

Problema 3

```

c0      X := X - 1
c1      if (X ≥ Y)
c2          skip
c3          Y := 2X
c4      else
c5          if (W ≥ 8)
c6              W := 3
c7              X := W + X
c8          else
c9              Y := 5
    
```

$$\begin{aligned}
 \text{est} [6-9] &= 2 + 2 \cdot [X-1 \geq Y] + [X-1 < Y] \\
 &\quad + 2 \cdot [W \geq 8] [X-1 < Y] \\
 &\quad + \cancel{[W < 8]} [X-1 < Y] \\
 &\quad [W < 8].
 \end{aligned}$$

$$\begin{aligned}
\text{ert}[c_4 - c_9](0) &= 1 + [w \geq 8] * \text{ert}[w := 3; x := w + x](0) \\
&\quad + [w < 8] * \text{ert}[y := 5](0) \\
&= 1 + [w \geq 8] * \text{ert}[w := 3](\text{ert}[x := w + x](0)) \\
&\quad + [w < 8] * \text{ert}[y := 5](0) \\
&= 1 + [w \geq 8] * \text{ert}[w := 3](1 + 0) \\
&\quad + [w < 8] * (1 + 0) \\
&= 1 + [w \geq 8] * (1 + 1) + [w < 8] * 1 \\
&= 1 + 2 * [w \geq 8] + [w < 8]
\end{aligned}$$

$$\begin{aligned}
\text{ert}[c_2 - c_3](0) &= \text{ert}[\text{skip}](\text{ert}[x := 2x](0)) \\
&= \text{ert}[\text{skip}](1 + 0) \\
&= 1 + 1 \\
&= 2
\end{aligned}$$

$$\begin{aligned}
\text{ert}[c_1 - c_9](0) &= 1 + [x \geq 7] * \text{ert}[c_2 - c_3](0) \\
&\quad + [x < 7] * \text{ert}[c_4 - c_9](0) \\
&= 1 + 2 * [x \geq 7] + [x < 7] \\
&\quad + 2 * [w \geq 8] * [x < 7] + [w < 8] * [x < 7]
\end{aligned}$$

$$\begin{aligned}
 \text{er} \vdash [c_0 - c_9](0) &= \text{er} \vdash [x := x - 1](\text{er} \vdash [c_1 - c_9](0)) \\
 &= \text{er} \vdash [x := x - 1](1 + 2 * [x \geq y] + [x < y] + 2 * [w \geq 8] * [x < y] \\
 &\quad + [w < 8] * [x < x])
 \end{aligned}$$

$$\begin{aligned}
 &= 1 + 1 + 2 * [x - 1 \geq y] + [x - 1 < y] \\
 &\quad + 2 * [w \geq 8] * [x - 1 < y] + [w < 8] * [x - 1 < y]
 \end{aligned}$$