



## Common Distributions

This thesis makes use of a number of common distributions. The notation  $z \sim P(\theta)$  means that the random variable  $z$  is sampled from (or distributed according to) the distribution  $P$ , which is parameterized by  $\theta$ . When we write  $P(z \mid \theta)$  we refer to the density (assuming it exists) of  $P$  evaluated at  $z$ . Here, we provide a summary of common distributions and their parametric densities or mass functions.

### BERNOULLI

For a binary random variable  $x \in \{0, 1\}$  with  $\rho \in [0, 1]$ ,

$$\text{Bern}(x \mid \rho) = \rho^x (1 - \rho)^{1-x}.$$

### BETA

For a continuous random variable  $\rho \in [0, 1]$  with  $a > 0$  and  $b > 0$ ,

$$\text{Beta}(\rho \mid a, b) = \frac{\Gamma(a+b)}{\Gamma(a)\Gamma(b)} \rho^{a-1} (1-\rho)^{b-1}.$$

The beta distribution is a conjugate prior for the Bernoulli, binomial, and negative binomial distributions.

#### BINOMIAL

For an integer-valued random variable  $x \in \{1, \dots, N\}$  with  $N \in \mathbb{N}$  and  $\rho \in [0, 1]$ ,

$$\text{Bin}(x \mid N, \rho) = \binom{N}{x} \rho^x (1 - \rho)^{N-x}.$$

#### DIRICHLET

For a probability vector  $\boldsymbol{\pi} \in [0, 1]^K$  such that  $\pi_k \geq 0$  and  $\sum_k \pi_k = 1$ , and parameter  $\boldsymbol{\alpha} \in \mathbb{R}_+^K$ ,

$$\text{Dir}(\boldsymbol{\pi} \mid \boldsymbol{\alpha}) = \frac{\Gamma(\sum_{k=1}^K \alpha_k)}{\prod_{k=1}^K \Gamma(\alpha_k)} \prod_{k=1}^K \pi_k^{\alpha_k - 1}.$$

The Dirichlet distribution is a conjugate prior to the discrete and multinomial distributions.

#### DISCRETE

For a discrete random variable  $x \in \{1, \dots, K\}$  with  $K$  distinct outcomes, and a probability vector  $\boldsymbol{\pi} \in [0, 1]^K$  that is nonnegative and sums to one,

$$\text{Discrete}(x \mid \boldsymbol{\pi}) = \prod_{k=1}^K \pi_k^{\mathbb{I}[x=k]}.$$

#### GAMMA

For a nonnegative random variable  $\lambda \in \mathbb{R}_+$  with shape parameter  $a > 0$  and rate parameter  $b > 0$ ,

$$\text{Gamma}(\lambda \mid a, b) = \frac{b^a}{\Gamma(a)} \lambda^{a-1} e^{-b\lambda}.$$

The gamma distribution is the conjugate prior to the Poisson distribution, as well as to the rate parameter of the gamma distribution. The gamma distribution may also be parameterized in terms of a scale parameter,  $\theta = b^{-1}$ , but we do not use that parameterization in this thesis.

#### GAUSSIAN

For a random variable  $\mathbf{x} \in \mathbb{R}^D$  with mean  $\boldsymbol{\mu} \in \mathbb{R}^D$  and positive semidefinite covariance matrix  $\boldsymbol{\Sigma} \in \mathbb{R}^{D \times D}$ ,

$$\mathcal{N}(\mathbf{x} \mid \boldsymbol{\mu}, \boldsymbol{\Sigma}) = (2\pi)^{-D/2} |\boldsymbol{\Sigma}|^{-1/2} \exp \left\{ -\frac{1}{2} (\mathbf{x} - \boldsymbol{\mu})^\top \boldsymbol{\Sigma}^{-1} (\mathbf{x} - \boldsymbol{\mu}) \right\}.$$

#### MULTINOMIAL

For a vector of discrete counts  $\mathbf{x} \in \mathbb{N}^K$  with  $\sum_k x_k = N$  and a probability vector  $\boldsymbol{\pi} \in [0, 1]^K$ ,

$$\text{Mult}(\mathbf{x} \mid N, \boldsymbol{\pi}) = \binom{N}{x_1, x_2, \dots, x_K} \prod_{k=1}^K \pi_k^{x_k},$$

where

$$\binom{N}{x_1, x_2, \dots, x_K} = \frac{N!}{x_1! \dots x_K!}.$$

#### NEGATIVE BINOMIAL

For an integer-valued random variable  $x \in \mathbb{N}$  with shape parameters  $\nu \in \mathbb{R}_+$  and probability  $\rho \in [0, 1]$ ,

$$\text{NB}(x \mid \nu, \rho) = \binom{x + \nu - 1}{x} \rho^x (1 - \rho)^\nu.$$

## POISSON

For an integer random variable  $x \in \mathbb{N}$  and a nonnegative rate parameters  $\lambda \in \mathbb{R}_+$ ,

$$\text{Poisson}(x \mid \lambda) = \frac{1}{x!} \lambda^x e^{-\lambda}.$$

## UNIFORM

For a continuous random variable  $x \in \mathbb{R}$ ,

$$\text{Unif}(x \mid a, b) = \begin{cases} \frac{1}{b-a} & \text{if } a < x < b, \\ 0 & \text{o.w..} \end{cases}$$

## References

- Yashar Ahmadian, Jonathan W Pillow, and Liam Paninski. Efficient Markov chain Monte Carlo methods for decoding neural spike trains. *Neural Computation*, 23(1):46–96, 2011.
- Misha B Ahrens, Michael B Orger, Drew N Robson, Jennifer M Li, and Philipp J Keller. Whole-brain functional imaging at cellular resolution using light-sheet microscopy. *Nature methods*, 10(5):413–420, 2013.
- Laurence Aitchison and Peter E Latham. Synaptic sampling: A connection between PSP variability and uncertainty explains neurophysiological observations. *arXiv preprint arXiv:1505.04544*, 2015.
- Laurence Aitchison and Máté Lengyel. The Hamiltonian brain. *arXiv preprint arXiv:1407.0973*, 2014.
- David J Aldous. Representations for partially exchangeable arrays of random variables. *Journal of Multivariate Analysis*, 11(4):581–598, 1981.
- Charles H Anderson and David C Van Essen. Neurobiological computational systems. *Computational intelligence imitating life*, pages 1–11, 1994.
- Christophe Andrieu, Nando De Freitas, Arnaud Doucet, and Michael I Jordan. An introduction to MCMC for machine learning. *Machine learning*, 50(1-2):5–43, 2003.
- Christophe Andrieu, Arnaud Doucet, and Roman Holenstein. Particle Markov chain Monte Carlo methods. *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 72(3):269–342, 2010.
- Michael J Barber, John W Clark, and Charles H Anderson. Neural representation of probabilistic information. *Neural computation*, 15(8):1843–64, August 2003.
- Leonard E Baum and Ted Petrie. Statistical inference for probabilistic functions of finite state Markov chains. *The annals of mathematical statistics*, 37(6):1554–1563, 1966.

Matthew J. Beal, Zoubin Ghahramani, and Carl E. Rasmussen. The infinite hidden Markov model. In *Advances in Neural Information Processing Systems 14*, pages 577–585, Cambridge, MA, 2002. MIT Press.

Jeffrey M Beck and Alexandre Pouget. Exact inferences in a neural implementation of a hidden Markov model. *Neural computation*, 19(5):1344–1361, 2007.

Jeffrey M Beck, Peter E Latham, and Alexandre Pouget. Marginalization in neural circuits with divisive normalization. *The Journal of Neuroscience*, 31(43):15310–15319, 2011.

Jeffrey M Beck, Katherine A Heller, and Alexandre Pouget. Complex inference in neural circuits with probabilistic population codes and topic models. *Advances in Neural Information Processing Systems*, pages 1–9, 2012.

Yoshua Bengio and Paolo Frasconi. An input output HMM architecture. *Advances in neural information processing systems*, pages 427–434, 1995.

Pietro Berkes, Gergo Orbán, Máté Lengyel, and József Fiser. Spontaneous cortical activity reveals hallmarks of an optimal internal model of the environment. *Science*, 331(6013):83–7, January 2011.

Gordon J Berman, Daniel M Choi, William Bialek, and Joshua W Shaevitz. Mapping the stereotyped behaviour of freely moving fruit flies. *Journal of The Royal Society Interface*, 11(99):20140672, 2014.

Philippe Biane, Jim Pitman, and Marc Yor. Probability laws related to the Jacobi theta and Riemann zeta functions, and Brownian excursions. *Bulletin of the American Mathematical Society*, 38(4):435–465, 2001.

Christopher M Bishop. *Pattern Recognition and Machine Learning*. Springer, 2006.

David M Blei. Build, compute, critique, repeat: Data analysis with latent variable models. *Annual Review of Statistics and Its Application*, 1:203–232, 2014.

David M Blei, Andrew Y Ng, and Michael I Jordan. Latent Dirichlet allocation. *the Journal of Machine Learning Research*, 3:993–1022, 2003.

Carolyn R Block and Richard Block. *Street gang crime in Chicago*. US Department of Justice, Office of Justice Programs, National Institute of Justice, 1993.

Carolyn R Block, Richard Block, and Illinois Criminal Justice Information Authority. Homicides in Chicago, 1965-1995. ICPSR06399-v5. Ann Arbor, MI: Inter-university Consortium for Political and Social Research [distributor], July 2005.

Charles Blundell, Katherine A Heller, and Jeffrey M Beck. Modelling reciprocating relationships with Hawkes processes. *Advances in Neural Information Processing Systems*, 2012.

George EP Box. Sampling and Bayes' inference in scientific modelling and robustness. *Journal of the Royal Statistical Society. Series A (General)*, pages 383–430, 1980.

David H Brainard and William T Freeman. Bayesian color constancy. *JOSA A*, 14(7):1393–1411, 1997.

Kevin L Briggman, Henry DI Abarbanel, and William B Kristan. Optical imaging of neuronal populations during decision-making. *Science*, 307(5711):896–901, 2005.

David R. Brillinger. Maximum likelihood analysis of spike trains of interacting nerve cells. *Biological Cybernetics*, 59(3):189–200, August 1988.

David R Brillinger, Hugh L Bryant Jr, and Jose P Segundo. Identification of synaptic interactions. *Biological cybernetics*, 22(4):213–228, 1976.

Michael Bryant and Erik B Sudderth. Truly nonparametric online variational inference for hierarchical Dirichlet processes. In *Advances in Neural Information Processing Systems 25*, pages 2699–2707, 2012.

Lars Buesing, Johannes Bill, Bernhard Nessler, and Wolfgang Maass. Neural dynamics as sampling: a model for stochastic computation in recurrent networks of spiking neurons. *PLoS computational biology*, 7(11):e1002211, November 2011.

Lars Buesing, Jakob H. Macke, and Maneesh Sahani. Learning stable, regularised latent models of neural population dynamics. *Network: Computation in Neural Systems*, 23: 24–47, 2012a.

Lars Buesing, Jakob H Macke, and Maneesh Sahani. Spectral learning of linear dynamics from generalised-linear observations with application to neural population data. In *Advances in neural information processing systems*, pages 1682–1690, 2012b.

Lars Buesing, Timothy A Machado, John P Cunningham, and Liam Paninski. Clustered factor analysis of multineuronal spike data. In *Advances in Neural Information Processing Systems*, pages 3500–3508, 2014.

Ed Bullmore and Olaf Sporns. Complex brain networks: graph theoretical analysis of structural and functional systems. *Nature Reviews Neuroscience*, 10(3):186–198, 2009.

Santiago Ramón Cajal. *Textura del Sistema Nervioso del Hombre y los Vertebrados*, volume 1. Imprenta y Librería de Nicolás Moya, Madrid, Spain, 1899.

Natalia Caporale and Yang Dan. Spike timing-dependent plasticity: a Hebbian learning rule. *Annual Review of Neuroscience*, 31:25–46, 2008.

Nick Chater and Christopher D Manning. Probabilistic models of language processing and acquisition. *Trends in cognitive sciences*, 10(7):335–344, 2006.

Zhe Chen, Fabian Kloosterman, Emery N Brown, and Matthew A Wilson. Uncovering spatial topology represented by rat hippocampal population neuronal codes. *Journal of Computational Neuroscience*, 33(2):227–255, 2012.

Zhe Chen, Stephen N Gomperts, Jun Yamamoto, and Matthew A Wilson. Neural representation of spatial topology in the rodent hippocampus. *Neural Computation*, 26(1):1–39, 2014.

Sharat Chikkerur, Thomas Serre, Cheston Tan, and Tomaso Poggio. What and where: A Bayesian inference theory of attention. *Vision research*, 50(22):2233–2247, 2010.

Yoon Sik Cho, Aram Galstyan, Jeff Brantingham, and George Tita. Latent point process models for spatial-temporal networks. *arXiv:1302.2671*, 2013.

International Human Genome Sequencing Consortium et al. Finishing the euchromatic sequence of the human genome. *Nature*, 431(7011):931–945, 2004.



Aaron C Courville, Nathaniel D Daw, and David S Touretzky. Bayesian theories of conditioning in a changing world. *Trends in cognitive sciences*, 10(7):294–300, 2006.

Ronald L Cowan and Charles J Wilson. Spontaneous firing patterns and axonal projections of single corticostriatal neurons in the rat medial agranular cortex. *Journal of neurophysiology*, 71(1):17–32, 1994.

W Maxwell Cowan, Thomas C Südhof, and Charles F Stevens. *Synapses*. Johns Hopkins University Press, 2003.

Mary Kathryn Cowles and Bradley P Carlin. Markov chain Monte Carlo convergence diagnostics: a comparative review. *Journal of the American Statistical Association*, 91: 883–904, 1996.

John P Cunningham and Byron M Yu. Dimensionality reduction for large-scale neural recordings. *Nature neuroscience*, 17(11):1500–1509, 2014.

Paul Dagum and Michael Luby. Approximating probabilistic inference in Bayesian belief networks is NP-hard. *Artificial intelligence*, 60(1):141–153, 1993.

Daryl J Daley and David Vere-Jones. *An introduction to the theory of point processes: Volume I: Elementary Theory and Methods*. Springer Science & Business Media, 2 edition, 2003.

Peter Dayan and Larry F Abbott. *Theoretical neuroscience: Computational and mathematical modeling of neural systems*. MIT Press, 2001.

Peter Dayan and Joshua A Solomon. Selective Bayes: Attentional load and crowding. *Vision research*, 50(22):2248–2260, 2010.

Arthur P Dempster, Nan M Laird, and Donald B Rubin. Maximum likelihood from incomplete data via the EM algorithm. *Journal of the Royal Statistical Society. Series B (Methodological)*, pages 1–38, 1977.

Sophie Deneve. Bayesian spiking neurons I: inference. *Neural computation*, 20(1):91–117, January 2008.

Luc Devroye. *Non-Uniform Random Variate Generation*. Springer-Verlag, New York, USA, 1986.

Christopher DuBois, Carter Butts, and Padhraic Smyth. Stochastic block modeling of relational event dynamics. In *Proceedings of the Sixteenth International Conference on Artificial Intelligence and Statistics*, pages 238–246, 2013.

Seif Eldawlatly, Yang Zhou, Rong Jin, and Karim G Oweiss. On the use of dynamic Bayesian networks in reconstructing functional neuronal networks from spike train ensembles. *Neural Computation*, 22(1):158–189, 2010.

Marc O Ernst and Martin S Banks. Humans integrate visual and haptic information in a statistically optimal fashion. *Nature*, 415(6870):429–433, 2002.

Sean Escola, Alfredo Fontanini, Don Katz, and Liam Paninski. Hidden Markov models for the stimulus-response relationships of multistate neural systems. *Neural computation*, 23(5):1071–1132, 2011.

Warren John Ewens. Population genetics theory—the past and the future. In S. Lessard, editor, *Mathematical and Statistical Developments of Evolutionary Theory*, pages 177–227. Springer, 1990.

Daniel E Feldman. The spike-timing dependence of plasticity. *Neuron*, 75(4):556–71, August 2012.

Daniel J Felleman and David C Van Essen. Distributed hierarchical processing in the primate cerebral cortex. *Cerebral cortex*, 1(1):1–47, 1991.

Thomas S Ferguson. A Bayesian analysis of some nonparametric problems. *The Annals of Statistics*, pages 209–230, 1973.

Christopher R Fetsch, Amanda H Turner, Gregory C DeAngelis, and Dora E Angelaki. Dynamic reweighting of visual and vestibular cues during self-motion perception. *The Journal of Neuroscience*, 29(49):15601–15612, 2009.

- Christopher R Fetsch, Alexandre Pouget, Gregory C DeAngelis, and Dora E Angelaki. Neural correlates of reliability-based cue weighting during multisensory integration. *Nature neuroscience*, 15(1):146–154, 2012.
- József Fiser, Pietro Berkes, Gergő Orbán, and Máté Lengyel. Statistically optimal perception and learning: from behavior to neural representations. *Trends in cognitive sciences*, 14(3):119–130, 2010.
- Alyson K Fletcher, Sundeeep Rangan, Lav R Varshney, and Aniruddha Bhargava. Neural reconstruction with approximate message passing (neuramp). In *Advances in neural information processing systems*, pages 2555–2563, 2011.
- Emily B Fox. *Bayesian nonparametric learning of complex dynamical phenomena*. PhD thesis, Massachusetts Institute of Technology, 2009.
- Emily B Fox, Erik B Sudderth, Michael I Jordan, and Alan S Willsky. An HDP-HMM for systems with state persistence. In *Proceedings of the 25th International Conference on Machine learning*, pages 312–319, 2008.
- Jeremy Freeman, Greg D Field, Peter H Li, Martin Greschner, Deborah E Gunning, Keith Mathieson, Alexander Sher, Alan M Litke, Liam Paninski, Eero P Simoncelli, et al. Mapping nonlinear receptive field structure in primate retina at single cone resolution. *eLife*, 4:e05241, 2015.
- Karl Friston. The free-energy principle: a unified brain theory? *Nature reviews. Neuroscience*, 11(2):127–38, February 2010.
- Karl J Friston. Functional and effective connectivity in neuroimaging: a synthesis. *Human brain mapping*, 2(1-2):56–78, 1994.
- Deep Ganguli and Eero P Simoncelli. Implicit encoding of prior probabilities in optimal neural populations. *Advances in Neural Information Processing Systems*, pages 6–9, 2010.
- Peiran Gao and Surya Ganguli. On simplicity and complexity in the brave new world of large-scale neuroscience. *Current opinion in neurobiology*, 32:148–155, 2015.

- Andrew Gelman, John B Carlin, Hal S Stern, David B Dunson, Aki Vehtari, and Donald B Rubin. *Bayesian Data Analysis*. CRC press, 3rd edition, 2013.
- Stuart Geman and Donald Geman. Stochastic relaxation, Gibbs distributions, and the Bayesian restoration of images. *Pattern Analysis and Machine Intelligence, IEEE Transactions on*, (6):721–741, 1984.
- Felipe Gerhard, Tilman Kispersky, Gabrielle J Gutierrez, Eve Marder, Mark Kramer, and Uri Eden. Successful reconstruction of a physiological circuit with known connectivity from spiking activity alone. *PLoS Computational Biology*, 9(7):e1003138, 2013.
- Samuel J Gershman, Matthew D Hoffman, and David M Blei. Nonparametric variational inference. *Proceedings of the 29th International Conference on Machine Learning*, pages 663–670, 2012a.
- Samuel J Gershman, Edward Vul, and Joshua B Tenenbaum. Multistability and perceptual inference. *Neural computation*, 24(1):1–24, 2012b.
- Sebastian Gerwinn, Jakob Macke, Matthias Seeger, and Matthias Bethge. Bayesian inference for spiking neuron models with a sparsity prior. In *Proceedings of the 21st Annual Conference on Neural Information Processing Systems*, pages 529–536, 2008.
- Charles J Geyer. Practical Markov Chain Monte Carlo. *Statistical Science*, pages 473–483, 1992.
- Walter R Gilks. *Markov Chain Monte Carlo*. Wiley Online Library, 2005.
- Anna Goldenberg, Alice X Zheng, Stephen E Fienberg, and Edoardo M Airolidi. A survey of statistical network models. *Foundations and Trends in Machine Learning*, 2(2):129–233, 2010.
- Manuel Gomez-Rodriguez, Jure Leskovec, and Andreas Krause. Inferring networks of diffusion and influence. In *Proceedings of the 16th ACM SIGKDD International Conference on Knowledge Discovery and Data Mining*, pages 1019–1028. ACM, 2010.

Noah Goodman, Vikash Mansinghka, Daniel M Roy, Keith Bonawitz, and Joshua B Tenenbaum. Church: a language for generative models. *Proceedings of the 24th Conference on Uncertainty in Artificial Intelligence*, pages 220–229, 2008.

Noah D Goodman, Joshua B Tenenbaum, and Tobias Gerstenberg. Concepts in a probabilistic language of thought. Technical report, Center for Brains, Minds and Machines (CBMM), 2014.

Agnieszka Grabska-Barwinska, Jeff Beck, Alexandre Pouget, and Peter Latham. Demixing odors-fast inference in olfaction. In *Advances in Neural Information Processing Systems*, pages 1968–1976, 2013.

SG Gregory, KF Barlow, KE McLay, R Kaul, D Swarbreck, A Dunham, CE Scott, KL Howe, K Woodfine, CCA Spencer, et al. The DNA sequence and biological annotation of human chromosome 1. *Nature*, 441(7091):315–321, 2006.

Thomas L Griffiths, Charles Kemp, and Joshua B Tenenbaum. Bayesian models of cognition. In Ron Sun, editor, *The Cambridge Handbook of Computational Psychology*. Cambridge University Press, 2008.

Roger B Grosse, Chris J Maddison, and Ruslan R Salakhutdinov. Annealing between distributions by averaging moments. In *Advances in Neural Information Processing Systems*, pages 2769–2777, 2013.

Roger B Grosse, Zoubin Ghahramani, and Ryan P Adams. Sandwiching the marginal likelihood using bidirectional Monte Carlo. *arXiv preprint arXiv:1511.02543*, 2015.

Yong Gu, Dora E Angelaki, and Gregory C DeAngelis. Neural correlates of multisensory cue integration in macaque MSTd. *Nature neuroscience*, 11(10):1201–1210, 2008.

Fangjian Guo, Charles Blundell, Hanna Wallach, and Katherine A Heller. The Bayesian echo chamber: Modeling influence in conversations. *arXiv preprint arXiv:1411.2674*, 2014.

Alan G Hawkes. Spectra of some self-exciting and mutually exciting point processes. *Biometrika*, 58(1):83, 1971.

Moritz Helmstaedter, Kevin L Briggman, Srinivas C Turaga, Viren Jain, H Sebastian Seung, and Winfried Denk. Connectomic reconstruction of the inner plexiform layer in the mouse retina. *Nature*, 500(7461):168–174, 2013.

Geoffrey E Hinton. How neural networks learn from experience. *Scientific American*, 1992.

Geoffrey E Hinton and Terrence J Sejnowski. Optimal perceptual inference. In *Proceedings of the IEEE conference on Computer Vision and Pattern Recognition, Washington DC*, 1983.

Daniel R Hochbaum, Yongxin Zhao, Samouil L Farhi, Nathan Klapoetke, Christopher A Werley, Vikrant Kapoor, Peng Zou, Joel M Kralj, Dougal Maclaurin, Niklas Smedemark-Margulies, et al. All-optical electrophysiology in mammalian neurons using engineered microbial rhodopsins. *Nature methods*, 2014.

Peter D Hoff. Modeling homophily and stochastic equivalence in symmetric relational data. *Advances in Neural Information Processing Systems 20*, 20:1–8, 2008.

Matthew D Hoffman, David M Blei, Chong Wang, and John Paisley. Stochastic variational inference. *The Journal of Machine Learning Research*, 14(1):1303–1347, 2013.

Douglas N. Hoover. Relations on probability spaces and arrays of random variables. *Technical report, Institute for Advanced Study, Princeton*, 1979.

John J Hopfield. Neural networks and physical systems with emergent collective computational abilities. *Proceedings of the national academy of sciences*, 79(8):2554–2558, 1982.

Patrik O Hoyer and Aapo Hyvarinen. Interpreting neural response variability as Monte Carlo sampling of the posterior. *Advances in neural information processing systems*, pages 293–300, 2003.

Yanping Huang and Rajesh P. N. Rao. Predictive coding. *Wiley Interdisciplinary Reviews: Cognitive Science*, 2(5):580–593, September 2011.

David H Hubel and Torsten N Wiesel. Receptive fields, binocular interaction and functional architecture in the cat’s visual cortex. *The Journal of physiology*, 160(1):106–154, 1962.

Hemant Ishwaran and Mahmoud Zarepour. Exact and approximate sum representations for the Dirichlet process. *Canadian Journal of Statistics*, 30(2):269–283, 2002.

Tomoharu Iwata, Amar Shah, and Zoubin Ghahramani. Discovering latent influence in online social activities via shared cascade Poisson processes. In *Proceedings of the 19th ACM SIGKDD International Conference on Knowledge Discovery and Data Mining*, pages 266–274. ACM, 2013.

Mehrdad Jazayeri and Michael N Shadlen. Temporal context calibrates interval timing. *Nature neuroscience*, 13(8):1020–1026, 2010.

Mehrdad Jazayeri and Michael N Shadlen. A neural mechanism for sensing and reproducing a time interval. *Current Biology*, 25(20):2599–2609, 2015.

Matthew J Johnson. *Bayesian time series models and scalable inference*. PhD thesis, Massachusetts Institute of Technology, June 2014.

Matthew J Johnson and Alan S Willsky. Bayesian nonparametric hidden semi-Markov models. *Journal of Machine Learning Research*, 14(1):673–701, 2013.

Matthew J Johnson and Alan S Willsky. Stochastic variational inference for Bayesian time series models. *Proceedings of the 31st International Conference on Machine Learning*, 32:1854–1862, 2014.

Matthew J Johnson, Scott W Linderman, Sandeep R Datta, and Ryan P Adams. Discovering switching autoregressive dynamics in neural spike train recordings. *Computational and Systems Neuroscience (Cosyne) Abstracts*, 2015.

Lauren M Jones, Alfredo Fontanini, Brian F Sadacca, Paul Miller, and Donald B Katz. Natural stimuli evoke dynamic sequences of states in sensory cortical ensembles. *Proceedings of the National Academy of Sciences*, 104(47):18772–18777, 2007.

Michael I Jordan, Zoubin Ghahramani, Tommi S Jaakkola, and Lawrence K Saul. An introduction to variational methods for graphical models. *Machine learning*, 37(2):183–233, 1999.

- Eric R Kandel, James H Schwartz, Thomas M Jessell, et al. *Principles of neural science*, volume 4. McGraw-Hill New York, 2000.
- David Kappel, Stefan Habenschuss, Robert Legenstein, and Wolfgang Maass. Network plasticity as Bayesian inference. *PLoS Computational Biology*, 11(11):e1004485, 2015a.
- David Kappel, Stefan Habenschuss, Robert Legenstein, and Wolfgang Maass. Synaptic sampling: A Bayesian approach to neural network plasticity and rewiring. In *Advances in Neural Information Processing Systems*, pages 370–378, 2015b.
- Robert E Kass and Adrian E Raftery. Bayes factors. *Journal of the American Statistical Association*, 90(430):773–795, 1995.
- Jason ND Kerr and Winfried Denk. Imaging in vivo: watching the brain in action. *Nature Reviews Neuroscience*, 9(3):195–205, 2008.
- Roozbeh Kiani and Michael N Shadlen. Representation of confidence associated with a decision by neurons in the parietal cortex. *Science*, 324(5928):759–64, May 2009.
- John F. C. Kingman. *Poisson Processes (Oxford Studies in Probability)*. Oxford University Press, January 1993. ISBN 0198536933.
- David C Knill and Whitman Richards. *Perception as Bayesian inference*. Cambridge University Press, 1996.
- Konrad P Körding and Daniel M Wolpert. Bayesian integration in sensorimotor learning. *Nature*, 427(6971):244–7, January 2004.
- Alp Kucukelbir, Rajesh Ranganath, Andrew Gelman, and David Blei. Automatic variational inference in Stan. In *Advances in Neural Information Processing Systems*, pages 568–576, 2015.
- Stephen W Kuffler. Discharge patterns and functional organization of mammalian retina. *Journal of neurophysiology*, 16(1):37–68, 1953.
- Harold W Kuhn. The Hungarian method for the assignment problem. *Naval research logistics quarterly*, 2(1-2):83–97, 1955.



- Kenneth W Latimer, Jacob L Yates, Miriam LR Meister, Alexander C Huk, and Jonathan W Pillow. Single-trial spike trains in parietal cortex reveal discrete steps during decision-making. *Science*, 349(6244):184–187, 2015.
- Tai Sing Lee and David Mumford. Hierarchical Bayesian inference in the visual cortex. *JOSA A*, 20(7):1434–1448, 2003.
- Robert Legenstein and Wolfgang Maass. Ensembles of spiking neurons with noise support optimal probabilistic inference in a dynamically changing environment. *PLoS Comput Biol*, 10(10):e1003859, 2014.
- William C Lemon, Stefan R Pulver, Burkhard Hockendorf, Katie McDole, Kristin Branson, Jeremy Freeman, and Philipp J Keller. Whole-central nervous system functional imaging in larval *Drosophila*. *Nature communications*, 6, 2015.
- Michael S Lewicki. A review of methods for spike sorting: the detection and classification of neural action potentials. *Network: Computation in Neural Systems*, 9(4):R53–R78, 1998.
- Percy Liang, Slav Petrov, Michael I Jordan, and Dan Klein. The infinite PCFG using hierarchical Dirichlet processes. In *Proceedings of Empirical Methods in Natural Language Processing*, pages 688–697, 2007.
- David Liben-Nowell and Jon Kleinberg. The link-prediction problem for social networks. *Journal of the American society for information science and technology*, 58(7):1019–1031, 2007.
- Jeff W Lichtman, Jean Livet, and Joshua R Sanes. A technicolour approach to the connectome. *Nature Reviews Neuroscience*, 9(6):417–422, 2008.
- Scott W Linderman and Ryan P. Adams. Discovering latent network structure in point process data. In *Proceedings of the 31st International Conference on Machine Learning*, pages 1413–1421, 2014.
- Scott W Linderman and Ryan P Adams. Scalable Bayesian inference for excitatory point process networks. *arXiv preprint arXiv:1507.03228*, 2015.

Scott W Linderman and Ryan P Johnson, Matthew Jand Adams. Dependent multinomial models made easy: Stick-breaking with the Pólya-gamma augmentation. In *Advances in Neural Information Processing Systems*, pages 3438–3446, 2015.

Scott W Linderman, Christopher H Stock, and Ryan P Adams. A framework for studying synaptic plasticity with neural spike train data. In *Advances in Neural Information Processing Systems*, pages 2330–2338, 2014.

Scott W Linderman, Ryan P Adams, and Jonathan W Pillow. Inferring structured connectivity from spike trains under negative-binomial generalized linear models. *Computational and Systems Neuroscience (Cosyne) Abstracts*, 2015.

Scott W Linderman, Matthew J Johnson, Matthew W Wilson, and Zhe Chen. A nonparametric Bayesian approach to uncovering rat hippocampal population codes during spatial navigation. *Journal of Neuroscience Methods*, 263:36–47, 2016a.

Scott W Linderman, Aaron Tucker, and Matthew J Johnson. Bayesian latent state space models of neural activity. *Computational and Systems Neuroscience (Cosyne) Abstracts*, 2016b.

Fredrik Lindsten, Michael I Jordan, and Thomas B Schön. Ancestor sampling for particle Gibbs. In *Advances in Neural Information Processing Systems*, pages 2600–2608, 2012.

Shai Litvak and Shimon Ullman. Cortical circuitry implementing graphical models. *Neural computation*, 21(11):3010–3056, 2009.

James Robert Lloyd, Peter Orbanz, Zoubin Ghahramani, and Daniel M Roy. Random function priors for exchangeable arrays with applications to graphs and relational data. *Advances in Neural Information Processing Systems*, 2012.

Wei Ji Ma and Mehrdad Jazayeri. Neural coding of uncertainty and probability. *Annual review of neuroscience*, 37:205–220, 2014.

Wei Ji Ma, Jeffrey M Beck, Peter E Latham, and Alexandre Pouget. Bayesian inference with probabilistic population codes. *Nature neuroscience*, 9(11):1432–8, November 2006.

David JC MacKay. Bayesian interpolation. *Neural computation*, 4(3):415–447, 1992.

Jakob H Macke, Lars Buesing, John P Cunningham, M Yu Byron, Krishna V Shenoy, and Maneesh Sahani. Empirical models of spiking in neural populations. In *Advances in neural information processing systems*, pages 1350–1358, 2011.

Evan Z Macosko, Anindita Basu, Rahul Satija, James Nemesh, Karthik Shekhar, Melissa Goldman, Itay Tirosh, Allison R Bialas, Nolan Kamitaki, Emily M Martersteck, et al. Highly parallel genome-wide expression profiling of individual cells using nanoliter droplets. *Cell*, 161(5):1202–1214, 2015.

Vikash Mansinghka, Daniel Selsam, and Yura Perov. Venture: a higher-order probabilistic programming platform with programmable inference. *arXiv preprint arXiv:1404.0099*, 2014.

David Marr. *Vision: A computational investigation into the human representation and processing of visual information*. MIT Press, 1982.

Paul Miller and Donald B Katz. Stochastic transitions between neural states in taste processing and decision-making. *The Journal of Neuroscience*, 30(7):2559–2570, 2010.

T. J. Mitchell and J. J. Beauchamp. Bayesian variable selection in linear regression. *Journal of the American Statistical Association*, 83(404):1023–1032, 1988.

Shakir Mohamed, Zoubin Ghahramani, and Katherine A Heller. Bayesian and L1 approaches for sparse unsupervised learning. In *Proceedings of the 29th International Conference on Machine Learning*, pages 751–758, 2012.

Jesper Møller, Anne Randi Syversveen, and Rasmus Plenge Waagepetersen. Log Gaussian Cox processes. *Scandinavian Journal of Statistics*, 25(3):451–482, 1998.

Michael L Morgan, Gregory C DeAngelis, and Dora E Angelaki. Multisensory integration in macaque visual cortex depends on cue reliability. *Neuron*, 59(4):662–673, 2008.

Abigail Morrison, Markus Diesmann, and Wulfram Gerstner. Phenomenological models of synaptic plasticity based on spike timing. *Biological cybernetics*, 98(6):459–478, 2008.

Kevin P Murphy. *Machine learning: a probabilistic perspective*. MIT press, 2012.

Radford M Neal. Annealed importance sampling. *Statistics and Computing*, 11(2):125–139, 2001.

Radford M. Neal. MCMC using Hamiltonian dynamics. *Handbook of Markov Chain Monte Carlo*, pages 113–162, 2010.

John A Nelder and R Jacob Baker. Generalized linear models. *Encyclopedia of Statistical Sciences*, 1972.

Bernhard Nessler, Michael Pfeiffer, Lars Buesing, and Wolfgang Maass. Bayesian computation emerges in generic cortical microcircuits through spike-timing-dependent plasticity. *PLoS Computational Biology*, 9(4):e1003037, 2013.

Mark EJ Newman. The structure and function of complex networks. *SIAM review*, 45(2):167–256, 2003.

Krzysztof Nowicki and Tom A B Snijders. Estimation and prediction for stochastic block-structures. *Journal of the American Statistical Association*, 96(455):1077–1087, 2001.

Seung Wook Oh, Julie A Harris, Lydia Ng, Brent Winslow, Nicholas Cain, Stefan Mihalas, Quanxin Wang, Chris Lau, Leonard Kuan, Alex M Henry, et al. A mesoscale connectome of the mouse brain. *Nature*, 508(7495):207–214, 2014.

Erkki Oja. Simplified neuron model as a principal component analyzer. *Journal of Mathematical Biology*, 15(3):267–273, 1982.

John O’Keefe and Lynn Nadel. *The Hippocampus as a Cognitive Map*, volume 3. Clarendon Press, 1978.

Peter Orbanz and Daniel M Roy. Bayesian models of graphs, arrays and other exchangeable random structures. *Pattern Analysis and Machine Intelligence, IEEE Transactions on*, 37(2):437–461, 2015.

Peter Orbanz and Yee Whye Teh. Bayesian nonparametric models. In *Encyclopedia of Machine Learning*, pages 81–89. Springer, 2011.

Adam M Packer, Darcy S Peterka, Jan J Hirtz, Rohit Prakash, Karl Deisseroth, and Rafael Yuste. Two-photon optogenetics of dendritic spines and neural circuits. *Nature methods*, 9(12):1202–1205, 2012.

Liam Paninski. Maximum likelihood estimation of cascade point-process neural encoding models. *Network: Computation in Neural Systems*, 15(4):243–262, January 2004.

Liam Paninski, Yashar Ahmadian, Daniel Gil Ferreira, Shinsuke Koyama, Kamiar Rahnama Rad, Michael Vidne, Joshua Vogelstein, and Wei Wu. A new look at state-space models for neural data. *Journal of computational neuroscience*, 29(1-2):107–126, 2010.

Andrew V Papachristos. Murder by structure: Dominance relations and the social structure of gang homicide. *American Journal of Sociology*, 115(1):74–128, 2009.

Il Memming Park and Jonathan W Pillow. Bayesian spike-triggered covariance analysis. In *Advances in neural information processing systems*, pages 1692–1700, 2011.

Patrick O Perry and Patrick J Wolfe. Point process modelling for directed interaction networks. *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 2013.

Biljana Petreska, Byron Yu, John P Cunningham, Gopal Santhanam, Stephen I Ryu, Krishna V Shenoy, and Maneesh Sahani. Dynamical segmentation of single trials from population neural data. In *Neural Information Processing Systems*, pages 756–764, 2011.

David Pfau, Eftychios A Pnevmatikakis, and Liam Paninski. Robust learning of low-dimensional dynamics from large neural ensembles. In *Advances in neural information processing systems*, pages 2391–2399, 2013.

Jonathan W. Pillow and James Scott. Fully Bayesian inference for neural models with negative-binomial spiking. In *Advances in Neural Information Processing Systems*, pages 1898–1906, 2012.

Jonathan W Pillow, Jonathon Shlens, Liam Paninski, Alexander Sher, Alan M Litke, EJ Chichilnisky, and Eero P Simoncelli. Spatio-temporal correlations and visual signalling in a complete neuronal population. *Nature*, 454(7207):995–999, 2008.

Eftychios A Pnevmatikakis, Daniel Soudry, Yuanjun Gao, Timothy A Machado, Josh Merel, David Pfau, Thomas Reardon, Yu Mu, Clay Lacefield, Weijian Yang, et al. Simultaneous denoising, deconvolution, and demixing of calcium imaging data. *Neuron*, 2016.

Nicholas G Polson, James G Scott, and Jesse Windle. Bayesian inference for logistic models using Pólya-gamma latent variables. *Journal of the American Statistical Association*, 108(504):1339–1349, 2013.

Ruben Portugues, Claudia E Feierstein, Florian Engert, and Michael B Orger. Whole-brain activity maps reveal stereotyped, distributed networks for visuomotor behavior. *Neuron*, 81(6):1328–1343, 2014.

Alexandre Pouget, Jeffrey M Beck, Wei Ji Ma, and Peter E Latham. Probabilistic brains: knowns and unknowns. *Nature neuroscience*, 16(9):1170–1178, 2013.

Robert Prevedel, Young-Gyu Yoon, Maximilian Hoffmann, Nikita Pak, Gordon Wetstein, Saul Kato, Tina Schrödel, Ramesh Raskar, Manuel Zimmer, Edward S Boyden, et al. Simultaneous whole-animal 3d imaging of neuronal activity using light-field microscopy. *Nature methods*, 11(7):727–730, 2014.

Lawrence R Rabiner. A tutorial on hidden Markov models and selected applications in speech recognition. *Proceedings of the IEEE*, 77(2):257–286, 1989.

Adrian E Raftery and Steven Lewis. How many iterations in the Gibbs sampler? In J. M. Bernardo, J. Berger, A. P. Dawid, and A. F. M. Smith, editors, *Bayesian Statistics*, pages 763–773. Oxford University Press, 1992.

Rajesh Ranganath, Sean Gerrish, and David M Blei. Black box variational inference. *17th International Conference on Artificial Intelligence and Statistics*, 33:275–283, 2014.

Rajesh P. N. Rao. Bayesian computation in recurrent neural circuits. *Neural computation*, 16(1):1–38, January 2004.

Rajesh P. N. Rao. Neural models of Bayesian belief propagation. In *Bayesian brain: Probabilistic approaches to neural computation*, pages 236–264. MIT Press Cambridge, MA, 2007.

Rajesh P. N. Rao and Dana H Ballard. Predictive coding in the visual cortex: a functional interpretation of some extra-classical receptive-field effects. *Nature neuroscience*, 2(1):79–87, January 1999.

Danilo J Rezende, Daan Wierstra, and Wulfram Gerstner. Variational learning for recurrent spiking networks. In *Advances in Neural Information Processing Systems*, pages 136–144, 2011.

Fred Rieke, David Warland, Rob de Ruyter van Steveninck, and William Bialek. *Spikes: exploring the neural code*. MIT press, 1999.

Christian Robert and George Casella. *Monte Carlo statistical methods*. Springer Science & Business Media, 2013.

Dan Roth. On the hardness of approximate reasoning. *Artificial Intelligence*, 82(1):273–302, 1996.

Maneesh Sahani. *Latent variable models for neural data analysis*. PhD thesis, California Institute of Technology, 1999.

Maneesh Sahani and Peter Dayan. Doubly distributional population codes: simultaneous representation of uncertainty and multiplicity. *Neural Computation*, 2279:2255–2279, 2003.

Joshua R Sanes and Richard H Masland. The types of retinal ganglion cells: current status and implications for neuronal classification. *Annual review of neuroscience*, 38:221–246, 2015.

Jayaram Sethuraman. A constructive definition of Dirichlet priors. *Statistica Sinica*, 4: 639–650, 1994.

Ben Shababo, Brooks Paige, Ari Pakman, and Liam Paninski. Bayesian inference and online experimental design for mapping neural microcircuits. In *Advances in Neural Information Processing Systems*, pages 1304–1312, 2013.

- Vahid Shalchyan and Dario Farina. A non-parametric Bayesian approach for clustering and tracking non-stationarities of neural spikes. *Journal of Neuroscience Methods*, 223: 85–91, 2014.
- Lei Shi and Thomas L Griffiths. Neural implementation of hierarchical Bayesian inference by importance sampling. *Advances in Neural Information Processing Systems*, 2009.
- Yousheng Shu, Andrea Hasenstaub, and David A McCormick. Turning on and off recurrent balanced cortical activity. *Nature*, 423(6937):288–293, 2003.
- Jack W Silverstein. The spectral radii and norms of large dimensional non-central random matrices. *Stochastic Models*, 10(3):525–532, 1994.
- Aleksandr Simma and Michael I Jordan. Modeling events with cascades of Poisson processes. *Proceedings of the 26th Conference on Uncertainty in Artificial Intelligence*, 2010.
- Eero P Simoncelli. Optimal estimation in sensory systems. *The Cognitive Neurosciences, IV*, 2009.
- Anne C Smith and Emery N Brown. Estimating a state-space model from point process observations. *Neural Computation*, 15(5):965–91, May 2003.
- Jasper Snoek, Hugo Larochelle, and Ryan P Adams. Practical Bayesian optimization of machine learning algorithms. In *Advances in Neural Information Processing Systems*, pages 2951–2959, 2012.
- Sen Song, Kenneth D Miller, and Lawrence F Abbott. Competitive Hebbian learning through spike-timing-dependent synaptic plasticity. *Nature Neuroscience*, 3(9):919–26, September 2000. ISSN 1097-6256.
- Daniel Soudry, Suraj Keshri, Patrick Stinson, Min-hwan Oh, Garud Iyengar, and Liam Paninski. Efficient “shotgun” inference of neural connectivity from highly sub-sampled activity data. *PLoS Computational Biology*, 11(10):1–30, 10 2015. doi: 10.1371/journal.pcbi.1004464.
- Olaf Sporns, Giulio Tononi, and Rolf Kötter. The human connectome: a structural description of the human brain. *PLoS Comput Biol*, 1(4):e42, 2005.



Olav Stetter, Demian Battaglia, Jordi Soriano, and Theo Geisel. Model-free reconstruction of excitatory neuronal connectivity from calcium imaging signals. *PLoS computational biology*, 8(8):e1002653, 2012.

Ian Stevenson and Konrad Koerding. Inferring spike-timing-dependent plasticity from spike train data. In *Advances in Neural Information Processing Systems*, pages 2582–2590, 2011.

Ian H Stevenson, James M Rebesco, Nicholas G Hatsopoulos, Zach Haga, Lee E Miller, and Konrad P Körding. Bayesian inference of functional connectivity and network structure from spikes. *Neural Systems and Rehabilitation Engineering, IEEE Transactions on*, 17(3):203–213, 2009.

Alan A Stocker and Eero P Simoncelli. Noise characteristics and prior expectations in human visual speed perception. *Nature neuroscience*, 9(4):578–85, April 2006.

Yee Whye Teh and Michael I Jordan. Hierarchical Bayesian nonparametric models with applications. In N. L. Hjort, C. Holmes, P. Müller, and S. G. Walker, editors, *Bayesian Nonparametrics*, pages 158–207. Cambridge University Press, 2010.

Yee Whye Teh, Michael I Jordan, Matthew J Beal, and David M Blei. Hierarchical Dirichlet processes. *Journal of the American Statistical Association*, 101:1566–1581, 2006.

Joshua B Tenenbaum, Thomas L Griffiths, and Charles Kemp. Theory-based Bayesian models of inductive learning and reasoning. *Trends in cognitive sciences*, 10(7):309–318, 2006.

Joshua B Tenenbaum, Charles Kemp, Thomas L Griffiths, and Noah D Goodman. How to grow a mind: Statistics, structure, and abstraction. *science*, 331(6022):1279–1285, 2011.

Luke Tierney and Joseph B Kadane. Accurate approximations for posterior moments and marginal densities. *Journal of the american statistical association*, 81(393):82–86, 1986.

Wilson Truccolo, Uri T. Eden, Matthew R. Fellows, John P. Donoghue, and Emery N. Brown. A point process framework for relating neural spiking activity to spiking history,

neural ensemble, and extrinsic covariate effects. *Journal of Neurophysiology*, 93(2):1074–1089, 2005. doi: 10.1152/jn.00697.2004.

Philip Tully, Matthias Hennig, and Anders Lansner. Synaptic and nonsynaptic plasticity approximating probabilistic inference. *Frontiers in synaptic neuroscience*, 6(8), 2014.

Srini Turaga, Lars Buesing, Adam M Packer, Henry Dagleish, Noah Pettit, Michael Hausser, and Jakob Macke. Inferring neural population dynamics from multiple partial recordings of the same neural circuit. In *Advances in Neural Information Processing Systems*, pages 539–547, 2013.

Leslie G Valiant. *Circuits of the Mind*. Oxford University Press, Inc., 1994.

Leslie G Valiant. Memorization and association on a realistic neural model. *Neural computation*, 17(3):527–555, 2005.

Leslie G Valiant. A quantitative theory of neural computation. *Biological Cybernetics*, 95(3):205–211, 2006.

Jurgen Van Gael, Yunus Saatci, Yee Whye Teh, and Zoubin Ghahramani. Beam sampling for the infinite hidden Markov model. In *Proceedings of the 25th International Conference on Machine Learning*, pages 1088–1095, 2008.

Michael Vidne, Yashar Ahmadian, Jonathon Shlens, Jonathan W Pillow, Jayant Kulkarni, Alan M Litke, EJ Chichilnisky, Eero Simoncelli, and Liam Paninski. Modeling the impact of common noise inputs on the network activity of retinal ganglion cells. *Journal of computational neuroscience*, 33(1):97–121, 2012.

Joshua T Vogelstein, Brendon O Watson, Adam M Packer, Rafael Yuste, Bruno Jedynek, and Liam Paninski. Spike inference from calcium imaging using sequential Monte Carlo methods. *Biophysical journal*, 97(2):636–655, 2009.

Joshua T Vogelstein, Adam M Packer, Timothy A Machado, Tanya Sippy, Baktash Babadi, Rafael Yuste, and Liam Paninski. Fast nonnegative deconvolution for spike train inference from population calcium imaging. *Journal of neurophysiology*, 104(6):3691–3704, 2010.

- Hermann von Helmholtz and James Powell Cocke Southall. *Treatise on Physiological Optics: Translated from the 3rd German Ed.* Optical Society of America, 1925.
- Martin J Wainwright and Michael I Jordan. Graphical models, exponential families, and variational inference. *Foundations and Trends in Machine Learning*, 1(1-2):1–305, 2008.
- Yair Weiss, Eero P Simoncelli, and Edward H Adelson. Motion illusions as optimal percepts. *Nature neuroscience*, 5(6):598–604, 2002.
- Mike West, P Jeff Harrison, and Helio S Migon. Dynamic generalized linear models and Bayesian forecasting. *Journal of the American Statistical Association*, 80(389):73–83, 1985.
- John G White, Eileen Southgate, J Nichol Thomson, and Sydney Brenner. The structure of the nervous system of the nematode *Caenorhabditis elegans*: the mind of a worm. *Philosophical Transactions of the Royal Society of London: Series B (Biological Sciences)*, 314:1–340, 1986.
- Louise Whiteley and Maneesh Sahani. Attention in a Bayesian framework. *Frontiers in human neuroscience*, 6, 2012.
- Alexander B Wiltschko, Matthew J Johnson, Giuliano Iurilli, Ralph E Peterson, Jesse M Katon, Stan L Pashkovski, Victoria E Abaira, Ryan P Adams, and Sandeep Robert Datta. Mapping sub-second structure in mouse behavior. *Neuron*, 88(6):1121–1135, 2015.
- Jesse Windle, Nicholas G Polson, and James G Scott. Sampling Pólya-gamma random variates: alternate and approximate techniques. *arXiv preprint arXiv:1405.0506*, 2014.
- Frank Wood and Michael J Black. A nonparametric Bayesian alternative to spike sorting. *Journal of Neuroscience Methods*, 173(1):1–12, 2008.
- Frank Wood, Jan Willem van de Meent, and Vikash Mansinghka. A new approach to probabilistic programming inference. *arXiv preprint arXiv:1507.00996*, 2015.
- Tianming Yang and Michael N Shadlen. Probabilistic reasoning by neurons. *Nature*, 447(7148):1075–80, June 2007.

- Byron M. Yu, John P. Cunningham, Gopal Santhanam, Stephen I. Ryu, Krishna V. Shenoy, and Maneesh Sahani. Gaussian-process factor analysis for low-dimensional single-trial analysis of neural population activity. *Journal of Neurophysiology*, 102:614–635, 2009.
- Alan Yuille and Daniel Kersten. Vision as Bayesian inference: analysis by synthesis? *Trends in cognitive sciences*, 10(7):301–308, 2006.
- Richard S Zemel, Peter Dayan, and Alexandre Pouget. Probabilistic interpretation of population codes. *Neural computation*, 10(2):403–30, February 1998.
- Ke Zhou, Hongyuan Zha, and Le Song. Learning social infectivity in sparse low-rank networks using multi-dimensional Hawkes processes. In *Proceedings of the International Conference on Artificial Intelligence and Statistics*, volume 16, 2013.
- Mingyuan Zhou, Lingbo Li, Lawrence Carin, and David B Dunson. Lognormal and gamma mixed negative binomial regression. In *Proceedings of the 29th International Conference on Machine Learning*, pages 1343–1350, 2012.