AMAL JYOTHI COLLEGE OF ENGINEERING
KANJIRAPPALLY

MCA-INTEGRATED

MCAINT2022-27-S6 : 20INMCA308-Design & Analysis of Algorithms-Assignment 1

QP Code: 20INMCA308/2020/A/5 **Max.Marks :6**

Q.No	Questions	Marks	CO	BL	PI
1	I. Solve the recurrence relation using Iteration Method a. $T(n)= 2T(n/2) +n$ b. $T(n)= c+(n-1)$ c. $T(n)= T(n/2) +1$ d. $T(n)= 8T(n/2) +n^2$ $(T(1) =1)$ e. $T(n)=T(n-1) +n$ II. Solve the recurrence relation using Recurrence Tree Method a. $T(n)= \begin{cases} 1 & n=1 \\ 1.\ T(n/2) +n & n>1 \end{cases}$ b. $T(n)= \begin{cases} \begin{cases} n=1 \end{cases} & \\ 1.\ 2T(n/2) +n & n>1 \end{cases}$ c. $T(n)=T(n-1) +n$ d. $T(n) = T(n/10) + T(9n/10) + n$ e. $T(n) = T(n/5) + T(4n/5) + n$ III. Apply the Master's Theorem to determine the time complexity of the recurrence a. $T(n)= 3T(n/2) +n^2$ b. $T(n)= 4T(n/2) +n^2$ c. $T(n)= 9T(n/3) +n$ d. $T(n)= 2T(n/2) +cn$ e. $T(n)= 16T(n/4) + n$	3	CO1	L6	1.1.1,1.1.2,1.3.1, 2.1.3,2.2.1,2.2.5, 2.3.1
2	I. Given a sorted array **arr[] = {2, 5, 8, 12, 16, 23, 38, 56, 72, 91}** and a target value **23**, implement a Binary Search algorithm to determine whether the target exists in the array. II. Given a sorted array **a[] = {2, 3, 7, 7, 11, 15, 25},** implement a Binary Search algorithm to find the target element **11**. III. Given an unsorted array **a[] = {38, 27, 43, 3, 9, 82, 10},** implement the Merge Sort algorithm to sort the array in ascending order. Perform a step-by-step dry run, explaining	3	CO2	L6	1.1.1,1.1.2, 1.3.1,1.4.1,2.1.1, 2.1.2,2.2.1,2.2.3, 2.2.5

<table>
<tr><th>Q.No</th><th>Questions</th><th>Marks</th><th>CO</th><th>BL</th><th>PI</th></tr>
<tr><td></td><td>and visualizing how the array is recursively divided and merged at each stage of the Merge Sort algorithm.
IV. Formulate the Merge Sort algorithm for the given array a[] = {12, 11, 13, 5, 6, 7} and sort it in ascending order. Count and display the number of comparisons made during the sorting process.
V. Given an unsorted array a[] = {29, 10, 14, 37, 13, 20}, implement the Quick Sort algorithm to sort the array in ascending order, and demonstrate a step-by-step dry run of the algorithm, showing the partitioning process at each step.
VI. Given the unsorted array a[] = {44, 33, 55, 22, 88, 77, 11, 99}, implement the Quick Sort algorithm. Demonstrate the sorting process, showing the choice of pivot and partitioning at each recursion step.
VII. Analyse and implement a divide and conquer algorithm to find the maximum and minimum values in the array [3, 1, 4, 1, 5, 9, 2].
VIII. Design a recursive divide and conquer approach to find the minimum and maximum elements in a given array of integers [12, 7, 5, 10, 8]
IX. A thief enters a store with a knapsack that can carry a maximum weight of 50 kg. There are three items available, each with a specific weight and value. The thief can take fractional parts of an item. Find the maximum value the thief can carry using the Greedy Algorithm.
<table>
<tr><th>X.</th><th>Item</th><th>XI.</th><th>Weight</th><th>XII.</th><th>Value</th></tr>
<tr><td>XIII.</td><td>1</td><td>XIV.</td><td>10</td><td>XV.</td><td>60</td></tr>
<tr><td>XVI.</td><td>2</td><td>XVII.</td><td>20</td><td>VIII.</td><td>100</td></tr>
<tr><td>XIX.</td><td>3</td><td>XX.</td><td>30</td><td>XXI.</td><td>120</td></tr>
</table>
XII. A hiker has a backpack with a capacity of 60 kg and wants to carry the most valuable items. There are four items, each with a given weight and value. The hiker can take fractional parts of any item. Find the maximum value that can be carried using the Greedy Algorithm.
<table>
<tr><th>Item</th><th>Weight</th><th>Value</th></tr>
<tr><td>1</td><td>20</td><td>100</td></tr>
<tr><td>2</td><td>10</td><td>60</td></tr>
<tr><td>3</td><td>30</td><td>120</td></tr>
<tr><td>4</td><td>40</td><td>240</td></tr>
</table></td><td></td><td></td><td></td><td></td></tr>
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CO1: Implement design principles and analyze the asymptotic performance of algorithms.

CO2: Derive and solve recurrences describing the performance of divide-and-conquer algorithms and greedy algorithms

CO(s) contribution for PO/PSO Attainment from Assignment 1

Question	COs Mark & Mapped PO(s)/PSO(s)[Strength] *3.Substantial, 2.Moderate, 1.Slight*	Total Marks per CO	40% per CO(s)	CO contribution to calculate PO/PSO attainment(%)
1 a)	CO1[**3**]=>**PO1** (3), **PO2** (2), **PO3** (3), **PO4** (2), **PO5** (1), **PO7** (1), **PO8** (1),**PSO1** (2), **PSO2** (3)	CO1=>3 CO2=>3	CO1=>1.2 CO2=>1.2	
2 a)	CO2[**3**]=>**PO1** (2), **PO2** (3), **PO3** (3), **PO4** (2), **PO5** (1), **PO8** (1),**PSO1** (3), **PSO2** (2), **PSO3** (1)			

Rubrics used for the assessment- MCAINT2022-27-S6 : 20INMCA308-Design & Analysis of Algorithms-Assignment 1

Bloom's Level wise Marks Distribution

Blooms Taxonomy Level		Percentage
L6	Creating	100

Course Outcome wise Marks Distribution

COs	Percentage
CO1	50
CO2	50