

Linear Algebra

HW1 Cycle Detection

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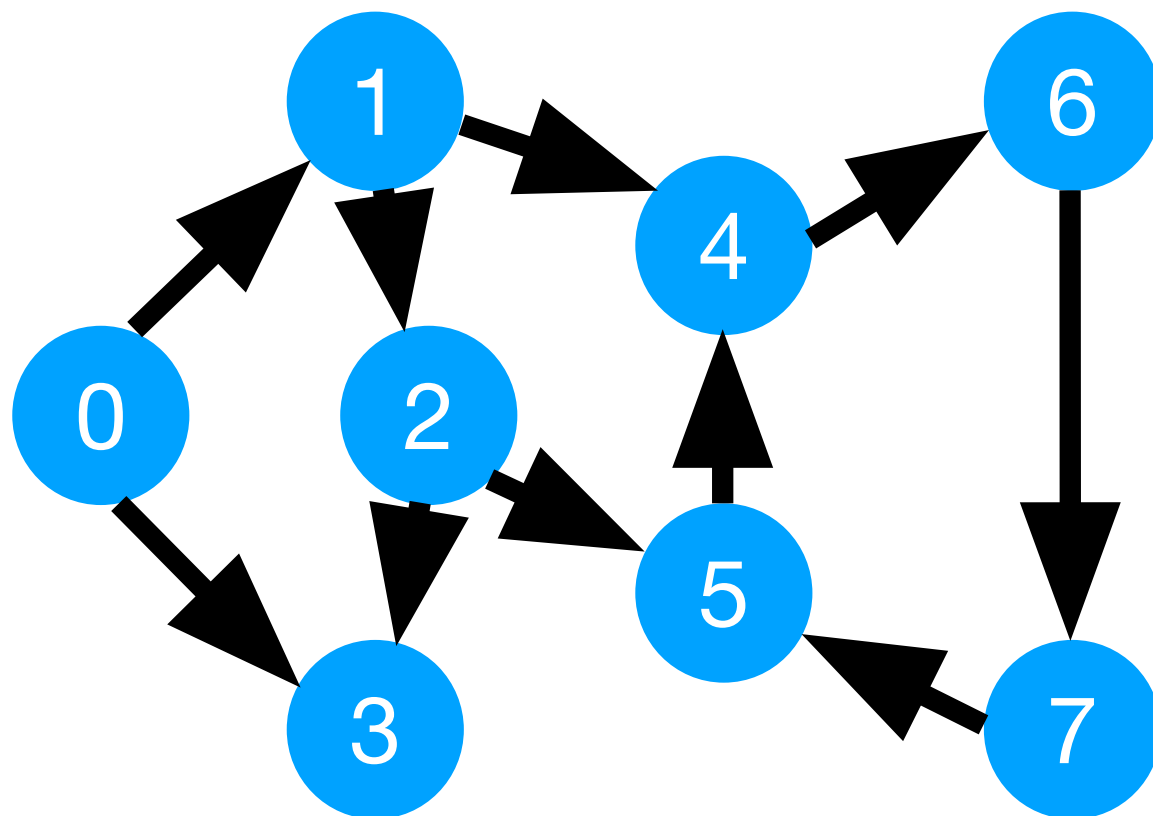
Outline

1. Task Introduction
2. Problem 1
3. Problem 2
4. Python Tips
5. Rules

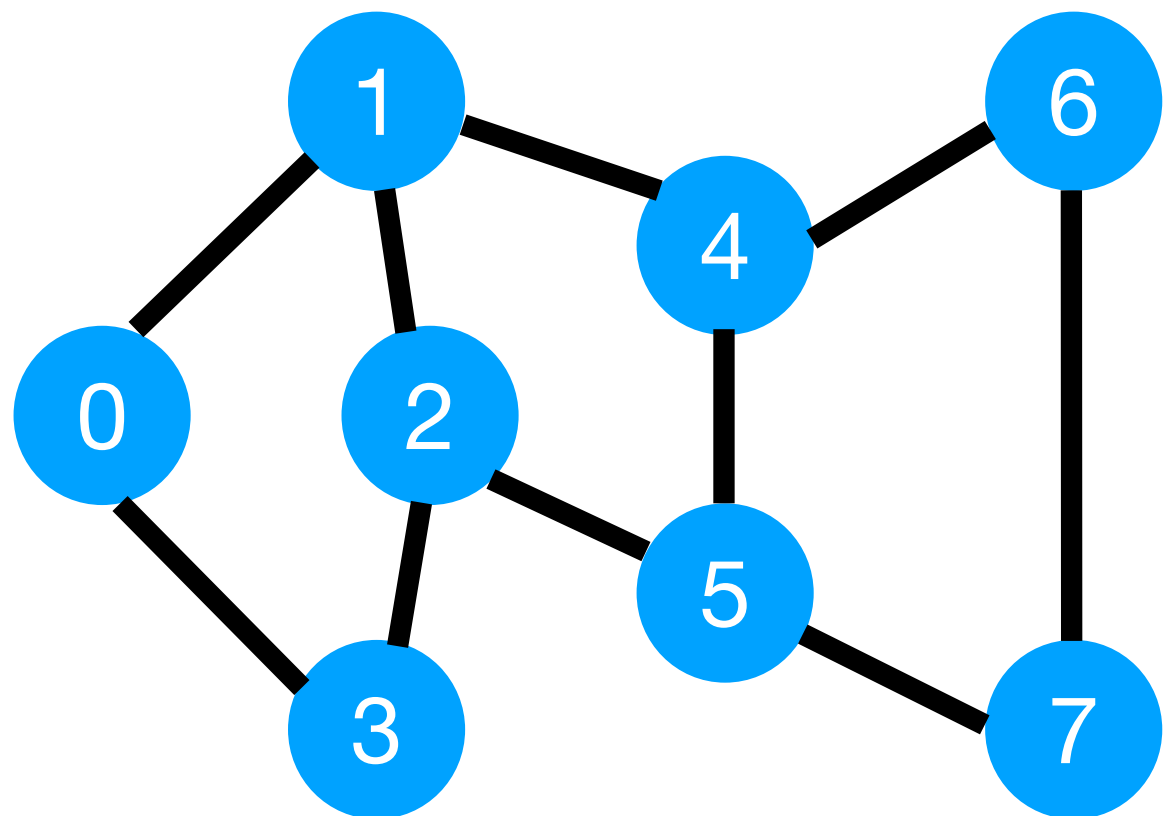
Task Introduction

Graph

- A graph contains some nodes and edges
- The edges can be directed or undirected
- This task is given the **directed graph**, we need to **find out whether there is a cycle** in the graph



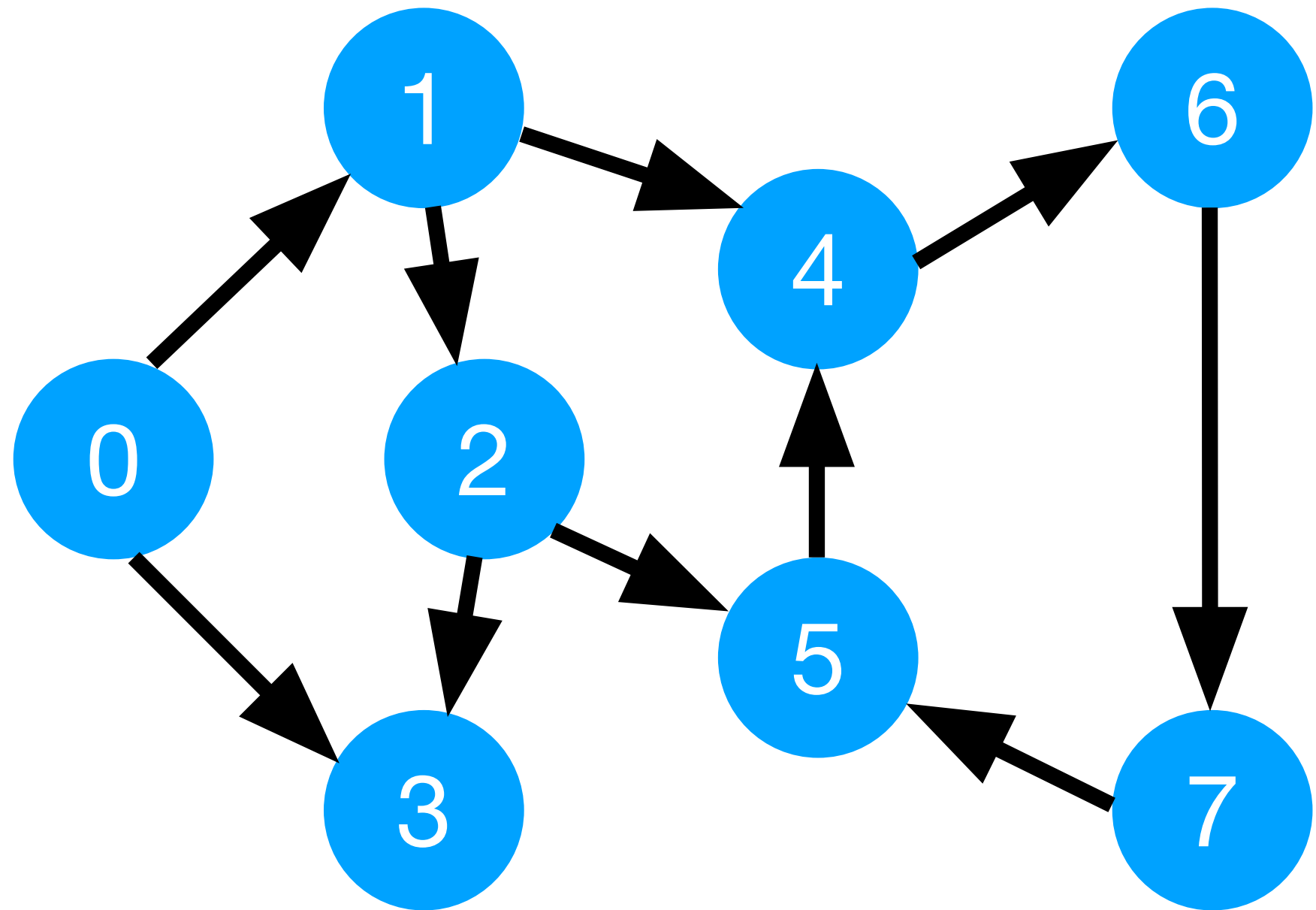
Directed Graph



Undirected Graph

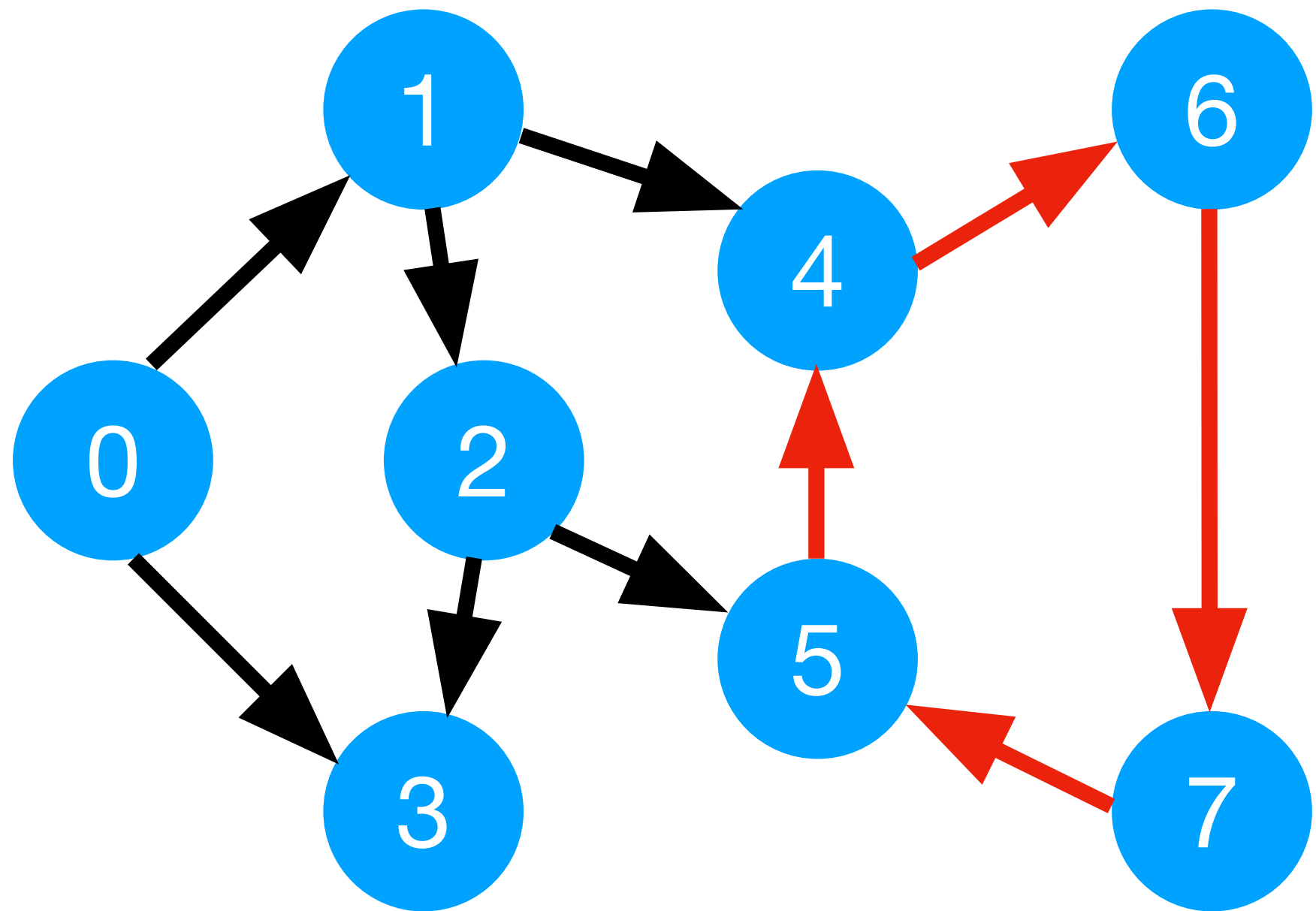
Directed Graph

0 → 1
0 → 3
1 → 2
1 → 4
2 → 3
2 → 5
4 → 6
5 → 4
6 → 7
7 → 5



Cycle Detection

0 → 1
0 → 3
1 → 2
1 → 4
2 → 3
2 → 5
4 → 6
5 → 4
6 → 7
7 → 5



Problem 1

Graph Representation

		0	1	2	3	4	5	6	7
0 → 1	0	-1	1						
0 → 3	1	-1			1				
1 → 2	2		-1	1					
1 → 4	3		-1			1			
2 → 3	4			-1	1				
2 → 5	5			-1			1		
4 → 6	6					-1		1	
5 → 4	7					1	-1		
6 → 7	8							-1	1
7 → 5	9						1		-1

- A row is a connection
- If a connection is from 0 to 1, the value of column 0 will be -1 and the value of column 1 will be 1
- 0 otherwise

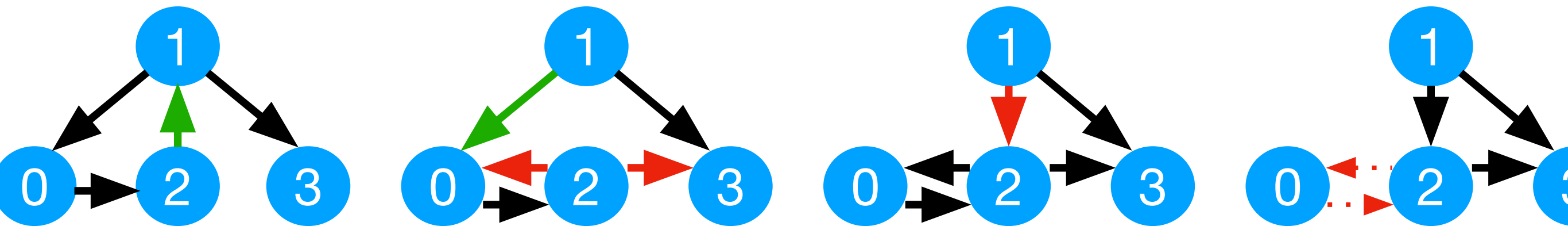
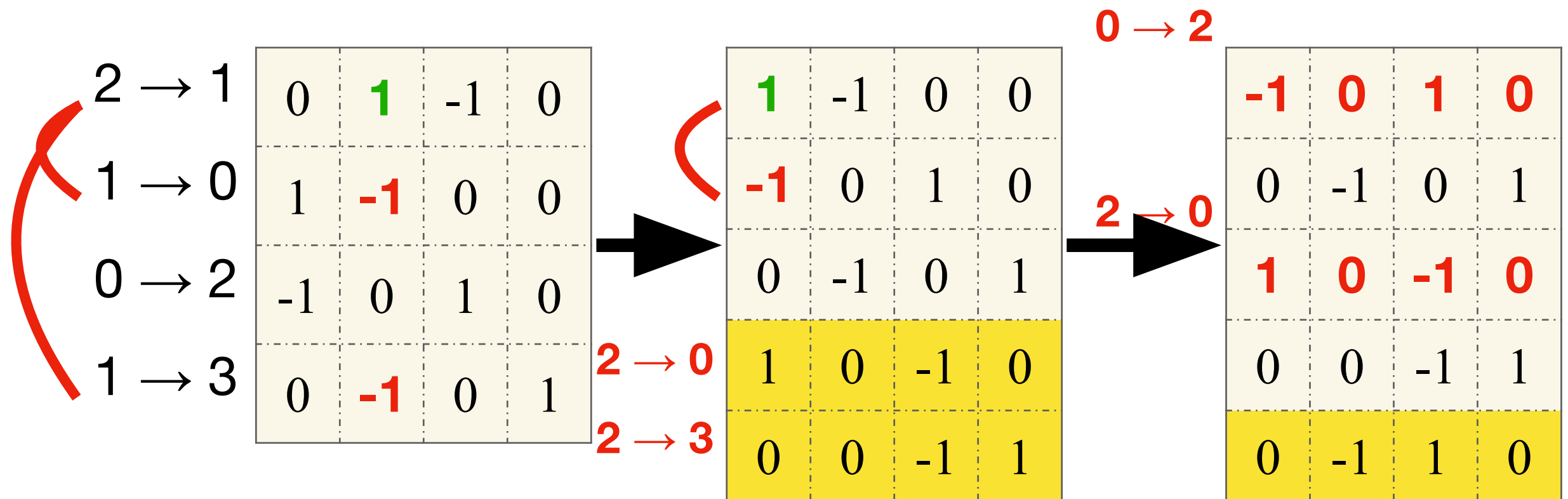
Linear Dependent

- Linear independence in row

2	1	3		2	1	3		2	1	3
1	-1	4	×	0	3	-5		0	3	-5
-2	5	1	-2	0	6	4	×	0	0	-7
1	1	-2	1	0	-1	7	-1/2	0	0	16
			-2				3			

- In cycle detection, we can only do **ADDITION**

Linear Dependent to Detect Cycle



Termination

- If we get a **ALL 0** row after addition, then the graph has a cycle.
- If we do addition on all the edges and we don't get a ALL 0, then the graph does not have a cycle.

p1.py

```
def has_cycle(sets):  
    # TODO  
    # return True if the graph has cycle; return False if not  
  
    return False  
...
```

HINT: You can `print(sets)` to show what the matrix looks like
If we have a directed graph with 2→3 4→1 3→5 5→2 0→1

	0	1	2	3	4	5
0	0	0	-1	1	0	0
1	0	1	0	0	-1	0
2	0	0	0	-1	0	1
3	0	0	1	0	0	-1
4	-1	1	0	0	0	0

The size of the matrix is (5,6)

```
...
```

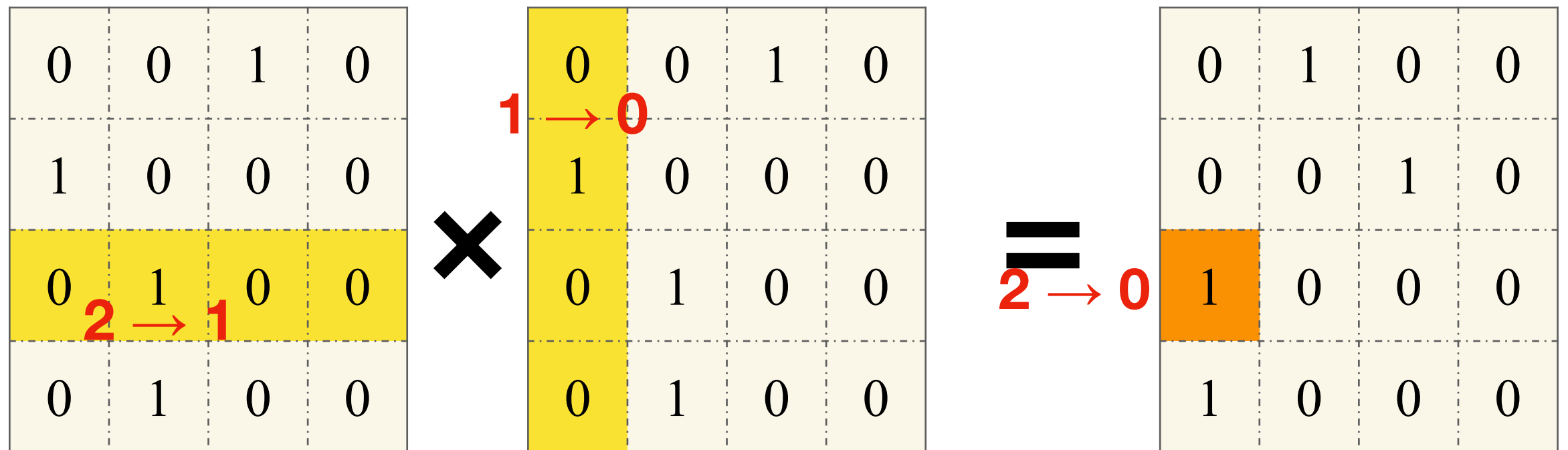
Problem 2

Graph Representation

		0	1	2	3	4	5	6	7
0 → 1	0		1		1				
0 → 3	1			1		1			
1 → 2	2				1		1		
1 → 4	3								
2 → 3	4							1	
2 → 5	5					1			
4 → 6	6								1
5 → 4	7						1		
6 → 7									
7 → 5									

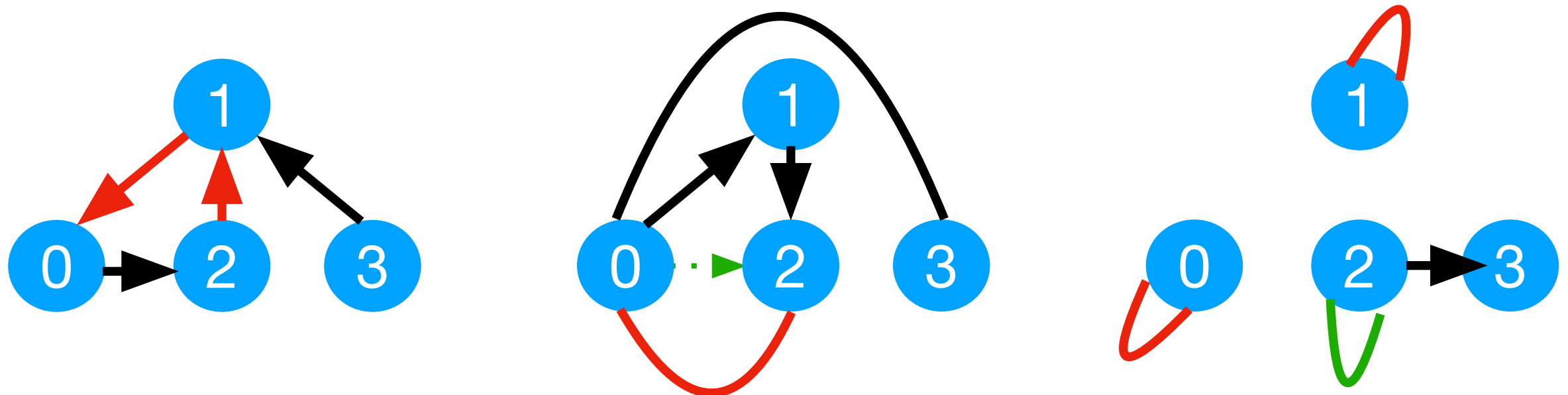
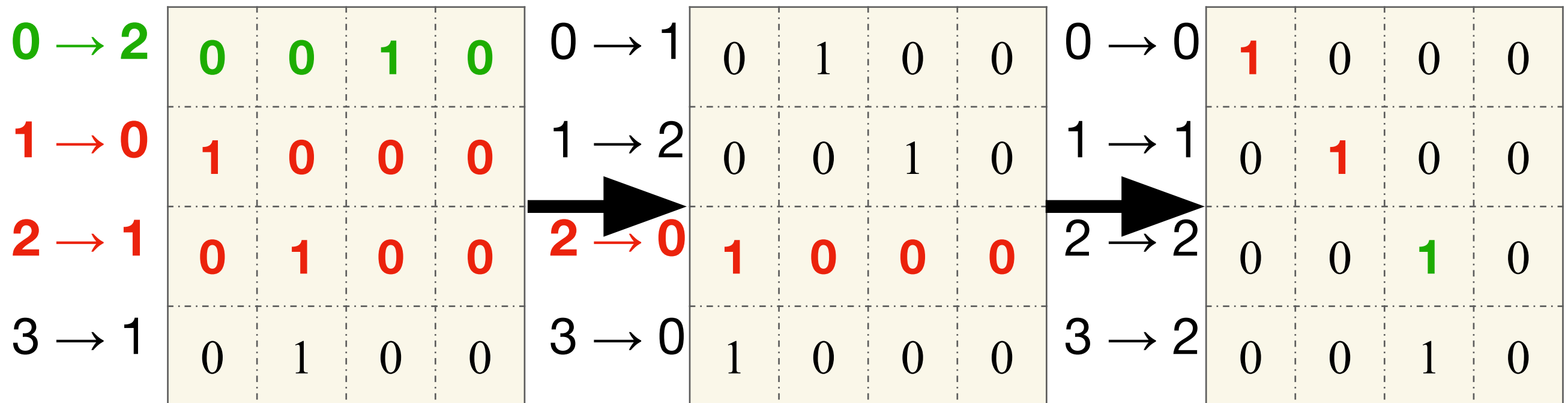
- A cell(x,y) = 1 if there is a connection from x to y
- 0 otherwise

Matrix Multiplication



- Do multiplication at most N times. (N: # of nodes)

Matrix Multiplication



Termination

- If we find a value bigger than 1 in the diagonal of matrix, then the graph has a cycle.
- If we do N times of multiplication and all value in the diagonal are 0, then the graph does not have a cycle.

p2.py

```
def has_cycle(sets):  
    # TODO  
    # return True if the graph has cycle; return False if not  
  
    return False  
'''  
HINT: You can `print(sets)` to show what the matrix looks like  
If we have a directed graph with 2->3 4->1 3->5 5->2 0->1  
    0  1  2  3  4  5  
0  0  1  0  0  0  0  
1  0  0  0  0  0  0  
2  0  0  0  1  0  0  
3  0  0  0  0  0  1  
4  0  1  0  0  0  0  
5  0  0  1  0  0  0  
The size of the matrix is (6,6)  
'''
```

Code Implementation

- You should only complete the function `has_graph(sets)` in `p1.py` and `p2.py`. **DO NOT** modify the other parts of code
- This function will return `True` or `False`
 - If the `graph(sets)` has cycles, this function should return `True`
 - Otherwise, return `False`

Python Tips

List

- Generate an empty list

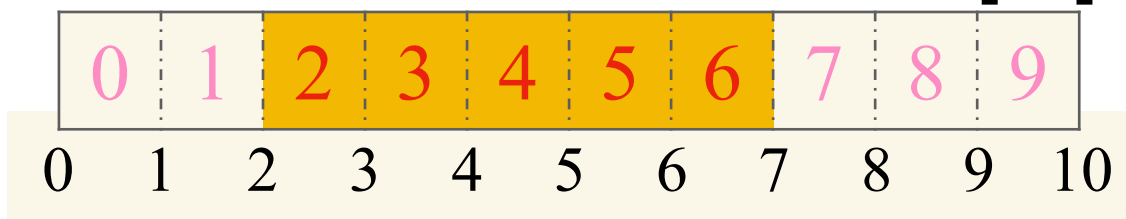
- `L = list()` or `L = []`

- Get a sublist of a list L

- From A to B: `L[A:B]`

- From begin to B: `L[:B]`

- From A to end: `L[A:]`



- Push an object in list

- `L.append(object)`

`L = [2, 4, [1, 2], [3, 6]]`

`object = 8`

`L.append(object)`

`>>> L = [2, 4, [1, 2], [3, 6], 8]`

- Extend a list L2 and push it in list L

- `L.extend(L2)`

`L2 = [4, [2, 3]]`

`L.append(L2)`

`>>> L = [2, 4, [1, 2], [3, 6], 8, 4, [2, 3]]`

NumPy

- Create a numpy object
 - `L = numpy.array([3, 2, 5, 1])`
- Two numpy matrix A, B multiplication
 - `numpy.matmul(A, B)`
`A = [[1, 2], [3, 4]]`
`B = [[2, 3], [4, 5]]`
`numpy.matmul(A, B)`
`>>> [[10, 13], [22, 29]]`

Rules

Run Code

- `python p1.py r07922072`

Yes

No

No

... 12 outputs

- You should run your code with your 學號

- You can generate answer text file by running command

`python p1.py 自己的學號 > p1_ans.txt`

`python p2.py 自己的學號 > p2_ans.txt`

- Or just type them by yourself

Yes

No

No

Yes

No

Yes

Yes

Yes

No

No

Yes

No

Code Structure

- Code you **download**
 - |—p1.py (TODO)
 - |—p2.py (TODO)
 - |—graph_gen.py
- Code you **submit** should be put in a folder and compressed in a zip file

r07922072_hw1.zip

r07922072_hw1

|—p1.py

|—p2.py

|—graph_gen.py

|—p1_ans.txt

|—p2_ans.txt

Rules

- 不要抄作業，不要交別人的答案，作弊一律0分計算
- 上傳 zip 檔案到 CEIBA
- 注意繳交的資料夾學號開頭英文用**小寫**
- **DEADLINE: 2018/10/18(四) 23:59 (GMT+8:00)**
- **遲交每過一天：分數 $\times 0.8$ (per day)**
- **格式、檔案、各種奇怪的錯誤讓我無法改作業：分數 $\times 0.8$**

Q & A

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