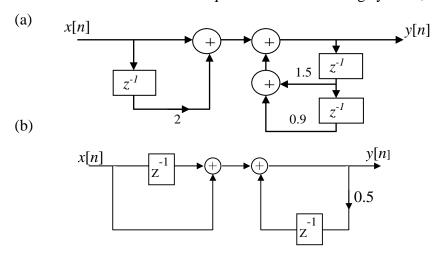
Due: Dec. 01, 2021 (Wednesday)

2021/11/12

Homework #6

** Reading Assignment: Chap. 2 in A.V. Oppenheim and R.W. Schafer, 1999.

1. Please determine the difference equation of the following systems,



2. A causal linear time-invariant system is described by the difference equation,

$$y[n] - 5y[n-1] + 6y[n-2] = 2x[n-1].$$

- (a) Determine the general form of homogeneous response of the system,
- (b) Determine the impulse response of the response,
- (c) Determine the step response of the system, i.e., when x[n] = u[n].
- 3. A causal linear time-invariant system is described by the input-output relation,

$$y[n] = x[n] + 2x[n-1] + x[n-2],$$

- (a) Determine the impulse response of the system,
- (b) Is this system stable?
- 4. A causal linear time-invariant system is described by the difference equation,

$$y[n] - (1/4) y[n-1] - (1/8) y[n-2] = 3 x[n].$$

- (a) Determine the general form of homogeneous response of the system,
- (b) Determine the impulse response of the response,
- (c) Show that this system is stable,
- (a) Fine a particular solution when $x[n] = (1/2)^n u[n]$.
- 5. Consider the difference equation representing a causal LTI system

$$y[n] + (1/a) y[n-1] = x[n-1]$$

- (a) Find the input response of the system, h[n], as the function of the constant a.
- (b) For what range of values of a will the system be stable?