

22) Let f be a function from \mathbb{N} into $2^{\mathbb{N}}$.

Let $D = \{n \in \mathbb{N} : n \notin f(n)\}$. D is a subset of \mathbb{N} , so $D \in 2^{\mathbb{N}}$.

Let n be an arbitrary natural number.

Case 1) $n \in f(n)$. Because $D = \{n \in \mathbb{N} : n \notin f(n)\} \Rightarrow n \notin D \Rightarrow D \neq f(n)$.

Case 2) $n \notin f(n)$. D is \mathbb{N} , but not contained in image set. $\Rightarrow n \notin D$.

Since $n \in D$ & $n \notin f(n)$, $\Rightarrow D \neq f(n)$.

Since there is no integer such that $f(n) = D \Rightarrow D$ is not in range of $f \Rightarrow f$ is not onto.

$f: \mathbb{N} \rightarrow 2^{\mathbb{N}}$. $2^{\mathbb{N}}$ is nonempty, $2^{\mathbb{N}}$ is not countable \square .

24) Let there exist (a, b) such that $a \neq b$ and the interval is finite

Because $a \neq b$, there exists a number c within a & b by axiom

Thus, there exists d between a & c , and \exists 'e' between c & d

This happens an infinite amount of times.

\Rightarrow a nondegenerate interval of real numbers fails to be finite \square

26) With Cantor Schröder Bernstein, it suffices to find an injection $R \times R \rightarrow R$, the equivalent of finding an injection $(0,1) \times (0,1) \rightarrow R$ as R is equipotent to $(0,1)$.
If $r \in (0,1)$, let $0.r_1 r_2 \dots r_n$ be its specific decimal.
To a pair $\langle r, s \rangle \in (0,1) \times (0,1)$, let $0.r_1 r_2 \dots r_n s_n \in (0,1)$.
The decimal development cannot be 9, meaning it being possible to get $r \neq s$, meaning the mapping is injective