

HW 6

6.2) 2^3 Factorial replicated twice

$2^3 \Rightarrow$ 3 factors, each has 2 levels

rep. twice $\Rightarrow 2 \times 2^3 = 16$

Source	df	
Main	3	$(16-1) - 3 - 3 - 1$
2-Way	3	$= 8$
3-Way	1	
Error	<u>8</u>	<u>8 degrees of freedom for Error</u>
Total	15	

6.4) 2^3 Factorial replicated three times

Source	df	
A	1	Error
B	1	$2^3 \times (3-1) = \underline{16}$
C	1	$2^k(r-1)$
AB	1	Total
AC	1	$2^3 \times 3 - 1 = \underline{23}$
BC	1	$2^k r - 1$
ABC	1	$k = \# \text{ factors}$
Error	16	$r = \# \text{ replicates}$
Total	23	$16 + \underline{2} \leftarrow \text{not sig.}$

= 18 degrees of freedom

f) none of the above

(6.5) a)

(1)	22	31	25	78
a	32	43	29	104
b	35	34	50	119
ab	55	47	46	148
c	44	45	38	127
ac	40	37	36	113
bc	60	50	54	164
abc	39	41	47	127

$$A = \frac{(104-78) + (148-119) + (113-127) + (127-164)}{4 \times 3} = \frac{26+29-14-37}{12} = \frac{4}{12} = 0.333$$

$$B = \frac{(119-78) + (148-104) + (164-127) + (127-113)}{4 \times 3} = \frac{41+44+37+14}{12} = \frac{136}{12} = 11.33$$

$$C = \frac{(127+113+164+127-78-104-119-148)}{4 \times 3} = \frac{82}{12} = 6.833$$

$$AB = \frac{(148-104-119+78) + (127-164-113+127)}{4 \times 3} = -\frac{20}{12} = -1.66$$

$$AC = \frac{(78-104+119-148-127+113-164+127)}{4 \times 3} = -\frac{106}{12} = -8.833$$

$$BC = \frac{(78+104-119-148-127-113+164+127)}{4 \times 3} = -\frac{34}{12} = -2.833$$

$$ABC = \frac{(127-164-113+127-148+119+104-78)}{4 \times 3} = -\frac{26}{12} = -2.166$$

The effects of B, C, and AC are significant.

The estimated factor effects are $A=4$, $B=136$, $C=82$
B & C appear to be large.

6.5) b)

$$SS_A = 4^2/24 = .667$$

$$SS_{AB} = -20^2/24 = 16.667$$

$$SS_{ABC} = -26^2/24 = 28.167$$

$$SS_B = 136^2/24 = 770.667$$

$$SS_{AC} = -106^2/24 = 468.167$$

$$SS_{BC} = -34^2/24 = 48.167$$

$$SS_C = 82^2/24 = 280.167$$

Source	df	SS	MS	F	P
A	1	.667	.667	.022	<.883 *
B	1	770.667	770.667	25.557	<.0001 *
C	1	280.167	280.167	9.297	<.0067 *
AB	1	16.667	16.667	.55	.461
AC	1	468.167	468.167	15.52	.0009 *
BC	1	48.167	48.167	1.6	.215
ABC	1	28.167	28.167	.93	.335
Error	16	482.66	30.166		
Total	23	2095.33			

B, C, & AC are significant at 1%.

(6.7)
$$SE_{\text{Effect}} = \sqrt{\frac{1}{n 2^{k-2}} s^2} = \sqrt{\frac{1}{(3) 2^{(3-2)}} (30.17)} = \underline{\underline{2.24}}$$

Variable	Effect
----------	--------

A	.333
---	------

B	11.333 *
---	----------

AB	-1.667
----	--------

C	6.833 *
---	---------

AC	-8.833 *
----	----------

BC	-2.833
----	--------

ABC	-2.167
-----	--------

The 95% CI intervals
for B, C, & AC do
not have zero.

I	II	III	IV		
14.037	16.165	13.972	13.907	58.081	(1)
13.880	13.860	14.032	13.914	55.686	(a)
14.821	14.757	14.843	14.878	59.299	(b)
14.888	14.921	14.415	14.932	59.156	(b)

6.14) $A = (59.156 + 55.686 - 59.299 - 58.081) / 2(4) = \underline{\underline{-2.538}}$

$B = (59.156 + 59.299 - 55.686 - 58.081) / 2(4) = \underline{\underline{.588}}$

$AB = (59.156 + 58.081 - 55.686 - 59.299) / 2(4) = \underline{\underline{.2815}}$

$SS_A = (ab + a - b - (1))^2 / 4n = (-2.538)^2 / 16 = .40259$

$SS_B = (ab + b - a - (1))^2 / 4n = (.588)^2 / 16 = .13735$

a) $SS_{AB} = (ab + (1) - a - b)^2 / 4n = (2.252)^2 / 16 = .3169$

Est. Factor Effects: $A = -2.538, B = .588, AB = 2.252$

Source	SS	DF	MS	F	P
A	.4023	1	.4023	1.2607	>.1
B	.13736	1	.13736	4.3046	.05 < P < .1
AB	.3170	1	.3170	.9934	>.1
Error	3.8287	12	.3191		
Total	5.9216	15			

In this model there are no significant terms.

Table generated through RStudio.