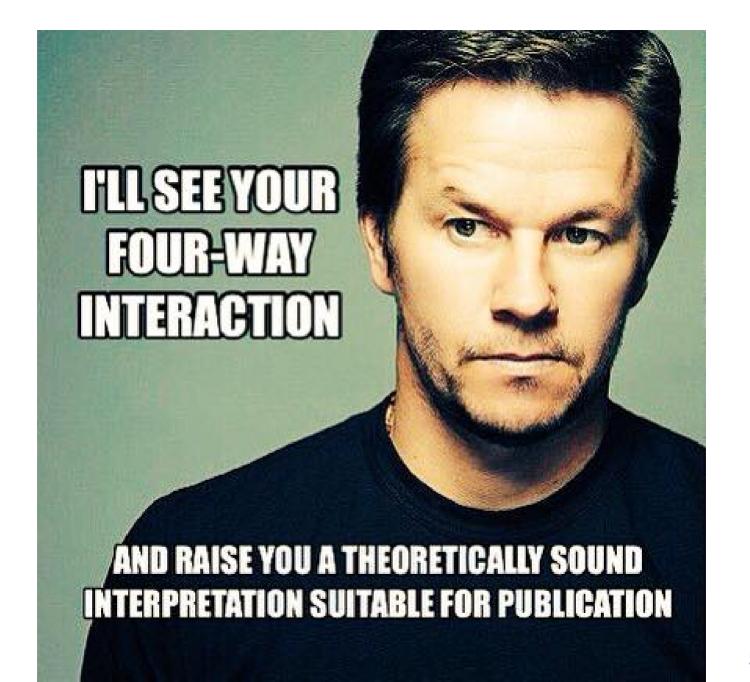
tidy(newmod)

```
## # A tibble: 8 × 5
##
                              estimate std.error statistic
                                                          p.value
    term
  <chr>
                                 <dbl>
                                          <dbl>
                                                    <dbl>
                                                            <dbl>
##
## 1 (Intercept)
                                 23.4
                                          0.845
                                                    27.7 3.89e-59
## 2 bad_day_c
                                          0.618
                                 -1.12
                                                    -1.82 7.15e- 2
## 3 talk c
                                 -1.71
                                          0.600
                                                    -2.86 4.94e- 3
## 4 gendermale
                                 16.2
                                          1.10
                                                    14.7 2.20e-30
## 5 bad_day_c:talk_c
                                 -1.42
                                          0.456
                                                    -3.12 2.22e- 3
## 6 bad_day_c:gendermale
                                  3.79
                                          0.870
                                                    4.36 2.47e- 5
## 7 talk_c:gendermale
                                 6.49
                                          0.882
                                                    7.36 1.38e-11
## 8 bad_day_c:talk_c:gendermale
                                  1.53
                                          0.734
                                                     2.08 3.93e- 2
```

Four-way?

$$\hat{Y} = b_0 + b_1 X + b_2 Z + b_3 W + b_4 Q + b_5 X W \\ + b_6 Z W + b_7 X Z + b_8 Q X + b_9 Q Z + b_{10} Q W \\ + b_{11} X Z Q + b_{12} X Z W + b_{13} X W Q + b_{14} Z W Q \\ + b_{15} X Z W Q$$

3-way (and higher) interactions are incredibly difficult to interpret, in part because they represent incredibly complicated processes. If you have a solid theoretical rationale for conducting a 3-day interaction, be sure you've collected enough subjects to power your test.



Especially with small samples, three-way interactions may be the result of a few outliers skewing a regression line. If you have stumbled upon a three-way interaction during exploratory analyses, **be careful.** This is far more likely to be a result of over-fitting than uncovering a true underlying process.

Use at least one nominal moderator (ideally with only 2 levels), instead of all continuous moderators. This allows you to examine the 2-way interaction at each level of the nominal moderator, esp if one moderator is experimenter manipulated, which increases the likelihood of balanced conditions.

Next time...

Questions about tested material & HW assistance

April 2nd = Exam 2!!!!!!!!!

(everything after this slide is extra or codebased; feel free to play around, but you won't be tested on it)

```
library(car)
fit = lm(Time~Speed*Noise, data = Data)
summary(aov(fit))
##
              Df Sum Sq Mean Sq F value Pr(>F)
## Speed 2 2805871 1402936 109.397 < 2e-16 ***
## Noise
         2 341315 170658 13.307 4.25e-06 ***
## Speed: Noise 4 295720 73930 5.765 0.000224 ***
## Residuals 171 2192939 12824
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(fit, type = 2)
## Anova Table (Type II tests)
##
## Response: Time
##
              Sum Sq Df F value Pr(>F)
## Speed 2805871 2 109.3975 < 2.2e-16 ***
## Noise
        341315 2 13.3075 4.252e-06 ***
## Speed:Noise 295720 4 5.7649 0.0002241 ***
## Residuals 2192939 171
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1 61/67
```

```
fit = lm(Time~Speed*Noise, data = Data)
summarv(fit)
##
## Call:
## lm(formula = Time ~ Speed * Noise, data = Data)
##
  Residuals:
##
      Min
               10 Median
                               30
                                      Max
## -316.23 -70.82
                     4.99
                            79.87
                                   244.40
##
## Coefficients:
##
                                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                    630.72
                                                       24.908 < 2e-16 *
                                                25.32
## SpeedMedium
                                                       -2.944 0.00369 *
                                   -105.44
                                                35.81
## SpeedFast
                                                       -8.418 1.49e-14 *
                                   -301.45
                                                35.81
## NoiseControllable
                                    -54.05
                                                35.81
                                                       -1.509 0.13305
## NoiseUncontrollable
                                    -36.28
                                                       -1.013
                                                35.81
                                                              0.31243
## SpeedMedium:NoiseControllable
                                     21.48
                                                50.64 0.424
                                                               0.67201
## SpeedFast:NoiseControllable
                                     12.01
                                                50.64 0.237
                                                              0.81287
## SpeedMedium:NoiseUncontrollable
                                   -184.39
                                                50.64
                                                       -3.641
                                                               0.00036 *
## SpeedFast:NoiseUncontrollable
                                    -24.84
                                                50.64
                                                       -0.490
                                                               0.62448
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 113.2 on 171 degrees of freedom

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##

```
library(emmeans)
fit.grid = ref_grid(fit)
pairs(fit.grid, adjust = "holm")
                                                 estimate SE df t.ratio
##
    contrast
    Slow None - Medium None
                                                     105.4 35.8 171
##
##
    Slow None - Fast None
                                                    301.4 35.8 171
    Slow None - Slow Controllable
                                                      54.1 35.8 171
##
    Slow None - Medium Controllable
##
                                                    138.0 35.8 171
    Slow None - Fast Controllable
                                                    343.5 35.8 171
##
    Slow None - Slow Uncontrollable
                                                      36.3 35.8 171
##
##
    Slow None - Medium Uncontrollable
                                                    326.1 35.8 171
    Slow None - Fast Uncontrollable
##
                                                    362.6 35.8 171
    Medium None - Fast None
                                                    196.0 35.8 171
##
    Medium None - Slow Controllable
##
                                                    -51.4 35.8 171
    Medium None - Medium Controllable
##
                                                      32.6 35.8 171
##
    Medium None - Fast Controllable
                                                    238.1 35.8 171
```

Medium None - Slow Uncontrollable

Medium None - Fast Uncontrollable

Fast None - Slow Controllable

Fast None - Fast Controllable

Fast None - Medium Controllable

Fast None - Slow Uncontrollable

Fast None - Fast Uncontrollable

Fast None - Medium Uncontrollable

Medium None - Medium Uncontrollable

##

##

##

##

##

##

##

2.944

8.418

1.509

3.854

9.592

1.013

9.106

10.124

5.473

-1.435

0.910

6.648

6.162

7.180

-6.908

-4.564

-7.405

1.174

1.707

-1.931

-69.2 35.8 171

220.7 35.8 171

257.1 35.8 171

-247.4 35.8 171

-163.4 35.8 171

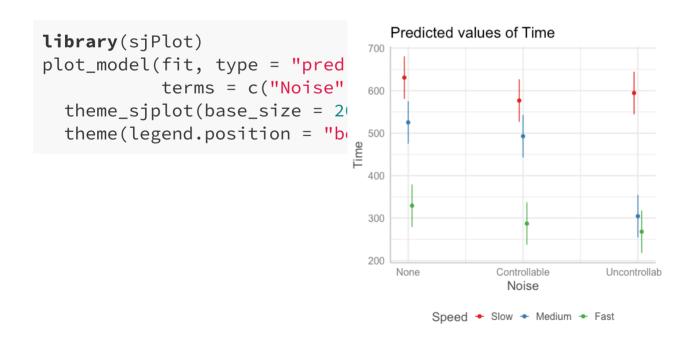
-265.2 35.8 171

42.0 35.8 171

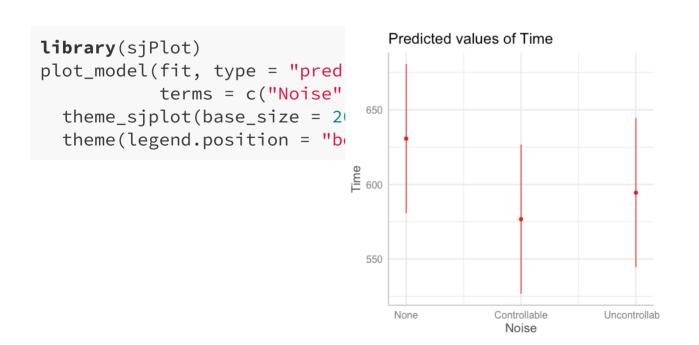
61.1 35.8 171

24.7 35.8 171 63 9 6 9 8 9

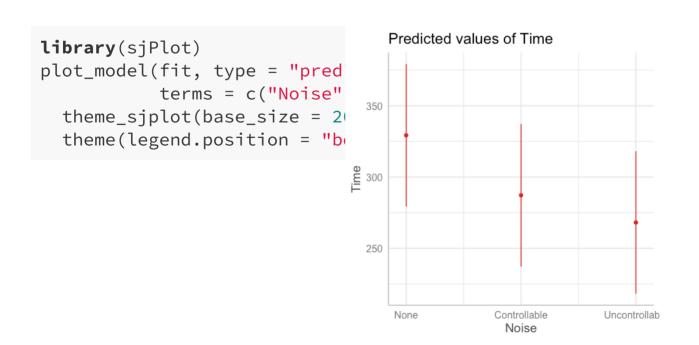
In sjPlot(), predicted values are the expected value of Y given all possible values of X, at specific values of M. If you don't give it all of M, it will choose every possible value.



In sjPlot(), predicted values are the expected value of Y given all possible values of X, at specific values of M. If you don't specify levels of M, it will choose the lowest possible value.



In sjPlot(), predicted values are the expected value of Y given all possible values of X, at specific values of M. If you don't specify levels of M, it will choose the lowest possible value.



In sjPlot(), estimated marginal means are the expected value of Y given all possible values of X, **ignoring M**.

