

Learning User-Specific Latent Influence and Susceptibility from Information Cascades

Yongqing Wang*, **Huawei Shen[†]**, **Shenghua Liu[†]** and **Xueqi Cheng[†]**

CAS Key Laboratory of Network Data Science and Technology,

Institute of Computing Technology, Chinese Academy of Sciences, Beijing 100190, China

*wangyongqing@software.ict.ac.cn, †{shenhuawei,liushenghua,cxq}@ict.ac.cn

Abstract

Predicting cascade dynamics has important implications for understanding information propagation and launching viral marketing. Previous works mainly adopt a pair-wise manner, modeling the propagation probability between pairs of users using n^2 independent parameters for n users. Consequently, these models suffer from severe overfitting problem, especially for pairs of users without direct interactions, limiting their prediction accuracy. Here we propose to model the cascade dynamics by learning two low-dimensional user-specific vectors from observed cascades, capturing their influence and susceptibility respectively. This model requires much less parameters and thus could combat overfitting problem. Moreover, this model could naturally model context-dependent factors like cumulative effect in information propagation. Extensive experiments on synthetic dataset and a large-scale microblogging dataset demonstrate that this model outperforms the existing pair-wise models at predicting cascade dynamics, cascade size, and “who will be retweeted”.

Introduction

Social media is revolutionizing the dissemination of information via its great ease in information delivery, accessing and filtering. In social media, users could post original messages or forward messages that they see from other users. Information propagation proceeds along social relationships between users, explicit or implicit, forming cascade dynamics. Modeling and predicting the cascade dynamics has important implications to understanding information propagation and launching viral marketing in social media. The key for this problem is inferring the interpersonal influence between users or estimating the probability that information propagates between them, fundamental to influence maximization (Kempe, Kleinberg, and Tardos 2003; Chen, Wang, and Yang 2009; Cheng et al. 2013), social recommendation (Huang et al. 2012; Ma, King, and Lyu 2009), and viral marketing (Richardson and Domingos 2002; Leskovec, Adamic, and Huberman 2007).

Existing studies mainly aim to determine the propagation probability of information between all pairs of users, based on structure of social network, the record of information cascade, and demographic/content characteristics of

users. Kempe et al. (Kempe, Kleinberg, and Tardos 2003) implemented the independent cascade model for information propagation, assuming a uniform propagation probability or a degree-modulated propagation probability. Goyal et al. (Goyal, Bonchi, and Lakshmanan 2010) provided two static models in terms of Bernoulli distribution and Jaccard index, and learned temporal factors to maximize likelihood of cascades. Saito et al. (Saito, Nakano, and Kimura 2008) learned the propagation probability for independent cascade model in terms of expectation maximization of cascades. Artzi et al. (Artzi, Pantel, and Gamon 2012) estimated the propagation probability by exploiting demographic and content characteristics. These methods all adopt a pair-wise manner, modeling the propagation probability between pairs of users using n^2 independent parameters for n users. Consequently, these models suffer from severe overfitting problem, limiting their prediction accuracy. For example, for a pair of users without observed interactions, these methods take the propagation probability between them as zero, indicating that it is never happened to propagate information between the two users in the future. To the best of our knowledge, we lack a model that could concisely model the interpersonal influence and accurately predict the cascade dynamics in large-scale social networks.

In this paper, we propose to model the cascade dynamics by learning two low-dimensional latent vectors for each user from observed cascades, capturing her influence and susceptibility respectively. In this latent influence and susceptibility (LIS) model, the propagation probability that one user forwards a piece of information is determined by the product of her activated neighbors’ influence vectors and her own susceptibility vector. The benefits of this model are three-fold: (1) It directly models user-specific influence and susceptibility, instead of the interpersonal influence between all pairs of users. Thus it requires much less parameters, and pairs of users are no longer independent, effectively combating the overfitting problem for pairs of users without direct interactions; (2) It could naturally capture context-dependent factors like cumulative effect in information propagation. For a target user, context means her previous exposures to the same message. In this model, one user’s previous exposures to a message improve the probability that she propagates the message, flexibly combining the benefits of both cascade model and threshold model; (3) It is applicable to scenar-

ios with explicit or implicit social networks, since it learns user-specific influence and susceptibility from the observed information cascades rather than the underlying social networks like many existing methods.

We evaluate the proposed LIS model by extensive experiments on synthetic dataset and a large-scale microblogging dataset from Sina Weibo, the largest social media in China. Compared with several widely-used methods that work in pair-wise manner, LIS model consistently outperforms them at predicting the dynamics of cascades. Moreover, the learned user-specific influence and susceptibility vectors provide us a quantitative way to understand topic-related interpersonal influence in information propagation.

Problem formulation

In this paper, we focus on the problem of inferring users' influence and susceptibility from detailed records of message cascades. Before diving into the details of the proposed model, we first clarify the two main motivations underlying our model.

First, existing models suffer from severe overfitting problem, especially for the pair of users without direct interactions. As shown in Fig. 1(a), when messages are forwarded by users along social links among them, not all social links matter in these message cascades. For example, no forwarding behavior occurs between users u_1 and u_4 , although they have direct social link. In this case, existing models take the propagation probability between them as zero, implying that it is never happened to propagate information between the two users in the future. This overfitting problem is actually caused by the hypothesis of existing models: *interpersonal influence between different pairs of users is independent of each other*. This motivates us to adopt a user-specific manner for modeling interpersonal influence among users, whose existence has been proved in (Aral and Walker 2012; Aral, Muchnik, and Sundararajan 2009). Specifically, each user u is modeled by two non-negative d -dimensional vectors: an influence vector I_u and a susceptibility vector S_u , characterizing the influence and susceptibility of user u over d latent topics. For a pair of user (u, v) , the interpersonal influence of u on v could be simply computed by the scalar product of I_u and S_v . This concise representation requires only $2nd$ ($\ll n^2$) parameters for n users.

Second, the role of context in information propagation is rarely captured. Existing models mostly assume that users are *memoryless*, i.e., whether a user forwards one message is not affected by her previous exposures to the message. Indeed, this assumption is not supported by empirical observations from real cascades of messages. Fig. 1(b) depicts the relationship between the number of times k that one user is exposed to a message and the probability that the user will forward the message when she is exposed to the message for the k -th time. As the number of exposures increases, the forwarding probability increases accordingly: from 0.008 when the number of exposures is 1 to 0.261 when the number of exposures is 5. This observation clearly demonstrates that cumulative effect does exist in information propagation, an effect also observed in many other scenarios (Bao et al.

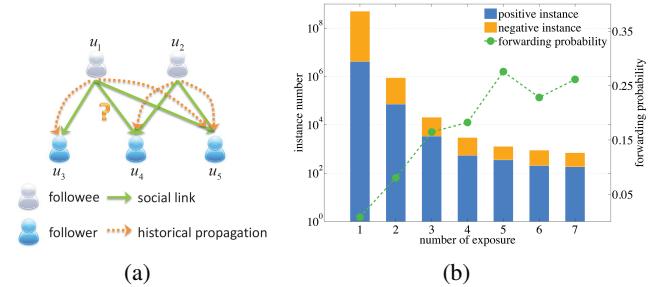


Figure 1: Motivations underlying our model. (a) Example of cascades to illustrate the overfitting problem suffered by pair-wise models; (b) Relationship between forwarding probability and number of exposures (observed from Sina Weibo, Jan. 1-15, 2011).

2013a; Leskovec, Adamic, and Huberman 2007). This motivates us to adopt a context-dependent way to model the cumulative effect.

Given a message m , we denote its cascade C^m with a chronological list of activated users (a_1^m, \dots, a_N^m) , where users are ranked in the ascending order of the time they forward the message m . Whenever one user is activated (i.e., she posts or forwards the message), she has one chance to attempt to activate other users. Whether her attempt succeeds depends on the *cascade context* at that time.

Cascade context: When one user a_i^m ($i = 1, \dots, N$) becomes activated and she attempts to activate a user v , the cascade context for this attempt is defined as

$$D_{v,i}^m = \{a_j^m | j \leq i, \delta(a_j^m, v) = 1\}, \quad (1)$$

where the indicator function $\delta(u, v)$ means whether v could be exposed to the message from u . In other words, cascade context means v 's previous exposures to the message from other users.

In practice, it is difficult to exactly determine $\delta(u, v)$ since there is no reliable mechanism to know whether user v is exposed to a message forwarded by user u , even when direct social link exists between them. In this paper, we circumvent this problem using a delegate of the function δ , i.e., the aggregate diffusion network of historical cascades of messages. Detailed discussions about diffusion network are given in experiments on real dataset. Diffusion network characterizes the actual flow of information between users in the past, providing us a good approximation for potential information propagation in the future. More importantly, diffusion network is always embedded in the collection of message cascades while social network is not explicitly available in many scenarios. Therefore, the proposed model is generally applicable to the scenarios with or without explicit social network.

With the above notations, we now model cascade dynamics of messages. For a message m with the cascade (a_1^m, \dots, a_N^m) , each user could be denoted by an N -dimensional status vector \mathbf{z}_v^m , with its element $z_{v,j}^m$ indicating whether the user v is in activated status right after she is exposed to the message m from user a_j^m . If user v becomes activated when she is exposed to the message m from

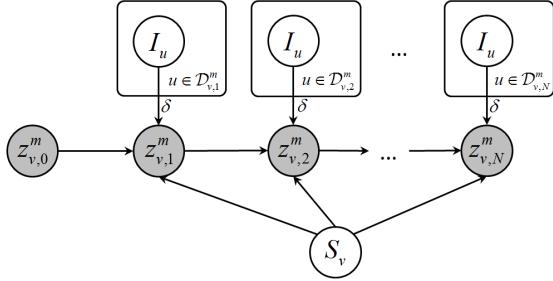


Figure 2: Graphical representation of the proposed model.

user a_j^m , we have $z_{v,i}^m = 0$ ($1 \leq i < j$) and $z_{v,i}^m = 1$ ($j \leq i \leq N$). If v keeps inactivated during the cascade dynamics of message m , $z_{v,i}^m = 0$ for any i .

The likelihood of \mathbf{z}_v^m is written as

$$P(\mathbf{z}_v^m | \delta) = p(z_{v,0}^m) \prod_{i=1}^N p(z_{v,i}^m | z_{v,i-1}^m, \mathcal{D}_{v,i}^m, \delta), \quad (2)$$

where $z_{v,0}^m$ is introduced only for simplifying the notation. Here the first term depicts whether v is the source of message m , defined as

$$p(z_{v,0}^m = 1) = \begin{cases} 1, & v \text{ is the source} \\ 0, & \text{otherwise} \end{cases}. \quad (3)$$

The second term characterizes the transition of user's status, formally defined as

$$\begin{aligned} p(z_{v,i}^m = 1 | z_{v,i-1}^m = 1, \mathcal{D}_{v,i}^m, \delta) &= 1, \\ p(z_{v,i}^m = 1 | z_{v,i-1}^m = 0, \mathcal{D}_{v,i}^m, \delta) &= \\ 1 - \exp(-\lambda \delta(a_i^m, v) \sum_{u \in \mathcal{D}_{v,i}^m} I_u^T S_v), \\ p(z_{v,i}^m = 0 | z_{v,i-1}^m = 0, \mathcal{D}_{v,i}^m, \delta) &= \\ 1 - p(z_{v,i}^m = 1 | z_{v,i-1}^m = 0, \mathcal{D}_{v,i}^m, \delta), \end{aligned} \quad (4)$$

where λ is a scaling factor, modulating the effect of cascade context. The first equation implies that a user cannot become inactivated as long as she is activated. The other two equations model how the transition probability is influenced by cascade context, reflected by a cumulative manner of interpersonal influence. The factor $\delta(a_i^m, v)$ determines whether the user v could be exposed to the message m from user a_i^m . For clarity, we give a graphical model representation in Fig. 2 to illustrate the process that user v 's status changes with the dynamics of message m .

Assuming independent cascades, the likelihood of all cascades \mathbf{C} is a product of the likelihoods given by Eq. (2)

$$L(\mathbf{C}) = \prod_{m=1}^{|\mathbf{C}|} \prod_{v \in V} P(\mathbf{z}_v^m | \delta). \quad (5)$$

The parameters of the model are learned by minimizing the negative logarithmic likelihood, namely loss function, of all the collection of cascades as the following objective function

$$\mathcal{L}(\mathbf{C}) = - \sum_{m=1}^{|\mathbf{C}|} \sum_{v \in V} \sum_{i=1}^N \log p(z_{v,i}^m | z_{v,i-1}^m, \mathcal{D}_{v,i}^m, \delta). \quad (6)$$

Algorithm 1 Parameter estimation

Input: Collection of cascades observed in a given time period, the maximum epoch M , and regularization parameters γ_I and γ_S

Output: User-specific influence and susceptibility I, S

Construct diffusion network δ from cascades
Initialize parameters with random values, including I, S
repeat
 for $i = 1$ to n **do**
 Calculate gradients $\partial \hat{\mathcal{L}} / \partial I_u$ and $\partial \hat{\mathcal{L}} / \partial S_v$
 end for
 Update I and S with PG method
until maximum epoch M is reached or gradients vanish

Note that $p(z_{v,0}^m)$ is always 1, hence omitted in Eq. (6).

Parameter estimation

In this section, we develop algorithm to estimate the parameters of the proposed model. Generally speaking, parameter estimation could be completed via directly minimizing Eq. (6) with respect to I and S . However, the huge number of possible configurations of cascade contexts in Eq. (6) results in high computational cost. Indeed, *one* cascade context could repeatedly occur in many cascades, causing huge duplicated computation of Eq. (4).

Here we propose to reduce the duplicated computation by taking advantage of overlapped cascade contexts among multiple cascades. Firstly, we introduce some symbols to simplify the optimization. Let $\mathcal{P}(v)$ be the set of possible configurations of cascade contexts pertaining to v , occurred in all cascades. For example, as shown in Fig. 1(a), $\{u_1\}$, $\{u_2\}$ and $\{u_1, u_2\}$ are all the cascade contexts for user u_5 . We group cascade contexts in terms of users and re-organize the logarithmic likelihood in Eq. (6) as

$$\mathcal{L}(\mathbf{C}) = - \sum_{v \in V} \sum_{\substack{\mathcal{D}_{v,i} \in \\ \mathcal{P}(v)}} (n_{z_{v,i}, \mathcal{D}_{v,i}} \log p(z_{v,i} | z_{v,i-1}, \mathcal{D}_{v,i}, \delta)), \quad (7)$$

where $\mathcal{D}_{v,i}$ refers to one configuration of cascade context for user v , independent of specific cascade, and $n_{z_{v,i}, \mathcal{D}_{v,i}}$ counts the frequency of the configuration $\mathcal{D}_{v,i}$ emerged in all cascades, relative to user v 's status $z_{v,i}$.

Parameters estimated by directly minimizing the logarithmic likelihood in Eq. (7) may suffer from overfitting problem, a common problem in likelihood maximization estimation. To combat this problem, we regularize the parameter vectors I and S and obtain the final objective function for parameter estimation

$$\begin{aligned} \hat{\mathcal{L}}(\mathbf{C}) &= - \sum_{v \in V} \sum_{\substack{\mathcal{D}_{v,i} \in \\ \mathcal{P}(v)}} (n_{z_{v,i}, \mathcal{D}_{v,i}} \log p(z_{v,i} | z_{v,i-1}, \mathcal{D}_{v,i}, \delta)) \\ &\quad + \gamma_I \|I\|_F^2 + \gamma_S \|S\|_F^2, \\ \text{s.t. } I_{ij} &\geq 0, S_{ij} \geq 0, \forall i, j, \end{aligned} \quad (8)$$

where γ_I and γ_S are regularization parameters, and $\|\cdot\|_F$ is Frobenius norm.

Finally, using *Projected Gradient* (PG) method (Lin 2007), we develop an iterative algorithm for parameter estimation, leveraging the gradients with respect to I and S

as

$$\begin{aligned} \frac{\partial \hat{\mathcal{L}}}{\partial I_u} &= -\lambda \sum_{v \in V} S_v \sum_{\substack{\mathcal{D}_{v,i} \in \\ \mathcal{P}(v)}} \mathcal{I}_{u \in \mathcal{D}_{v,i}} \left(n_{z_{v,i}=1, \mathcal{D}_{v,i}} \frac{1 - p_{v,\mathcal{D}_{v,i}}}{p_{v,\mathcal{D}_{v,i}}} \right. \\ &\quad \left. - n_{z_{v,i}=0, \mathcal{D}_i(v)} \right) + \gamma_I I_u, \quad (9) \\ \frac{\partial \hat{\mathcal{L}}}{\partial S_v} &= -\lambda \sum_{\substack{\mathcal{D}_{v,i} \in \\ \mathcal{P}(v)}} \sum_{u \in \mathcal{D}_{v,i}} I_u \left(n_{z_{v,u}=1, \mathcal{D}_{v,u}} \frac{1 - p_{v,\mathcal{D}_{v,u}}}{p_{v,\mathcal{D}_{v,u}}} \right. \\ &\quad \left. - n_{z_{v,u}=0, \mathcal{D}_{v,u}} \right) + \gamma_S S_v, \end{aligned}$$

where \mathcal{I} is an indicator function, and $p_{v,\mathcal{D}_{v,i}}$ is a concise form of $p(z_{v,i}=1|z_{v,i-1}, \mathcal{D}_{v,i}, \delta)$. The algorithm for parameter estimation is described in Algorithm 1.

Experiments

We evaluate LIS model on both synthetic data and real world data, i.e. microblogging data from Sina Weibo. Here we only choose scalable modeling methods as baselines, i.e., expectation maximization estimation (EM) (Saito, Nakano, and Kimura 2008), static Bernoulli model (SB), and static Jaccard model (SJ) (Goyal, Bonchi, and Lakshmanan 2010). To reduce the overfitting problem suffered from these models, we apply *matrix factorization* (MF) method (Salakhutdinov and Mnih 2008) as a post-processing improvement, forming a stronger baseline. We demonstrate the benefit of the LIS model at predicting the cascade dynamics, cascade size, and “who will be retweeted”. Finally, we analyze the topics associated with the learned user-specific latent influence and susceptibility.

Experiments on synthetic data

To validate whether the proposed algorithm could obtain good estimation of user-specific influence and susceptibility, we first conduct tests on synthetic data, where cascades are generated according to parameters known a prior. These tests also offer us some intuitions about difficulties at predicting cascade dynamics.

Experimental setup. We first generate two synthetic diffusion networks: one is constructed using Barabási-Albert (BA) model (Barabási and Albert 1999), denoted as original network; the other is generated by shuffling the original network (Molloy and Reed 1995), denoted as shuffle network. We set the dimensionality of user’s influence I_u and susceptibility S_u as 5, and sample I_u and S_u from $f(\mathbf{x}) = 1/2\sqrt{\mathbf{x}}, \mathbf{x} \sim U(0, 1)^5$, where $U(0, 1)$ refers to a uniform distribution. We then generate cascades over the two networks according to our LIS model with $\lambda = 0.01$. We take 80% of the cascades generated from original network as training dataset, and the rest of cascades generated from the original network and the cascades from the shuffle network as test dataset. The two test datasets have equal size, offering a fair comparison.

Predicting cascade dynamics. We deal with this problem as a set of binary classification problem, predicting whether one user will be activated under specific cascade context. Thus we use AUC (the area of under the ROC curve) as

Table 1: Cascade dynamics prediction on synthetic data

network	UB	LIS	SB	SJ	EM
original	0.659	0.654	0.607	0.618	0.561
shuffle	0.659	0.608	0.509	0.525	0.507

Table 2: Dataset statistics

	training data		test data	
	cascades	period	cascades	period
D1	395,852	01/01-01/15	T1	160,868
D2	453,356	01/16-01/31	T2	122,509
D3	386,152	02/01-02/15	T3	145,143
				01/16-01/31
				02/01-02/05
				02/16-02/20

the evaluation metric (Fawcett 2006). As a reference for the performance comparison, we offer an upper bound of our LIS model (denoted as UB): predicting cascade dynamics according to the parameters I and S that are used to generate cascades in test data.

Results are listed in Table 1. It is seen that LIS model consistently outperforms baselines, and its AUC value is very close to UB, when predicting on original network. Particularly, the performance of LIS model is stable on both original and shuffle networks, while baseline methods suffer from much performance reduction (some even close to 0.5, equal to random guess approach), resulted from the overfitting problem of pair-wise models.

Experiments on Microblog

Dataset. The Microblog data from Sina Weibo website is published by WISE 2012 Challenge¹, spanning from January 1, 2011 to February 15, 2011. We extract the cascade records posted between January 1, 2011 and February 15, 2011, and split the extracted records into three training datasets, i.e., D1, D2, D3, each persisting a period of half a month. Furthermore, for each training dataset, we extract the cascade records in the following 5 days as test, i.e., T1, T2 and T3. We only consider the users who appear in all the three training datasets, obtaining 199,408 users. Dataset statistics are depicted in Table 2. We conduct an empirical study to demonstrate the severity of overfitting problem. Over 70% of *forwarding traces*—historical paths for information flows—in test data are never observed in training data, posing a big challenge to previous pair-wise models, when applied in real data.

Diffusion network. Exact diffusion network is hard to obtain, since there is no clear clues indicating whether a user is exposed to a message forwarded by her followee. Previous works focus on directly inferring diffusion networks, which is not applicable to large-scale scenarios (Gomez-Rodriguez, Leskovec, and Krause 2010; Gomez-Rodriguez, Leskovec, and Schölkopf 2013; Du et al. 2012; Kurashima et al. 2014). Here we estimate diffusion network according to a large collection of historical cascades: one cascade has a collection of forwarding traces over the period of observation, forming a directed graph. We aggregate these graphs of all cascades into a diffusion network, providing us a good approximation for potential information propagation in the

¹<http://www.wise2012.cs.ucy.ac.cy/challenge.html>

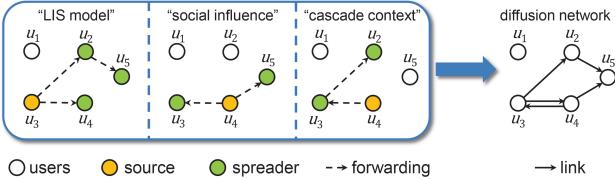


Figure 3: Illustration of constructing diffusion network. The left box contains three observed cascades, and the right is their aggregated diffusion network.

future. Figure 3 gives an example to illustrate the construction of diffusion network.

Predicting cascade dynamics. We introduce the length of cascade context l to capture user’s context-dependent level for exploring context-dependent factors like cumulative effects in information propagation. When a user decides whether or not to forward a message, only the recent l exposures take effects in cascade context. The case $l = 0$ implies that users are memoryless, i.e., without cumulative effect, reproducing the independent assumption (Kempe, Kleinberg, and Tardos 2003). To illustrate the difference of prediction performance at combating overfitting problem, we additionally evaluate the prediction only over observed forwarding traces. The experimental results are presented in Fig. 4. Despite that baselines can better handle prediction instances over observed forwarding traces, the AUCs decrease dramatically when applied to the prediction over all forwarding traces in test data. It means that pair-wise models, even with an improvement using matrix factorization, still suffer from overfitting problem when a large proportion of forwarding traces in test data are unobserved. LIS model shows stable performance, indicating that it works consistently better than baseline models, no matter whether the forwarding traces are happened in history. Furthermore, we explore the effects of different length of cascade context l in LIS model. With different settings of l , LIS model performs better as the increase of l , shown in both two types of AUCs. It agrees with the empirical observation on cumulative effect of information propagation (Ugander et al. 2012; Bao et al. 2013a; Leskovec, Adamic, and Huberman 2007), and LIS model can effectively capture the effects.

Cascade size prediction. Cascade size prediction, as a key part of influence maximization and viral marketing, is one of the most important applications based on modeling cascade dynamics (Bao et al. 2013b; Shen et al. 2014). To guarantee that all cascades propagate sufficiently from their message sources, we only choose such cascades that are initially posted at the first day in each test data for cascade size prediction. Starting from the true sources of cascades in training dataset, we simulate cascade dynamics using the learned LIS model as a prediction. We group simulated cascades into bins according to their cascade size. By counting the number of cascades in each bin, we get a vector of counts indexed by cascade sizes. In the same way, we also get the vector of counts from the real cascades in test data as the ground truth, and we smooth out those size bins containing few cascades for statistical significance. Thus the cascade

Table 4: Accuracies and MRRs of prediction of “who will be retweeted”

	LIS ($l = 5$)	SB	SJ	EM
Acc(%)	T1	58.48	57.02	49.99
	T2	57.61	55.05	49.65
	T3	59.58	55.38	50.85
MRR	T1	0.791	0.784	0.748
	T2	0.786	0.773	0.745
	T3	0.797	0.775	0.752
				0.775

size prediction can be evaluated by *mean absolute percentage error* (MAPE), where a smaller value indicates a better prediction. Since the cascades are generated by simulations, we repeat the prediction, recording the average values and standard deviations of MAPE in Table 3. It is seen that all LIS models with different settings of l achieve better MAPE values than baselines on test data, indicating LIS model can estimate completed cascades propagation more efficiently than pair-wise models. Particularly, the MAPEs in test data T2 are much larger than the values in the other two test data. One possible explanation is that these cascades in test data T2 span Chinese New Year (from Jan. 2 to Jan. 8, 2011) when users were dominated by offline social activities. Thus, it is hardly to observe completed cascades in the short period, resulting in unexpected performance by simulating complete cascades without accounting these factors.

Prediction of “who will be retweeted”. The problem “who will be retweeted” is a way to examine interpersonal influence under quantitative understanding. In the scene of multi-exposures, high interpersonal influence will have high probability to be forwarded. LIS model provides a direct quantitative metric for interpersonal influence by the scalar product of I_i and S_j between user i and j . Propagation probability is another metric of interpersonal influence for traditional pair-wise models. We therefore deal with the prediction task as a ranking problem of interpersonal influence. The user with higher rank is more probable to be retweeted. We evaluate the prediction performance by metrics of average *Accuracy* (Acc) of top-1 prediction and *Mean Reciprocal Rank* (MRR) (Voorhees 1999). The larger values of Acc and MRR indicate better predictions. The results are given in Table 4. It is seen that LIS model achieves a much better Acc and MRR than the baselines, which indicates that LIS model provides a more efficient perspective to inspect interpersonal influence in information cascades.

Topic allocation in latent features To explore topic allocation in LIS model, we select top 10,000 users for each dimension of latent influence and susceptibility features, according to their influence and susceptibility respectively. We use hashtags as the topic of these messages posted by the selected users. Messages without hashtags are discarded. We keep 8 hashtags with statistical significance in terms of message number. Then we calculate the distribution of each remained hashtags in latent features according to the frequency used by users. Next, we rank hashtags by the results of distribution in latent features and utilize kendall- τ rank correlation coefficient (Kendall 1938) to analyze the difference between pairs of features. Figure 5 shows the heat map

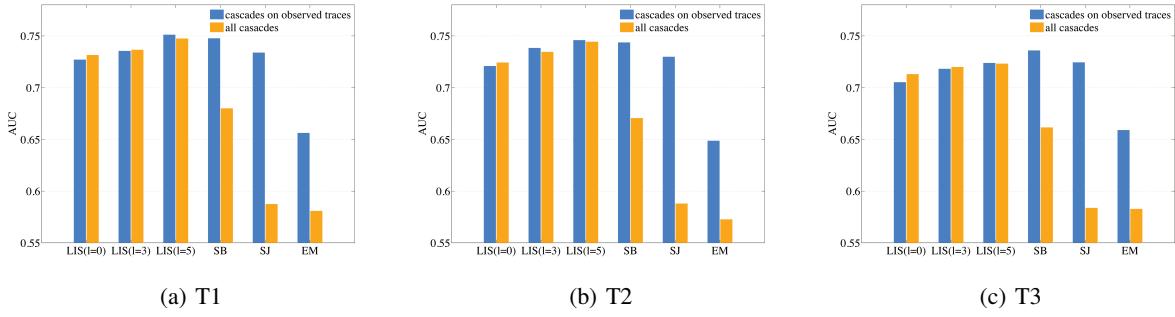


Figure 4: AUCs of cascade dynamics prediction on microblog.

Table 3: MAPEs of cascade size prediction

	LIS ($l = 0$)	LIS ($l = 3$)	LIS ($l = 5$)	SB	SJ	EM
T1	0.163 ± 0.0133	0.140 ± 0.0155	0.141 ± 0.0217	0.191 ± 0.0190	0.524 ± 0.0046	0.258 ± 0.0160
T2	0.287 ± 0.0093	0.280 ± 0.0080	0.286 ± 0.0065	0.333 ± 0.0099	0.621 ± 0.0048	0.338 ± 0.0387
T3	0.095 ± 0.0150	0.094 ± 0.0150	0.097 ± 0.0093	0.171 ± 0.0388	0.505 ± 0.0450	0.189 ± 0.0112

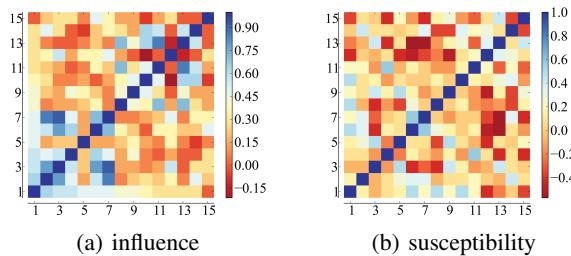


Figure 5: Kendall- τ rank correlation coefficient.

of difference between pairs of features. Every grid represents the correlation between two features. The coefficient values close to 1 or -1 refer to positive and negative correlation between two features, depicted in deep blue or deep red respectively. If two features are independent, the coefficient value approaches to 0, colored by yellow. As shown in Fig. 5, most pairs of features are approximatively independent in both influence and susceptibility, indicating that the learned features are highly discriminative in topic level. Furthermore, we illustrate the top 3 hashtags in latent features shown in Table 5, containing four pairs of features and their hashtags. The influence features 3 and 7 are coherent well with high kendall- τ coefficients 0.93, as hashtag “Xiaomi release” is on the top of both. Those influence and susceptibility features with lower or zero kendall- τ coefficients have distinguished hashtags.

Conclusions

In this paper, we proposed a concise probabilistic model for the information propagation on social network, explicitly characterizing the influence and susceptibility of each user with two low-dimensional vectors respectively. The proposed model distinguishes itself from previous models at its capability of modeling both the interpersonal influence between any pair of users and the cumulative effect in information propagation. We also designed effective algorithms

Table 5: Topic allocation in features

(a) two pairs of features in influence		
kendall- τ coefficients	feature index	ranked hash tags
0.93	3	1. Xiaomi release; 2. Tang Jun education qualification fake; 3. House prices
	7	1. Xiaomi release; 2. Qian Yunhui; 3. House prices
0	2	1. Yao Ming retire; 2. Case of running fast car in Hebei University; 3. Xiaomi release
	14	1. Xiaomi release; 2. Qian Yunhui; 3. House prices

(b) two pairs of features in susceptibility		
kendall- τ coefficients	feature index	ranked hash tags
0.43	6	1. Incident of self-burning at Yancheng, Jiangsu; 2. Tang Jun education qualification fake; 3. Yao Ming retire
	11	1. Xiaomi release; 2. Qian Yunhui; 3. House prices
0	4	1. Incident of self-burning at Yancheng, Jiangsu; 2. Tang Jun education qualification fake; 3. Case of running fast car in Hebei University
	7	1. Qian Yunhui; 2. Incident of self-burning at Yancheng, Jiangsu; 3. House prices

to train the model based on maximizing logarithmic likelihood of information cascades. Our model does not require the knowledge of social network structure, hence having wide applicability to the scenarios with or without explicit social networks. We evaluated the effectiveness of our model on synthetic dataset and a large-scale microblogging dataset from Sina Weibo, the largest social media in China. Experimental results demonstrate that our model consistently outperforms existing methods at predicting cascade dynamics, cascade size, and “who will be retweeted”. Moreover, the learned user-specific influence and susceptibility vectors provide us a quantitative way to understand topic-related interpersonal influence in information propagation.

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