Introduction

Neuroscience is undergoing a data-driven revolution. In laboratories around the world, optical tools are illuminating thousands of neurons at a time (Kerr and Denk, 2008). For some organisms, we can now monitor large fractions of the neurons in the brain (Ahrens et al., 2013; Prevedel et al., 2014; Lemon et al., 2015). Not long ago, this immense recording capability would have been mind-boggling to the average practitioner poking around in the dark, hoping to record from a handful of neurons. Complementing these recording capabilities, recent advances in connectomics — the mapping of synaptic connectivity (Sporns et al., 2005) — are providing a more complete atlas of the wiring diagram that underlies neural activity (Lichtman et al., 2008; Helmstaedter et al., 2013; Oh et al., 2014). Likewise, sophisticated monitoring and processing methods (e.g. Berman et al., 2014; Wiltschko et al., 2015) are providing rich measurements of the natural behavior that this activity gives rise to.

These unprecedented technological capabilities are leading to a fundamental paradigm shift. The scientific process of proposing hypotheses, testing them against experimental observations, and revising them accordingly, is becoming increasingly data-driven. Rather than collecting data to test a specific hypothesis, we can now collect large-scale recordings in relatively unstructured experimental setups (e.g. from freely behaving animals) and use statistical structure in the data to guide us toward hypotheses. Of course, there is no "free

lunch" — we must still specify what types of structure to look for. For example, when we cluster neuronal data we are hypothesizing that there are different types of neurons, and when we apply principal components analysis to neural population recordings we are assuming that neural activity reflects a low-dimensional latent state. As we move toward this more data-driven paradigm, we are presented with a challenge: how do we formulate models that capture our intuitions and hypotheses about neural computation, how do we fit these models to large scale recordings, and how do we revise our models based on what we have learned?

This thesis builds a sequence of modeling and inference tools to address this challenge. We build tools for analyzing *neural spike trains*, which are sequences of discrete events in time, and we use probabilistic models to compose flexible hypotheses that allow us to *discover structure* in the dynamics of spike trains. The workhorse of this process is a set of *Bayesian methods*, statistical inference algorithms that take in a neural recording and output a distribution over parameters and variables of our model. We begin by describing each of these these in turn.

I.I NEURONS, SPIKES, AND COMPUTATION

The human brain is a three pound ball of densely packed cells. It is soft, with a consistency like that of tofu. Amazingly, from this curd-like mass of cells, our mental faculties arise. About half of the roughly 170 billion cells in our brain are neurons, widely believed to be the fundamental units of computation (Dayan and Abbott, 2001). Neurons are electrically excitable cells that contain an ionic soup of charged atoms like sodium, potassium, and calcium, which together maintain a difference in electrical potential between the inside and the outside of the cell membrane (Kandel et al., 2000). When the membrane potential is excited above a certain threshold, a cascade of ion channels opens and closes, causing the membrane potential to undergo a characteristic action potential, or "spike."

The first challenge of deciphering neural computation is understanding how information is encoded in patterns of coordinated spiking activity across neural populations. To first approximation, spikes are fundamentally discrete events in time. That is, in a short enough window of time, a neuron either does or does not fire an action potential. Much

progress has been made in understanding how sensory neurons digitize continuous signals and how the activity of motor neurons innervates muscles and drives behavior (Rieke et al., 1999), yet how internal states, plans, goals, decisions, and thoughts are encoded remains largely a mystery.

The second challenge is understanding how this information is transformed over time. The neurons in our brain are connected by about 10^{14} synapses (Kandel et al., 2000). When a pre-synaptic neuron fires an action potential, neurotransmitters are released that then bind with receptors on the post-synaptic neuron, causing its ion channels to open and allowing current to flow into or out of the post-synaptic cell. These currents induce brief changes in the membrane potential of the downstream cell called post-synaptic potentials (PSPs). Depending on the direction of current, the PSP will be either excitatory, making the downstream neuron more likely to spike, or inhibitory, suppressing post-synaptic spiking. The probability of neurotransmitter release and the number of post-synaptic receptors together determine the "strength" of the synapse, which is manifest in the amplitude of the PSP (Cowan et al., 2003).

This web of synaptic connections imbues neural circuits with complex dynamics that govern how patterns of neural activity evolve over time, along with the information they encode. It is these dynamics that actually perform computation — the transformation of an input into an output. While these dynamics have been very well studied at the level of single connections between pairs of neurons, the dynamics of large networks of interconnected neurons is at the frontier of research.

Perhaps the most fundamental aspect of intelligence is our ability to learn, to store memories, and to generalize from past experience. In neural circuits, learning is most directly associated with the process of synaptic plasticity. In response to coordinated patterns of pre- and post-synaptic spiking, synapses adapt their strength. This synaptic plasticity leads to changes in the dynamics of neural circuits. In some cases, this plasticity leads to the creation of new associations that support generalization from noisy or partial sensory input. Thus, a third challenge of deciphering neural computation is understanding the processes of learning that cause neural dynamics to evolve in an activity-dependent manner.

Our goal, as neuroscientists, is to address these three challenges — encoding, dynamics, and learning — by searching for patterns in large-scale recordings of neural spike trains,

simultaneously recorded time series of spiking activity in populations of neurons. While this type of data is very hard to collect in humans, it is widely collected in worms, fish, flies, mice, rats, monkeys, and a host of other model organisms. Still, these model organisms have taught us a great deal about the workings of human brains and intelligence. This thesis does not focus on the unique aspects of any single organism or brain region, but rather on the general challenges associated with modeling structure in time series of discrete events that are common to all neural spike trains.

1.2 DISCOVERING STRUCTURE: Types, Features, Networks, and States

Discovering structure is primarily about finding meaningful abstractions. While neurons, spikes, and synapses are the elementary building blocks of many models of neural computation, our goal is to connect this level of detail to more abstract theories of computation. Just as our knowledge of *in silico* computation is partitioned into a hierarchy of concepts — from transistors, logic gates, pipelines and processors, to assembly code, operating systems, algorithms and programs — our knowledge of neural computation must also include a hierarchy of concepts and descriptions. Marr (1982) proposed three levels of abstraction: the computational level, which concerns the inputs and outputs of a system; the algorithmic level, which specifies the transformations between inputs and outputs; and the implementation level, which focuses on how these transformations are realized in neural substrates. From this perspective, our goal is to interpolate between neural spike trains, typically associated with implementation level descriptions, and higher level abstractions, like those hypothesized by algorithmic and computational theories. To do so, we compose our spike train models out of a set of simple motifs that appear over and over again in models of neural computation.

1.2.1 DISCRETE TYPES AND LOW-DIMENSIONAL FEATURES

Many successes of neuroscience have come from careful cataloging of neural types and features. From the earliest investigations of Ramón y Cajal, it has been clear that the brain is made up of anatomically distinct cell types (Cajal, 1899), but further classifications have been made on the basis of functional distinctions as well. Kuffler (1953) identified the re-

sponse properties of "on" and "off" ganglion cells in the retina, characterizing the ways in which these cells respond to light. His work which was carried on by his students, Hubel and Wiesel, who characterized simple and complex cells in visual cortex (Hubel and Wiesel, 1962), and eventually won the Nobel Prize for their work. These are pioneering examples of a common theme in neuroscience: clustering cells into discrete types that facilitate our understanding of neural computation. Indeed, the clustering of cells in the early visual pathway continues to this day (Macosko et al., 2015; Sanes and Masland, 2015).

Complementing these classic examples of discrete subtypes of neurons are similarly compelling examples of neurons characterized by continuous features. Most prominent among these are the place cells of the hippocampus (O'Keefe and Nadel, 1978). These cells fire selectively when an animal is in a particular location in its environment. Thus, each cell is naturally associated with a continuous position in space. As we seek to make sense of spike trains from other complex neural circuits, discrete latent types and continuous latent features form one of the core building blocks in our probabilistic modeling toolkit.

1.2.2 Networks and Dynamics

Networks play a central role in modern neuroscience: they enable us to reason about complex systems in terms of relationships among their constituent parts. Whether the nodes of the network represent individual neurons in a "connectome" (e.g. Sporns et al., 2005), populations of cells in a neural circuit (e.g. Felleman and Van Essen, 1991), voxels in an fMRI recording (e.g. Friston, 1994), or idealized neurons in a theoretical model (e.g. Hopfield, 1982), networks tell us about the pairwise relationships in large populations of nodes. Once we have extracted such a network, a great deal of intuition can be gleaned from its aggregate properties (Bullmore and Sporns, 2009; Newman, 2003). Moreover, the network itself can often be summarized in terms of latent types and features of nodes that govern how likely any pair of nodes is to be connected (Goldenberg et al., 2010).

We often use networks to represent the dynamics of systems. For example, an edge in the network may represent the influence that activity on one node exerts on the subsequent activity of another. In this way, networks provide a simple summary of complex dynamics. Much of this thesis is devoted to learning network representations from neural spike trains, building on a rich body of existing work on generalized linear models for neu-

ral spike trains (Paninski, 2004; Truccolo et al., 2005; Pillow et al., 2008). In these models, nodes correspond to the individual neurons in our dataset, and the edges represent a probabilistic relationship between the spiking activity of one neuron and the future firing rate of its downstream neighbors. By combining latent variable models for the network with dynamics models for its edges, this thesis will construct sophisticated, hierarchical models for dynamical spike trains.

1.2.3 LATENT STATES OF NEURAL POPULATIONS

Networks model dynamic data in terms of relationships between nodes, which are typically associated with individual neurons in the generalized linear model. In some cases, however, it is more natural to think about neural dynamics in terms of a latent state that evolves over time but cannot be directly observed. For example, population activity might reflect a low-dimensional, continuous latent state with smooth (Yu et al., 2009) or linear (Smith and Brown, 2003; Paninski et al., 2010) dynamics, or a discrete latent state with Markovian dynamics (e.g. Jones et al., 2007; Latimer et al., 2015). In these models, the firing rates of individual neurons are a function of the underlying latent state.

By combining these simple building blocks — latent types and features, networks, and dynamic latent states — we can express sophisticated hypotheses about the underlying structure in observed neural spike trains. However, in order to determine this structure, we need to instantiate these hypotheses in the form of a model that we can fit and evaluate. Bayesian probabilistic models and inference algorithms provide a principled means of tackling this problem.

1.3 A BAYESIAN APPROACH

Structural hypotheses specify how a set of parameters and latent variables give rise to patterns of neural activity. These hypotheses are naturally formalized in terms of probabilistic generative models, which provide an intuitive way of expressing the joint probability of parameters, latent variables, and observed data. Once formalized, we use the tools of Bayesian inference to compute the posterior distribution over parameters and latent variables implied by a given spike train and our prior beliefs, and use this posterior distribution to gain

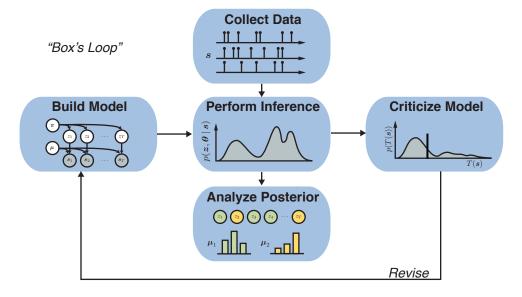


Figure 1.1: Box's loop for hypothesis driven probabilistic modeling. Adapted from Blei (2014).

insight into the structure of the data and potential shortcomings of our theories.

Recent decades have witnessed an explosion of interest in Bayesian machine learning methods, and the development of both theoretical and analytical tools have led to the widespread adoption of these techniques (Bishop, 2006; Murphy, 2012). Nevertheless, performing Bayesian inference in sophisticated models will always be a challenge. The art of probabilistic modeling lies in balancing two objectives: designing models that capture the details of the generative processes underlying our data, while simultaneously ensuring that these models admit efficient inference algorithms. To achieve this balance, we often look for model-specific structure that we can exploit during inference. This thesis is largely dedicated to developing algorithms that capitalize on the properties of models in order to efficiently scale to large recordings.

Figure 1.1 outlines the process of model building. We begin by collecting data, in this case, large-scale recordings of neural spike trains, and building a probabilistic model that captures our intuitions and hypotheses about structure in that data. Given these two ingredients, we perform Bayesian inference to compute the posterior distribution over structural variables and parameters. Visualizing, analyzing, and exploring this posterior often lead to

new insights and ways to think about generative processes that can explain further structure in the data. We can also criticize the model, formally, by assessing goodness-of-fit, evaluating predictive likelihoods, and performing posterior predictive checks (Gelman et al., 2013). This leads to new hypotheses, which in turn lead to new models and repetition of this process. Thus, model building is an interative process in which we are constantly adapting and refining hypotheses. Blei (2014), from whom this figure has been adapted, calls this "Box's loop," a reference to the foundational work of Box (1980).

We are certainly not the first to adopt a Bayesian approach to modeling of neural data. Indeed, probabilistic methods (e.g. Brillinger et al., 1976; Brillinger, 1988; Paninski, 2004; Truccolo et al., 2005; Pillow et al., 2008), particularly Bayesian methods (e.g. Sahani, 1999; Rieke et al., 1999; Yu et al., 2009; Park and Pillow, 2011; Macke et al., 2011), have played a major role in advancing our understanding of spike trains. We build on this foundation and specifically focus on expanding the set of models, combining standard point process and spike count models with hierarchical prior distributions that capture latent structure. To go along with these more sophisticated models, we also derive efficient* Bayesian inference algorithms that take advantage of clever data augmentation strategies. Together, these expand the repertoire of probabilistic models that we may leverage when looking for structure in neural data.

1.4 SUMMARY OF CONTRIBUTIONS

This thesis consists of a sequence of probabilistic models and inference algorithms that capture increasingly sophisticated structure in neural spike trains. While these models build upon one another, layering in additional structural hypotheses and incorporating more and more detail, the chapters can also be read independently without severe loss of clarity, especially by those who are more versed in machine learning.

We begin with a brief overview of point processes, probabilistic modeling, and Bayesian inference in Chapter 2. This lays the foundation for the methodological contributions in

^{*}We do not mean efficient in the formal, complexity-theoretic sense. Indeed, approximate Bayesian inference is, in the worst case, NP-hard (Dagum and Luby, 1993; Roth, 1996). We simply mean that the individual iterations of our algorithm can be performed in low-order polynomial time and that these algorithms yield good empirical results in a reasonable, if not provably polynomial, number of iterations.

the remainder of this thesis. We also introduce common notation for spike trains, firing rates, and latent variables of the model. Readers who are well versed in probabilistic modeling may skip this chapter without much harm.

Chapter 3 introduces our first probabilistic model for neural spike trains — a combination of continuous time Hawkes processes and probabilistic network models. This is based on Linderman and Adams (2014). However, since this is the first model of the thesis, we provide a more thorough discussion of network models, Hawkes processes, and the steps in deriving an efficient Markov chain Monte Carlo (MCMC) inference algorithm. This is also the only chapter that will apply these techniques to spike trains from domains other than neuroscience, specifically, from finance and criminology.

Chapter 4 continues the focus on Hawkes processes and networks, but here we break from the continuous time models of Chapter 3 and begin working in discrete time. The remainder of the thesis continues in this vein. This chapter also introduces a scalable variational inference algorithm that leverages the discrete model structure. This is based on Linderman and Adams (2015).

Chapter 5 reconsiders the linear interactions of Hawkes processes and develops a nonlinear autoregressive model for neural spike trains. Again, we use probabilistic network models as prior distributions over the pattern of functional interaction, and in doing so, show that interesting representations of neural populations can be learned directly from the data. The key to efficient inference is the Pólya-gamma augmentation — a recently developed method for performing Bayesian inference in models with linear Gaussian structure and discrete observations (Polson et al., 2013). A preliminary version of this work was presented by Linderman et al. (2015).

Chapter 6 continues the network theme, but here we begin to transition from static models to ones with dynamic latent states. Specifically, we adopt a mechanistic view of the network and treat its connections as actual synapses. This leads to a consideration of the evolution of synaptic weights over time. We construct a framework for modeling arbitrary synaptic plasticity rules and fitting them with particle MCMC. This chapter is based on Linderman et al. (2014).

Chapter 7 departs from network models and instead considers dynamical discrete state space models, specifically hidden Markov models (HMM), for neural data. We address

a major challenge in applying these well-known models, namely, selecting the number of latent states. By introducing a hierarchical Dirichlet process (HDP) prior and both an MCMC and a variational inference algorithm, we develop a Bayesian nonparametric solution to this problem. While this combination is relatively well studied, these models are notoriously sensitive to hyperparameter settings. Thus, we introduce a variety of methods for selecting hyperparameters and perform a thorough comparison on real and synthetic data. This is based on Linderman et al. (2016a).

Building on the discrete state space models of the preceding chapter, Chapter 8 develops efficient Bayesian inference algorithms for switching linear dynamical systems (SLDSs) with discrete count observations. The Pólya-gamma augmentation once again makes Bayesian inference surprisingly easy. Given these auxiliary variables, a host of tools for inference in Gaussian models is at our disposal. We then turn to a major problem, that of model comparison. We derive a novel sampling algorithm for the Pólya-gamma distribution that renders annealed importance sampling (AIS) simple and efficient for a broad class of models, including the SLDSs of this chapter. A preliminary version of this work was presented in Linderman et al. (2016b).

Chapter 9 takes a step in a radical direction. We build on the probabilistic models of the preceding chapters, but here we combine these models with a top-down theory of neural computation. Specifically, we consider the repercussions of the "Bayesian brain" hypothesis, namely, that neural circuits are performing approximate Bayesian inference in a probabilistic model of the world. We make predictions about the patterns of neural spike trains that would be expected from such a circuit, and show how the methods of previous chapters can be leveraged to reverse engineer probabilistic models from observations of neural spike trains. This work is necessarily speculative, but we believe it suggests a promising path forward as we seek to reconcile computational and algorithmic theories of neural computation with large scale recordings.

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