

Homework 4

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Problem 1

| Configuration | Virtual Addr bits | Physical Addr bits | VPN bits | PPN bits | Offset bits |
|--------------------------------------|-------------------|--------------------|----------|----------|-------------|
| a. 32-bit OS, 4 KB pages, 1 GB RAM | 32 | 30 | 20 | 18 | 12 |
| b. 32-bit OS, 16 KB pages, 2 GB RAM | 32 | 31 | 18 | 17 | 14 |
| c. 64-bit OS, 16 KB pages, 16 GB RAM | 64 | 34 | 50 | 20 | 14 |

Advantages of Larger Page Size

- Reduced page-table overhead: fewer entries smaller tables.
- Higher TLB coverage: each entry maps more bytes fewer TLB misses.
- Improved I/O efficiency: larger contiguous transfers fewer disk operations.

Disadvantages of Larger Page Size

- Increased internal fragmentation: more wasted space per page.
- Longer page-fault service time: loading a larger page takes more I/O.
- Potential memory-bandwidth waste: unused data still consumes bus cycles.

Problem 2

Address Stream and VPNs

| Virtual Address | VPN (VA \gg 12) |
|-----------------|-------------------|
| 0x0FFF | 0 |
| 0x7A28 | 7 |
| 0x3DAD | 3 |
| 0x3A98 | 3 |
| 0x1C19 | 1 |
| 0x1000 | 1 |
| 0x22D0 | 2 |

Step-by-Step Results

| VA | VPN | Result | PPN | Explanation |
|--------|-----|------------------|-----|---|
| 0x0FFF | 0 | TLB miss, PT hit | 5 | Load VPN 0 \rightarrow PPN 5 into TLB (evict LRU=1) |
| 0x7A28 | 7 | TLB hit | 4 | Tag 7 already in TLB |
| 0x3DAD | 3 | TLB hit | 6 | Tag 3 in TLB |
| 0x3A98 | 3 | TLB hit | 6 | Repeat access still TLB hit |
| 0x1C19 | 1 | Page fault | 13 | Allocate PPN 13, update PT and TLB (evict LRU=2) |
| 0x1000 | 1 | TLB hit | 13 | Just loaded |
| 0x22D0 | 2 | Page fault | 14 | Allocate PPN 14, update PT and TLB (evict LRU=3) |

Final TLB State

| Slot | Valid | Tag (VPN) | Physical Page # | LRU Rank (1=oldest, 4=newest) |
|------|-------|-----------|-----------------|-------------------------------|
| 1 | 1 | 2 | 14 | 4 |
| 2 | 1 | 1 | 13 | 3 |
| 3 | 1 | 3 | 6 | 2 |
| 4 | 1 | 7 | 4 | 1 |

Final Page Table

| VPN | Valid | Physical Page # / Disk |
|-----|-------|------------------------|
| 0 | 1 | 5 |
| 1 | 1 | 13 |
| 2 | 1 | 14 |
| 3 | 1 | 6 |
| 4 | 1 | 9 |
| 5 | 1 | 11 |
| 6 | 0 | Disk |
| 7 | 1 | 4 |
| 8 | 0 | Disk |
| 9 | 0 | Disk |
| 10 | 1 | 3 |
| 11 | 1 | 12 |