



# Elliptic Curve Cryptography | ECC in Cryptography and Network Security

Generated on December 19, 2023

## Summary

Notes

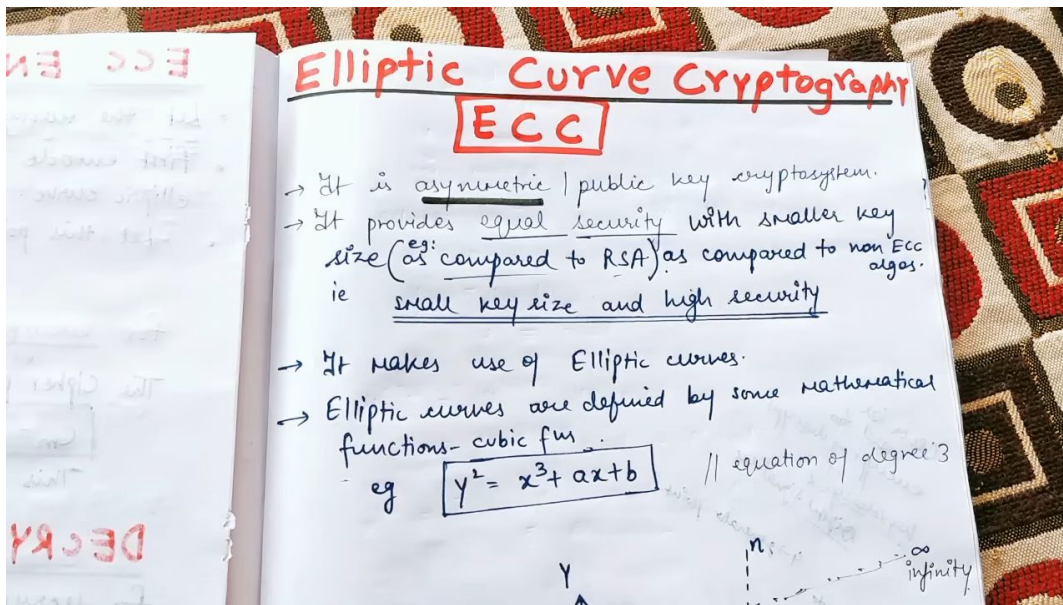
Screenshots

Bookmarks

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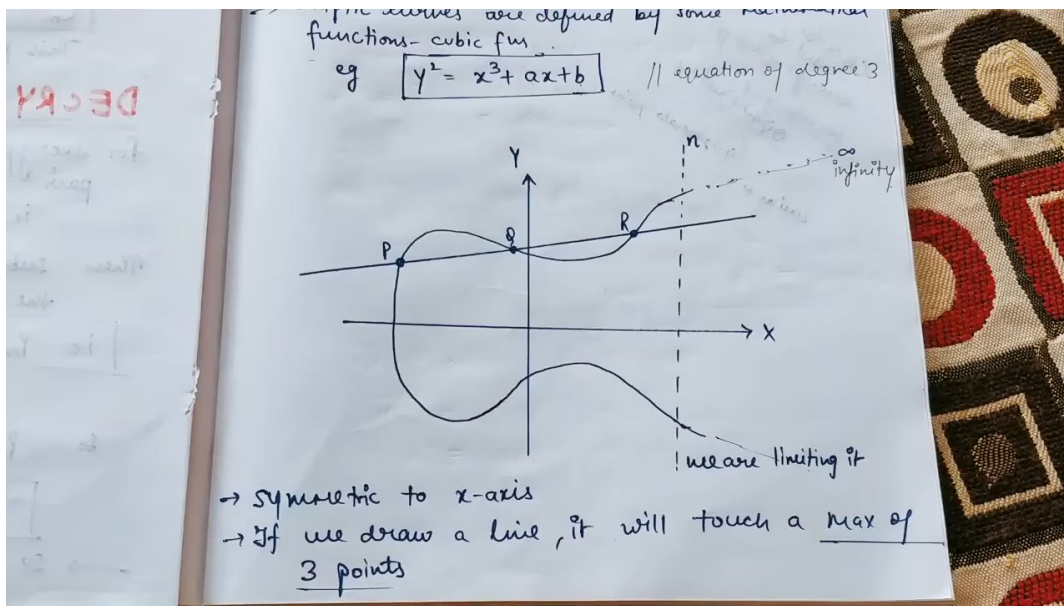
16

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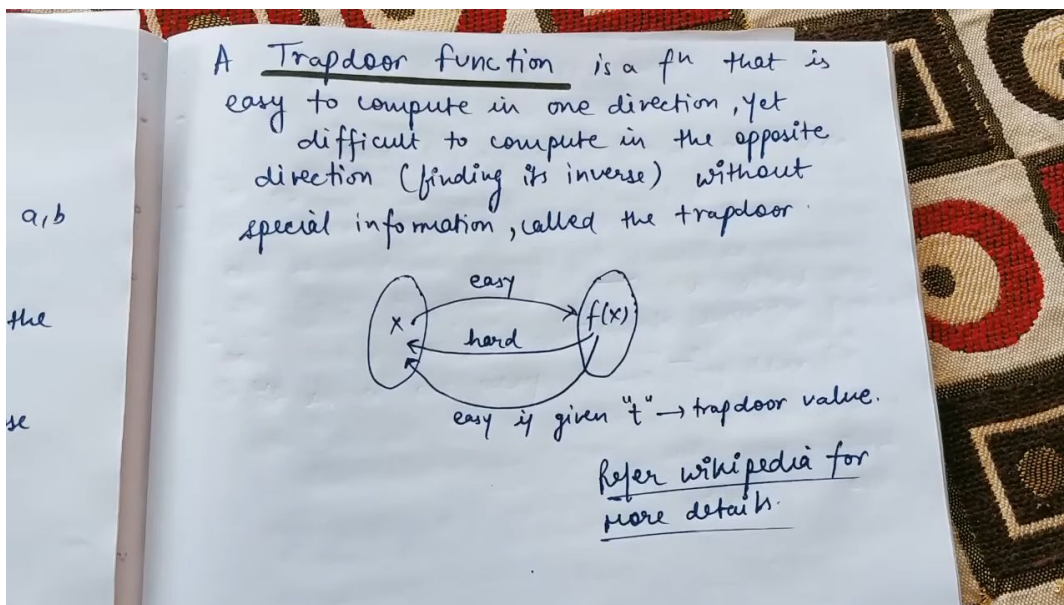
✦ The study of the 10 most powerful empires and reserve currencies over the last 500 years reveals fascinating patterns of rise and decline.

▶ 0:08



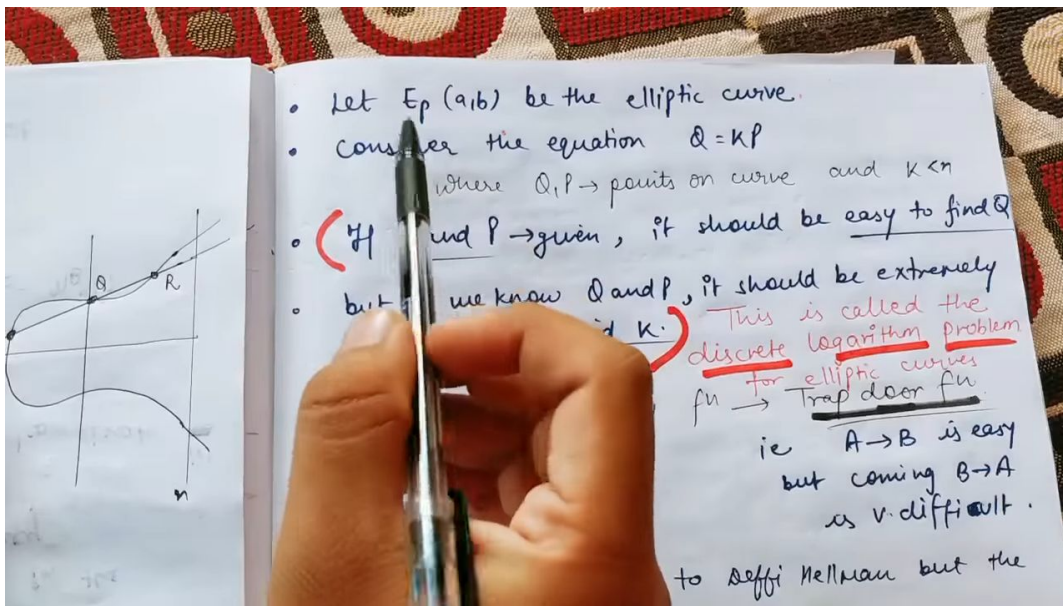
✦ A new study has developed a comprehensive method for measuring the power of different empires, using eight key metrics to determine their total strength.

▶ 1:43



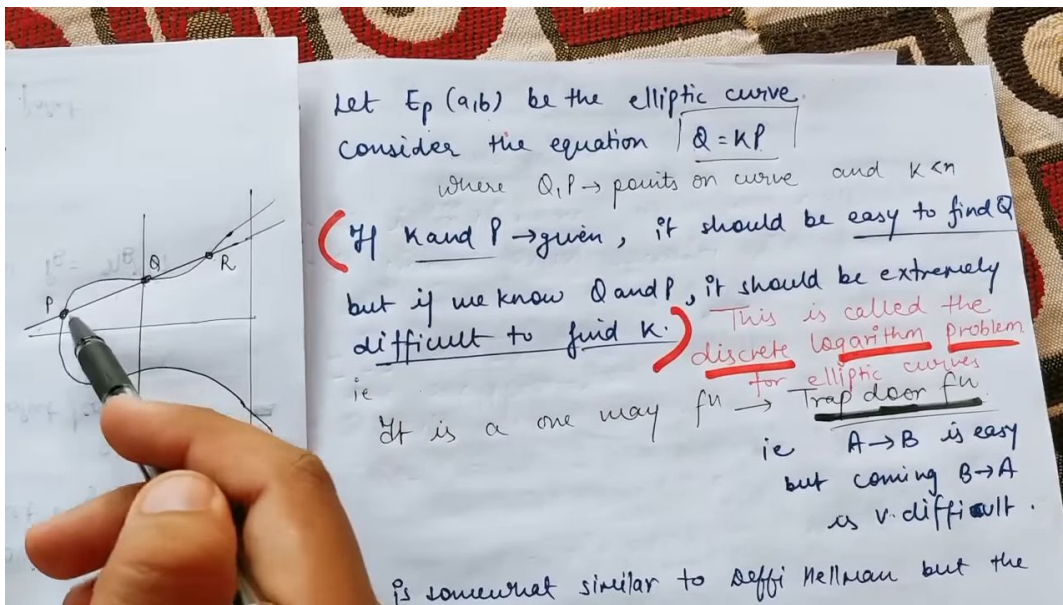
✦ The link between education, innovation, technology development, and currency reserve status is crucial for understanding a country's economic rise and decline.

▶ 2:49



✦ The uneven distribution of wealth in times of increased prosperity can lead to financial bubbles, internal conflict, and potential revolutions for wealth redistribution.

▶ 4:00



✦ Internal conflict and power struggles within the Empire may lead to a redistribution of wealth and potential civil unrest.

▶ 4:18



# ECC - ALGORITHM

## ECC - Key Exchange

### Global Public Elements

$E_2(a,b)$  : elliptic curve with parameters  $a, b$   
and  $q$   
↓  
prime no. or an integer of the  
form  $2^m$ .

$G_1$  : Point on the curve/elliptic curve whose  
order is large value of  $n$ .

### User A key generation

Select private key  $n_A$   $n_A < n$   
calculate public key  $P_A$   $P_A = n_A \times G_1$

▷ 5:48

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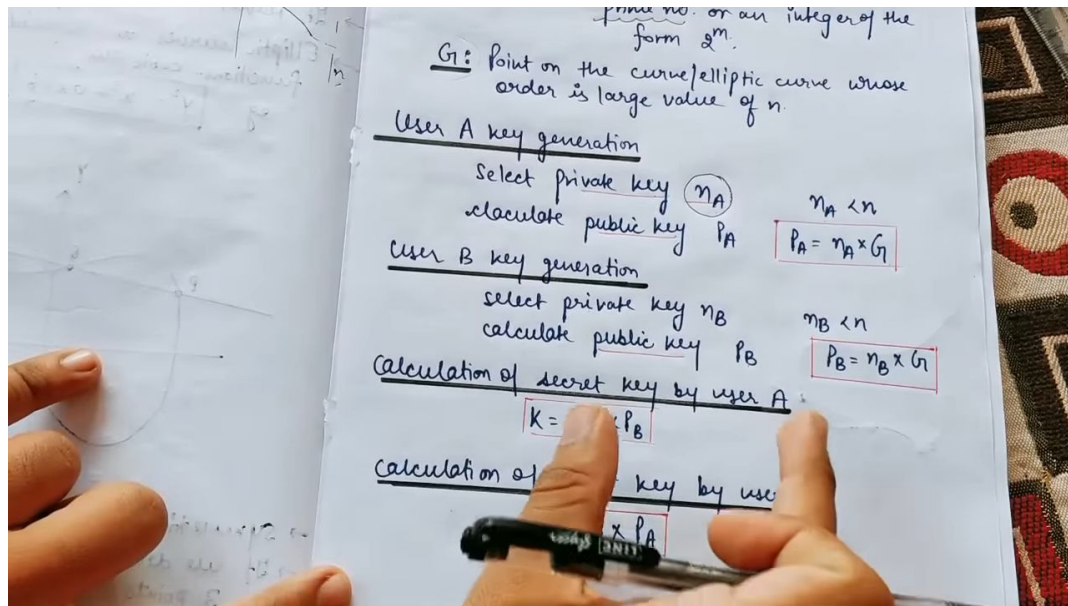
### User B key generation

Select private key  $n_B$   $n_B < n$   
calculate public key  $P_B$   $P_B = n_B \times G_1$

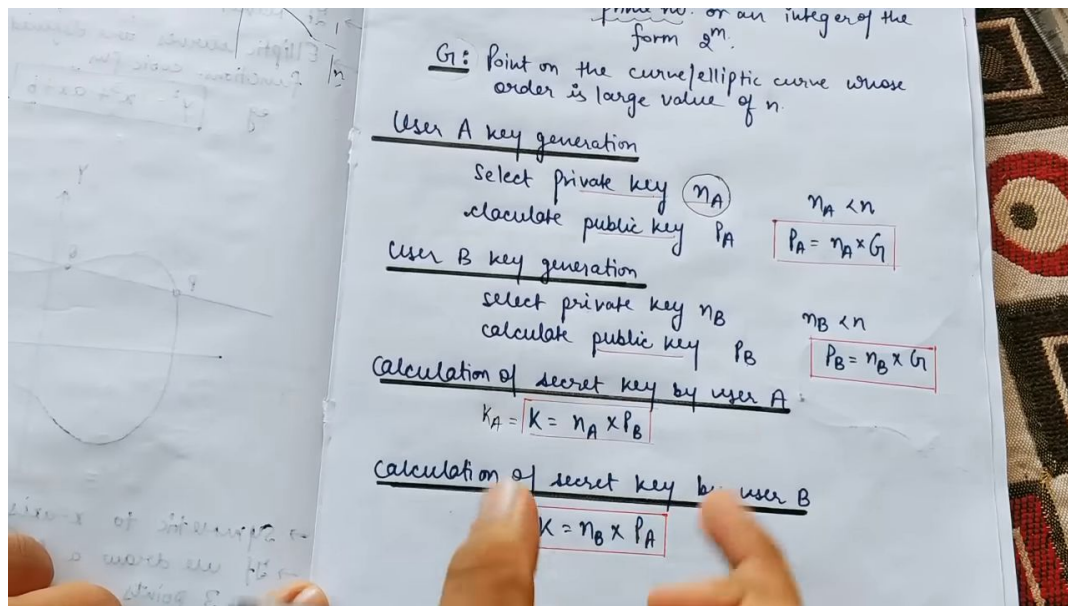
### Calculation of secret key

$K$

▷ 7:19



▶ 8:42



▶ 8:54

prime no. or an integer of the form  $2^n$ .

G: Point on the curve/elliptic curve whose order is large value of  $n$ .

User A key generation

Select private key  $n_A$   $n_A < n$   
 calculate public key  $P_A$   $P_A = n_A \times G$

User B key generation

Select private key  $n_B$   $n_B < n$   
 calculate public key  $P_B$   $P_B = n_B \times G$

Calculation of secret key by user A

$K_A = K = n_A \times P_B$

Calculation of secret key by user B

$K = n_B \times P_A$

▶ 9:36

**ECC ENCRYPTION**

- Let the message be  $M$ .
- First encode this message  $M$  into a point on elliptic curve.
- Let this point be  $P_m$ .

Now this point is encrypted.

for encryption, chose a random positive integer  $k$ .

The cipher point will be  $C_m = \{ kG, P_m + kP_B \}$  for encryption public key of B used

This point will be sent to the receiver

**DECRYPTION**

for decryption, multiply 1st point in the secret key

▶ 10:12



## ECC ENCRYPTION

- Let the message be  $M$ .
- First encode this message  $M$  into a point on elliptic curve.
- Let this point be  $P_m$ .

Now this point is encrypted.

for encryption, choose a random positive integer  $k$

The cipher point will be

$$C_m = \{ kG, P_m + kP_B \}$$

→ for encryption  
public key of B  
used

This point will be sent to the receiver

## DECRYPTION

for decryption, multiply 1st point in the pair with receiver's secret key

▶ 11:27

## ECC ENCRYPTION

- Let the message be  $M$ .
- First encode this message  $M$  into a point on elliptic curve.
- Let this point be  $P_m$ .

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for encryption, choose a random positive integer  $k$

Cipher point will be

$$C_m = \{ kG, P_m + kP_B \}$$

→ for encryption  
public key of B  
used

This point will be sent to the receiver

## DECRYPTION

for decryption, multiply 1st point in the pair with receiver's secret key

▶ 11:30

The cipher point will be

$$C_m = \{ kG, P_m + kP_B \}$$

*for encryption public key of B used*

This point will be sent to the receiver

## DECRYPTION

for decryption, multiply 1st point in the pair with receiver's secret key

$$\text{i.e. } kG * n_B \quad // \text{for decryption private key of B used}$$

Then subtract it from 2nd point / coordinate in the pair

$$\text{i.e. } P_m + kP_B - (kG * n_B)$$

$$\text{So } = P_m + kP_B$$

$$= P_m$$

→ So receiver

▷ 12:06

The cipher point will be

$$C_m = \{ kG, P_m + kP_B \}$$

*for encryption public key of B used*

This point will be sent to the receiver

## DECRYPTION

for decryption, multiply 1st point in the pair with receiver's secret key

$$\text{i.e. } kG * n_B \quad // \text{for decryption private key of B used}$$

Then subtract it from 2nd point / coordinate in the pair

$$\text{i.e. } P_m + kP_B - (kG * n_B)$$

$$\text{but we know } P_B = n_B * G$$

$$\text{So } = P_m + kP_B - kP_B$$

$$= P_m \quad (\text{original point}).$$

→ So receiver gets the same point

▷ 13:00



diff bw

Key Sizes in Terms of Computational Effort for Cryptanalysis

ECC-Based Scheme (size of $n$ in bits)	RSA/DSA (modulus size in bits)
112	512
160	1024
224	2048
256	3072
384	7680
512	15360

by showing comparable key sizes in terms of computational