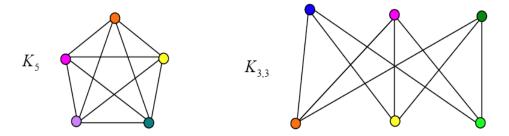
## **HOMEWORK PROBLEMS #2**

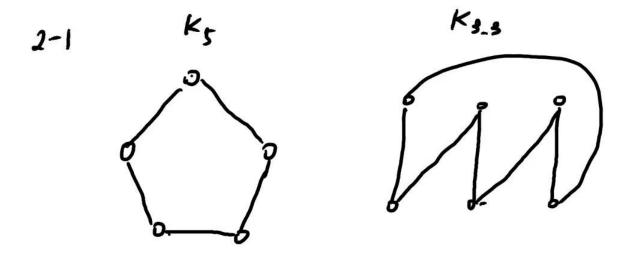
**2-1**Are the following two graphs Eulerian, semi-Eulerian, non-Eulerian, Hamiltonian, semi-Hamiltonian, and/or non-Hamiltonian graphs?



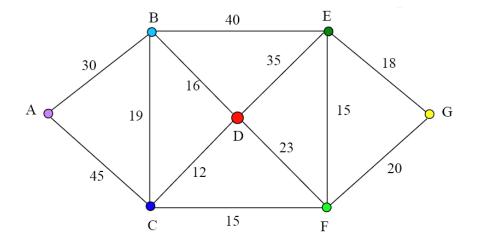
K5 is Eulerian, because the number of points with odd degrees is 0. Also, K5 is connected and there can be no isolated points.

K33 is a non-Eulerian, because the number of points with odd degrees is 6,not 2, so it is not a semi-Eulerian.

K5 and K33 are Hamiltonian. We can find the way



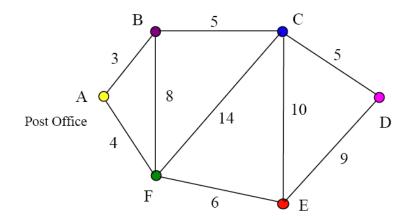
**2-2** Find the shortest path length from A to G in the following graph:

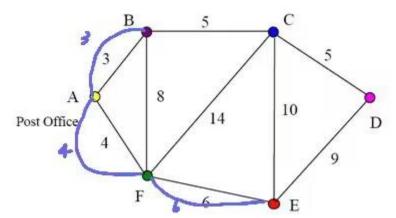


|        | В         | С         | D        | E  | F            | G  |
|--------|-----------|-----------|----------|----|--------------|----|
| Α      | 30        | 45        | ١        | ١  | ١            | ١  |
| AB     | 30        | 45        | 46       | 70 | ١            | ١  |
| ABC    | 30        | 45        | 46       | 70 | 60           | ١  |
| ABCD   | ade 02 30 | <b>45</b> | owade 46 | 70 | denvi60e Ver | ١  |
| ABCDF  | 30        | 45        | 46       | 70 | 60           | 80 |
| ABCDFE | 30        | 45        | 46       | 70 | 60           | 80 |
|        |           |           |          |    |              |    |

We can use the Dijkstra  $Path=A -> C -> F-> G \qquad the \ shortest \ length=80$ 

## **2-3** Solve the following Chinese postman problem:





We use Tpl represents "Total path-length", add three edges For each loop, we can find the increment is not longer than the original loop So it is a solution

A -> F -> E -> D -> C -> D -> F -> C -> B -> A -> B -> F -> A

And total path length is 3+3+4+4+6+6+8+5+14+10+5+9 = 77