Traveling Salesman Problem solution

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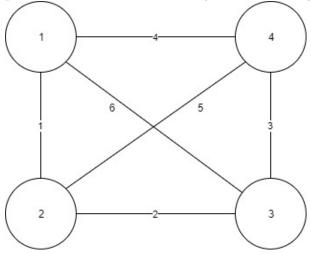
# Abstract

This paper discuss how to solve the Traveling Salesman Problem. I tried naive/BF solution at first. After research some other algorithm, I impoved my solution and use genetic algorithm.

### Traveling Salesman Problem solution

#### Introduction

Travelling salesman problem: Given a set of cities and distance between every pair of cities, the problem is to find the shortest possible route that visits every city exactly once and returns to the starting point. This problem is a famous NP hard problem, which means there is no polynomial time know the solution for the problem. However, when the number of city is very small, we can easily figure out the answer. For example, consider the given graph. There are 4 cities, which is 1,2,3,4. We can quickly figure out that the shortest route would be 1+2+3+4=10. However, if we search deep for how we get this out. The answer is that, we generate all the possible route, which is 1\*2\*3=6 possible ways. What's more when we are doing this we set 1 as the starting and ending point automatically. Theoretically, the idea is right. Calculate all the possible route and find out the minimum. Although the idea is simple, in real world, there would be much more cities involved. As the number of city goes up, the possible routes would increase like crazy. It will take too much time to calculate it, even we use computer programming. In this case, researchers find some other way to solve this problem, even the answer may not be exactly the right one, it is still very close.



## Naive/BF implementation

There are a lot of solutions for the traveling salesman problem. Naïve/BF is the simplest one. The idea about naïve solution is easy to understand. Consider all the

possible routes and compare with other and find the lowest cost. The algorithm of naïve/BF implementation is:

- 1. Consider a city as the starting and ending point.
- 2. Generate all (n-1) permutations of cities, which means generate all the possible routes.
- 3. Calculate cost of every permutation and keep track of min cost route.
- 4. Return the minimum cost route.

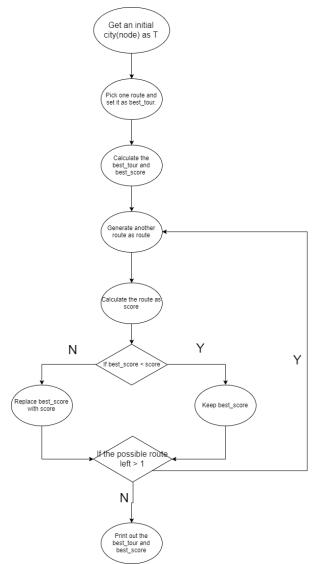
The code below is the pseudocode and flowchart for the BF implementation.

```
void brute_force_solver(const Tsp_map& cities) {
Tour tour(cities.get_default_tour());

double best_score = cities.score(tour);
Tour best_tour(tour);
cout << tour << " score = " << best_score << endl;
while (next_permutation(tour.begin() + 1, tour.end())) {
double s = cities.score(tour);
if (s < best_score) {
best_score = s;
best_tour = tour;
}

cout << tour << " score = " << s << endl;
} // while

cout << "best_tour = " << best_tour
<< "\nscore = " << best_score << endl;</pre>
```



Based on the flowchart and pseudocode, we

can generate those advantages about the naïve/BF implementation:

- 1. Naïve/BF implementation will find the most correct route if we have enough time to run this program. (The idea about most correct route I will declare it later in the paper)
- 2. Simple algorithm, and easy coding.

However, we can generate some disadvantages as well.

- 1. It is not efficient.
- 2. It takes too much time to run the program, no one in the real world would ever take so much time to calculate this. Not good for real problem.

### Genetic Algorithm

Since the naive solution is not good enough, researchers need to create some new algorithm to solve the problem. one of those algorithms is called genetic algorithm. It is a meta-heuristic inspired by the nature world, which is the process of natural selection. Implement this genetic algorithm into TSP, it will performance much more better than the naive solution. The idea about genetic algorithm is different than the naive solution. First, we also need to consider a city as starting and ending point, and then generate one route from starting point to ending point. Second, it is the part that different from naive solution. As the algorithm named, we will do the a magic part, which is called crossover and mutation. With this step, we will crossover and mutate our parameter in the TSP problem which will lead to some new routes. Third, find the lowest cost route, and repeat the second step. In order to understand more, we can think the genetic algorithm in this way, you find a route, and then you change some way in the middle of your previous routes. In this case, you will get some different cost of the routes. However, it must have one route is the closest to the correct answer. Thus, we repeat this steps over and over again until the lowest cost route stop changing. The following is the genetic algorithm from Mohd. Haque and Khalid Magld.

Step 1: Construct a tree or minimum spanning tree from the graph based on the group size. Root node is the starting point of the salesman.

Step 2: Construct the tours from each leaf node and from starting node in tree in the following way.

Step 3: Applying the GA to this tree. I. Select any chromosome form the tree II. Here we have two kind of crossover one is inside the chromosome and other in between two chromosomes. a) One point - part of the first parent is copied and the rest is taken in the same order as in the second parent b) Two point - two parts of the first parent are copied and the rest between is taken in the same order as in the second parent c) None - no crossover, offspring is exact copy of parents III. Mutation can be done to the chromosome in the following ways. a) Normal random - a few cities are chosen and exchanged

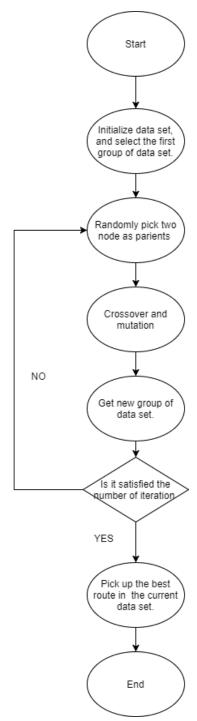
- b) Random, only improving a few cities are randomly chosen and exchanged only if they improve solution (increase fitness) c) Systematic, only improving cities are systematically chosen and exchanged only if they improve solution (increase fitness) d) None no mutation
- Step 4: Add the entire route from the entire computed tree (from step 3) with the route using EAX; consider two best route from the tree as A and B. If result of EAX is better than our A and B than take the result of EAX Otherwise take best route from A and B.
- Step 5: Compute the fitness score from the route formed from step 5 using fitness function if new route has better fitness score than previous then replace the route.
- Step 6: Repeat step 3 to step 5 until better fitness score is obtained or all computed tree (from Step 3) have been added to the route.
- Step 7: return the best result.(Mohd. JuneDul Haque and Khalid. W Magld, 2012)

#### **Ant Colony Optimization**

Ant Colony Optimization is another interesting algorithm to solve the TSP. I think ACO has some similar features with genetic algorithm. For example, the first sample data is very important. In this case, sometime we need to restart the whole process to check if we are on the right way. (Sarita Rai and Rajkumar Sharma, 2015)

#### My Solution

After research others algorithm to solve the TSP. I improved my previous naive solution to genetic algorithm which is much better and more efficient. The following is



the flowchart.

Compare my genetic algorithm with naive solution, genetic algorithm is much more faster and efficient. The reason is obvious, in the naive solution, the program will list all the possible routes which means it will goes to every possible nodes and then get the best route. However, in genetic algorithm, we use sample data set instead of whole data set which means the program didn't need to go through every route to find the best routes. Even though, in the genetic algorithm, the iteration time still would affect the time. In the test I made, when the iteration time is 500, the time is 2.074s, and when

the iteration times is 1500, the running time increase to around 6s. However, with more iteration time, the best route is smaller, which means more iteration time will make the result much more close to the correct answer.

#### References

Mohd. JuneDul Haque and Khalid. W. Magld. (2012) Improving the Solution of Traveling Salesman Problem Using Genetic, Memetic Algorithm and Edge assembly Crossover

Ayman Srour, Zulaiha Ali Othman, and Abdul Razak Hamdan. (2014) A Water Flow-Like Algorithm for the Travelling Salesman Problem

Sabah Sadiq. (2012) The Traveling Salesman Problem: Optimizing Delivery Routes Using Genetic Algorithms

Sarita Rai and Rajkumar Sharma. (2015) Solution to Travelling Salesman Problem by Nature Inspired Algorithm

Eric Kuang. (2012) A 2-opt-based Heuristic for the Hierarchical Traveling Salesman Problem

Houchaoqun. (2017) TSP genetic algorithm,

"http://blog.csdn.net/houchaoqun $_x$ mu/article/details/54584264"

# Appendix

```
oouble)
std::char_tralts<char> >& std::endl<char, std::char_tralts<char> >(std::basic_ostream<char, std::char_traits<char> >&)
std::ostream&(*)(std::ostream&))
int, int):
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hw3.aux hw3.ndf IMG1.png problem2.pdf texput.log TSP.aux tsp.ods TSP-problem-research TSP.tex
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//szede4/TSP-problem-researchs TSP.tex
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//szede4/TSP-problem-researchs TSP.tex
//szede4/TSP-problem-researchs GA-pp GA
```

# Code:

```
#include <iostream>
#include <fstream>
#include <iomanip>
#include <stdlib.h>
```

```
#include <ctime>
#include <algorithm>
#include "GA.h"
using namespace std;
int IndexCross_i;
int IndexCross_j;
int main(){
time_t T_begin = clock();
Graph G;
CreateGraph(G);
srand ( unsigned ( time(0) ) );
InitialGroup(G);
TSP_Evolution(G);
```

```
time_t T_end = clock();
double RunningTime = double(T_end - T_begin) / CLOCKS_PER_SEC;
cout<<endl<<" RunningTime = " << RunningTime << " "<<endl;</pre>
system("pause");
return 0;
}
void CreateGraph(Graph &G){
ifstream read_in;
read_in.open("/home/teddy/cse464/TSP-problem-research/att48_d.txt");
if (!read_in.is_open())
{
cout<<"read fail."<<endl;</pre>
return;
```

```
}
read_in >> G.vex_num;
// read_in >> G.arc_num;
G.arc_num = 0;
for (int i = 0;i < G.vex_num; i++)</pre>
{
read_in >> G.vexs[i];
}
G.vexs[G.vex_num] = '\0';
for (int i = 0; i < G.vex_num;i++)</pre>
{
for (int j = 0; j < G.vex_num; j++)</pre>
{
read_in >> G.arcs[i][j];
```

```
// calculate the arc_num
if (G.arcs[i][j] > 0)
{
G.arc_num++;
}
}
}
for (int i = 0; i < G.vex_num; i++)</pre>
{
cout << G.vexs[i] << " ";</pre>
}
}
void InitialGroup(Graph G){
cout<<"----"<<endl;
```

```
cout<<" CITY_NUM ="<< CITY_NUM <<endl;</pre>
cout<<" GROUP_NUM = "<< GROUP_NUM <<endl;</pre>
cout<<" SON_NUM = "<< SON_NUM <<endl;</pre>
cout<<" P_INHERIATANCE = "<< P_INHERIATANCE <<endl;</pre>
cout<<" P_COPULATION = "<< P_COPULATION <<endl;</pre>
cout<<" ITERATION_NUM = "<< ITERATION_NUM <<endl;</pre>
double total_length = 0.0;
for(int i = 0;i < GROUP_NUM; i++){</pre>
for (int j = 0; j < G.vex_num; j++)</pre>
{
TSP_Groups[i].path[j] = G.vexs[j];
}
random_shuffle(TSP_Groups[i].path + 1, TSP_Groups[i].path + G.vex_num);
if (Check_path(G, TSP_Groups[i]))
{
```

```
TSP_Groups[i].length_path = CalculateLength(G, TSP_Groups[i]);
total_length += TSP_Groups[i].length_path;
}else{
cout<<"error"<<endl;</pre>
TSP_Groups[i].length_path = MAX_INT;
TSP_Groups[i].P_Reproduction = 0;
}
}
Calc_Probablity(G, total_length);
TSP_Evaluate(G);
}
void Calc_Probablity(Graph G, double total_length){
double TempTotal_P = 0.0;
```

```
for (int i = 0; i < GROUP_NUM ;i++)</pre>
{
TSP_Groups[i].P_Reproduction = (1.0 / TSP_Groups[i].length_path ) *
   total_length;
TempTotal_P += TSP_Groups[i].P_Reproduction;
}
for (int i = 0;i < GROUP_NUM; i++)</pre>
{
TSP_Groups[i].P_Reproduction = TSP_Groups[i].P_Reproduction / TempTotal_P;
}
}
void TSP_Evolution(Graph G){
/* */
int iter = 0;
while(iter < ITERATION_NUM){</pre>
```

```
int Father_index = Evo_Select(G);
int Mother_index = Evo_Select(G);
while (Mother_index == Father_index)
{
Mother_index = Evo_Select(G);
}
TSP_solution Father = TSP_Groups[Father_index];
TSP_solution Mother = TSP_Groups[Mother_index];
int M = GROUP_NUM - GROUP_NUM/2;
Length_SonSoliton = 0;
while(M){
double Is_COPULATION = ((rand()%100 + 0.0) / 100);
```

```
if (Is_COPULATION > P_COPULATION)
{
// cout<<"Is_COPULATION = "<<Is_COPULATION<<endl;</pre>
}else{
Evo_Cross(G, Father, Mother);
M--;
}
}
double total_length = 0.0;
for (int IndexVariation = 0;IndexVariation < Length_SonSoliton;</pre>
   IndexVariation++)
{
double RateVariation = (rand()%100) / 100;
if (RateVariation < P_INHERIATANCE)</pre>
```

```
{
Evo_Variation(G, IndexVariation);
}
if (!Check_path(G, Son_solution[IndexVariation]))
{
cout<<"error"<<endl;</pre>
}
Son_solution[IndexVariation].length_path = CalculateLength(G,
   Son_solution[IndexVariation]);
total_length += Son_solution[IndexVariation].length_path;
}
Calc_Probablity(G, total_length);
/*
```

```
for (int i = 0; i < Length_SonSoliton; i++)</pre>
{
for (int j = 0; j < G.vex_num; j++)
{
cout<<Son_solution[i].path[j]<<" -> ";
}
cout<<Son_solution[i].path[0]<<" length_path =</pre>
   "<<Son_solution[i].length_path<<" P_Reproduction =
   "<<Son_solution[i].P_Reproduction<<endl;
}
*/
Evo_UpdateGroup(G);
iter++;
}
}
```

```
int Evo_Select(Graph G){
double selection_P = ((rand()%100 + 0.0) / 100);
// cout<<"selection_P = "<<selection_P<<endl;</pre>
double distribution_P = 0.0;
for (int i = 0; i < GROUP_NUM; i++)</pre>
{
distribution_P += TSP_Groups[i].P_Reproduction;
if (selection_P < distribution_P)</pre>
{
return i;
}
}
cout<<"Error(Evo_select)"<<endl;</pre>
return 0;
```

```
}
void Evo_Cross(Graph G, TSP_solution TSP_Father, TSP_solution TSP_Mother){
IndexCross_i = rand() % (CITY_NUM - 1) + 1; //
IndexCross_j = rand() % (CITY_NUM - 1) + 1; //
if (IndexCross_i > IndexCross_j)
{
int temp = IndexCross_i;
IndexCross_i = IndexCross_j;
IndexCross_j = temp;
}
if (IndexCross_j == CITY_NUM || IndexCross_i == 0)
{
cout<<"[error...]"<<endl;</pre>
```

```
}
int Father_Cross[CITY_NUM];
int Mother_Cross[CITY_NUM];
int Length_Cross = 0;
for (int i = IndexCross_i;i <= IndexCross_j; i++)</pre>
{
Father_Cross[Length_Cross] = TSP_Father.path[i];
Mother_Cross[Length_Cross] = TSP_Mother.path[i];
Length_Cross++;
}
int *Conflict_Father;
int *Conflict_Mother;
int Length_Conflict = 0;
Conflict_Father = Get_Conflict(Father_Cross, Mother_Cross, Length_Cross,
```

```
Length_Conflict);
Conflict_Mother = Get_Conflict(Mother_Cross, Father_Cross, Length_Cross,
   Length_Conflict);
int city_temp;
for (int i = IndexCross_i; i <= IndexCross_j; i++)</pre>
{
city_temp = TSP_Father.path[i];
TSP_Father.path[i] = TSP_Mother.path[i];
TSP_Mother.path[i] = city_temp;
}
TSP_solution Descendant_ONE = Handle_Conflict(G, TSP_Father, Conflict_Father,
   Conflict_Mother, Length_Conflict);
TSP_solution Descendant_TWO = Handle_Conflict(G, TSP_Mother, Conflict_Mother,
   Conflict_Father, Length_Conflict);
Son_solution[Length_SonSoliton++] = Descendant_ONE;
```

```
Son_solution[Length_SonSoliton++] = Descendant_TWO;
}
TSP_solution Handle_Conflict(Graph G, TSP_solution ConflictSolution, int
   *Detection_Conflict, int *Model_Conflict, int Length_Conflict){
for (int i = 0; i <= Length_Conflict; i++)</pre>
{
bool flag_FindCity = false;
int index = 0;
// [0, IndexCross_i)
for (index = 0; index < IndexCross_i; index++)</pre>
{
if (Model_Conflict[i] == ConflictSolution.path[index])
{
flag_FindCity = true;
break;
```

```
}
}
if (!flag_FindCity)
{
// [IndexCross_i + 1, G.vex_num)
for (index = IndexCross_j + 1; index < G.vex_num; index++)</pre>
{
if (Model_Conflict[i] == ConflictSolution.path[index])
{
break;
}
}
}
// 9 8 [1 4 0 3 2] 3 2 0 --> ConflictSolution
```

```
// 8 7 [4 5 6 7 1] 9 6 5
// [0 3 2] --> Detection_Conflict
// [4 5 6] --> Model_Conflict
// cout<<"index = "<<index<<endl;</pre>
ConflictSolution.path[index] = Detection_Conflict[i];
}
/*
for (int i = 0;i < G.vex_num;i++)</pre>
{
cout<<ConflictSolution.path[i]<<" -> ";
}
cout<<ConflictSolution.path[0]<<endl;</pre>
// CalculateLength(G, ConflictSolution);
*/
```

```
if (!Check_path(G, ConflictSolution))
{
cout<<"error"<<endl;</pre>
}
// cout<<" length_path = "<<ConflictSolution.length_path<<" P_Reproduction =</pre>
   "<<ConflictSolution.P_Reproduction<<endl;
return ConflictSolution;
}
int *Get_Conflict(int Detection_Cross[], int Model_Cross[], int Length_Cross,
   int &Length_Conflict){
int *Conflict = new int[CITY_NUM];
Length_Conflict = 0;
for (int i = 0; i < Length_Cross; i++)</pre>
{
bool flag_Conflict = true;
```

```
for (int j = 0; j < Length_Cross; j++)</pre>
{
if (Detection_Cross[i] == Model_Cross[j])
{
j = Length_Cross;
flag_Conflict = false;
}
}
if (flag_Conflict)
{
Conflict[Length_Conflict] = Detection_Cross[i];
Length_Conflict++;
}
}
return Conflict;
```

```
}
void Evo_Variation(Graph G, int Index_Variation){
int City_i = (rand() % (CITY_NUM - 1)) + 1;
int City_j = (rand() % (CITY_NUM - 1)) + 1; //
while(City_i == City_j){
City_j = (rand() \% (CITY_NUM - 1)) + 1;
}
int temp_City = Son_solution[Index_Variation].path[City_i];
Son_solution[Index_Variation].path[City_i] =
   Son_solution[Index_Variation].path[City_j];
Son_solution[Index_Variation].path[City_j] = temp_City;
}
```

```
void Evo_UpdateGroup(Graph G){
TSP_solution tempSolution;
for (int i = 0; i < Length_SonSoliton; i++)</pre>
{
for (int j = Length_SonSoliton - 1; j > i; j--)
{
if ( Son_solution[i].length_path > Son_solution[j].length_path )
{
tempSolution = Son_solution[i];
Son_solution[i] = Son_solution[j];
Son_solution[j] = tempSolution;
}
}
}
```

```
for (int i = 0; i < Length_SonSoliton; i++)</pre>
{
for (int j = 0; j < GROUP_NUM; j++)</pre>
{
if ( Son_solution[i].length_path < TSP_Groups[j].length_path )</pre>
{
TSP_Groups[j] = Son_solution[i];
break;
}
}
}
TSP_Evaluate(G);
}
```

double CalculateLength(Graph G, TSP\_solution newSolution){

```
double _length = 0;
for (int i = 0; i < G.vex_num - 1; i++)</pre>
{
int _startCity = newSolution.path[i] - 1;
int _endCity = newSolution.path[i+1] - 1;
if (G.arcs[_startCity][_endCity] == -1)
{
return MAX_INT;
}
else{
_length += G.arcs[_startCity][_endCity];
}
}
if (G.arcs[newSolution.path[G.vex_num - 1]][newSolution.path[0] - 1] == -1)
```

```
{
return MAX_INT;
}
else{
_length += G.arcs[newSolution.path[G.vex_num - 1] - 1][newSolution.path[0] -
   1];
// cout<<"_length = "<<_length<<endl;</pre>
return _length;
}
}
bool Check_path(Graph G, TSP_solution CurrentSolution){
for (int i = 0; i < G.vex_num;i++)</pre>
{
for (int j = i + 1; j < G.vex_num; j++)</pre>
{
if (CurrentSolution.path[i] == CurrentSolution.path[j])
```

```
{
return false;
}
}
}
return true;
}
void TSP_Evaluate(Graph G){
TSP_solution bsetSolution;
bsetSolution = TSP_Groups[0];
for (int i = 1; i < GROUP_NUM; i++)</pre>
{
if (bsetSolution.length_path > TSP_Groups[i].length_path)
{
bsetSolution = TSP_Groups[i];
```

```
}
}
cout<<" bsetSolution = ";</pre>
for (int i = 0;i < G.vex_num;i++)</pre>
{
cout<<bsetSolution.path[i]<<" -> ";
}
cout<<bsetSolution.path[0]<<" length = "<<bsetSolution.length_path<<endl;</pre>
}
#ifndef _GA_H_
#define _GA_H_
#define CITY_NUM 150
#define GROUP_NUM 30
#define SON_NUM 32
const double P_INHERIATANCE = 0.01;
const double P_COPULATION = 0.8;
const int ITERATION_NUM = 1500;
const double MAX_INT = 99999999.0;
```

```
typedef struct{
int vex_num, arc_num;
int vexs[CITY_NUM];
double arcs[CITY_NUM][CITY_NUM];
}Graph;
typedef struct{
double length_path;
int path[CITY_NUM];
double P_Reproduction;
}TSP_solution;
TSP_solution TSP_Groups[GROUP_NUM];
TSP_solution Son_solution[SON_NUM];
int Length_SonSoliton = 0;
void CreateGraph(Graph &G);
void InitialGroup(Graph G);
double CalculateLength(Graph G,TSP_solution newSolution);
void TSP_Evolution(Graph G);
int Evo_Select(Graph G);
void Evo_Cross(Graph G, TSP_solution TSP_Father, TSP_solution TSP_Mother);
void Evo_Variation(Graph G, int Index_Variation);
void Evo_UpdateGroup(Graph G);
void TSP_Evaluate(Graph G);
int *Get_Conflict(int Conflict_Father[], int Conflict_Mother[], int
   Length_Cross, int &Length_Conflict);
TSP_solution Handle_Conflict(Graph G, TSP_solution ConflictSolution, int
```

```
*Detection_Conflict, int *Model_Conflict, int Length_Conflict);

void Calc_Probablity(Graph G, double total_length);

bool Check_path(Graph G, TSP_solution CurrentSolution);

void Display(Graph G);

#endif
```