

# Prospect Theory and Robust Life-Cycle Investing

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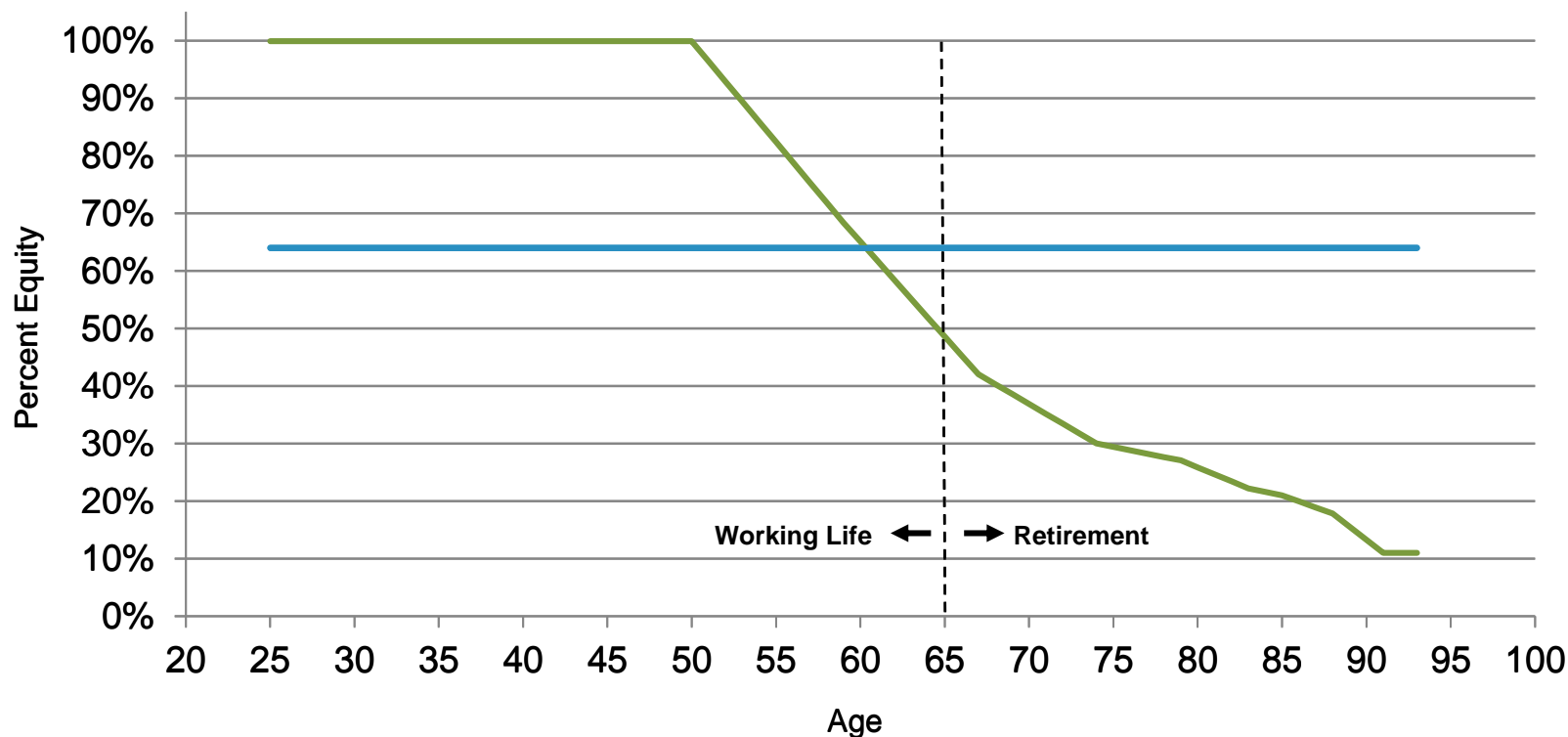
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# Need to Save for Retirement: How to Invest?

## PORTFOLIO ALLOCATION OVER THE LIFE-CYCLE

— Merton-Samuelson, CRRA = 2      — Prospect Theory, Loss Aversion = 2.25

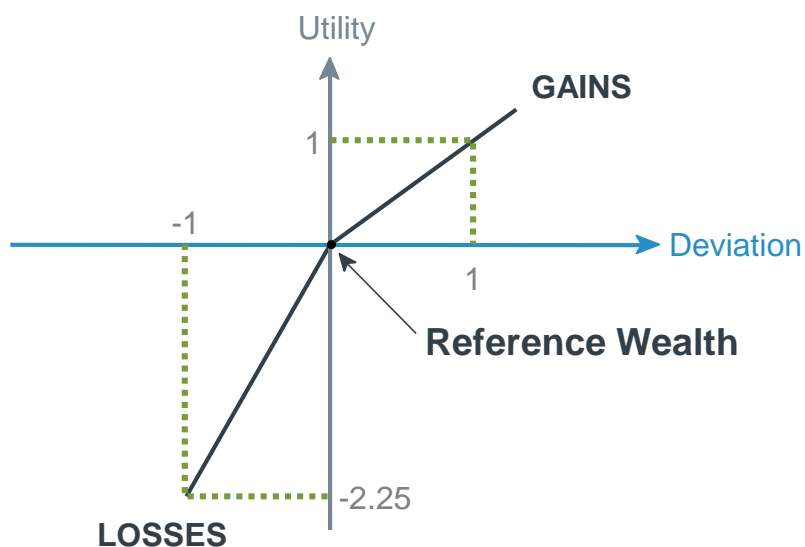


**For this presentation: Capital Markets is the only source of uncertainty**

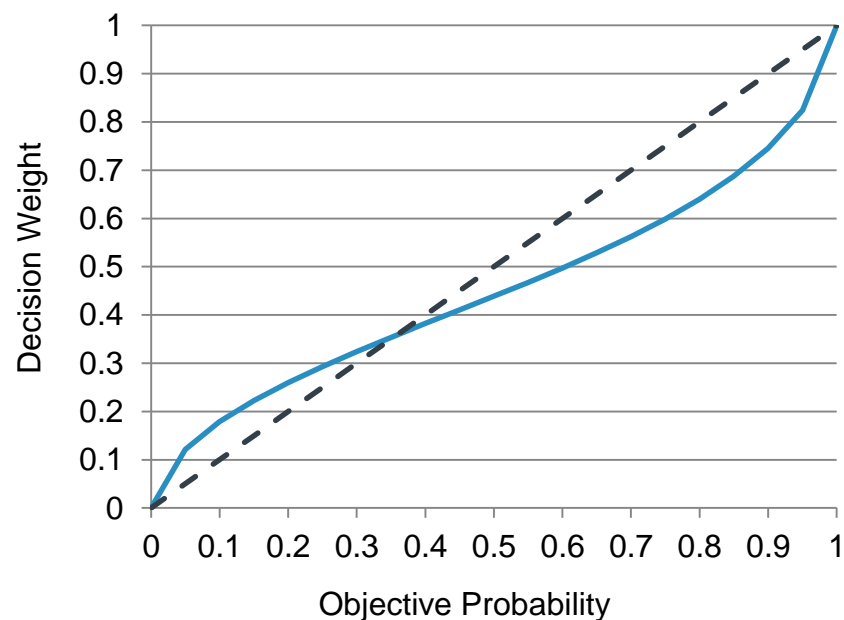
**Past performance is no guarantee of future results.** Sources: U.S. Equity: S&P 500 Global Financial Database (GFD) prior to 1926.07, Fama-French All Market since 1926.07. Non-U.S. Equity: 60% UK, 40% FRA equity prior to 1926 (per GFD relative weights, GFD WxUS (EAFE) 1926-1987, MSCI ACWIxUS since 1988. U.S. Bonds: UST10 (GFD) prior to 1975.12, Barclays US Agg since 1975.12.

# Prospect Theory: An Analysis of Decision Under Risk

## VALUE FUNCTION



## PROBABILITY WEIGHTING FUNCTION

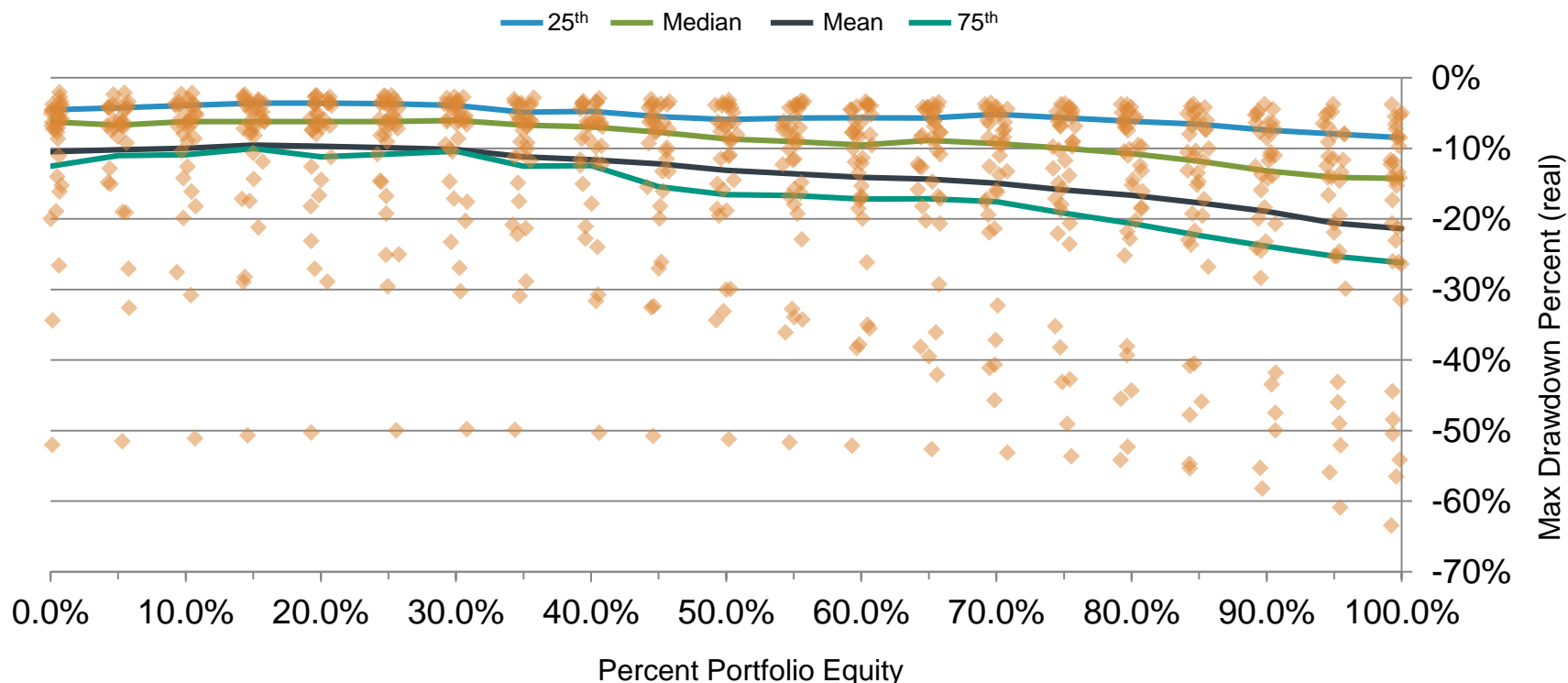


Source: Daniel Kahneman and Amos Tversky (1979, 1992).

# Loss Aversion + Concern for Tail Events = Robust Control

## HISTORICAL TOTAL PORTFOLIO DRAWDOWNS SINCE 1900

U.S. Aggregate Bond with 50/50 Mix of U.S./Non-U.S. Equity



**The set of historical worst case scenarios varies by portfolio**

An 80% bond portfolio can do well under high equity drawdowns

**Past performance is no guarantee of future results.** Sources: U.S. Equity: S&P 500 Global Financial Database (GFD) prior to 1926.07, Fama-French All Market since 1926.07. Non-U.S. Equity: 60% UK, 40% FRA equity prior to 1926 (per GFD relative weights, GFD WxUS (EAFE) 1926-1987, MSCI ACWIxUS since 1988. U.S. Bonds: UST10 (GFD) prior to 1975.12, Barclays US Agg since 1975.12.

# Composition of Cyclical Drawdowns For An All-Equity Portfolio

## STATISTICALLY REASONABLE SET OF WORSE-CASE SCENARIOS

### Market Risk:

Exposure to the largest market drawdowns (peak to trough)

### Recovery Risk:

Exposure to the slowest recoveries (time to par)

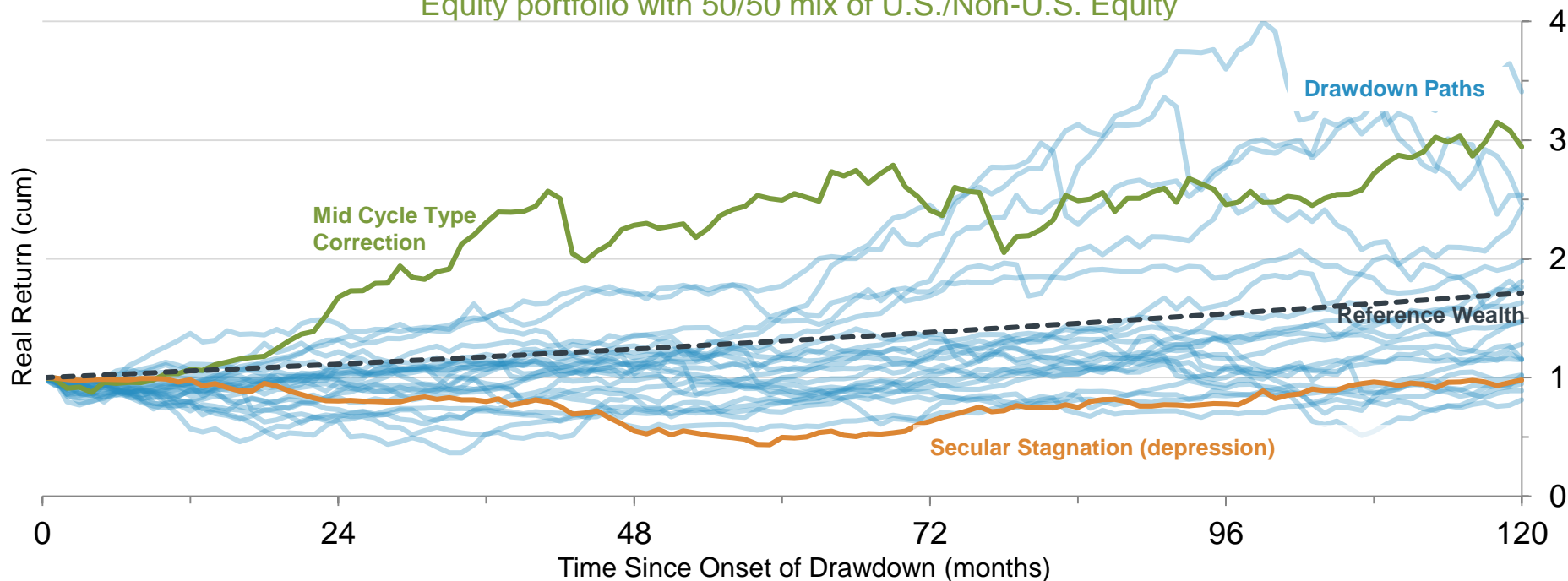
### Sequence Risk:

Evaluate each strategy at the event onset

## TOP 25 EQUITY DRAWDOWNS SINCE 1900

### Drawdown Plus Trailing 10-year Return

Equity portfolio with 50/50 mix of U.S./Non-U.S. Equity



Sources: U.S. Equity: S&P 500 Global Financial Database (GFD) prior to 1926.07, Fama-French All Market since 1926.07. Non-U.S. Equity: 60% UK, 40% FRA equity prior to 1926 (per GFD relative weights, GFD WxUS (EAFE) 1926-1987, MSCI ACWIxUS since 1988. U.S. Bonds: UST10 (GFD) prior to 1975.12, Barclays US Agg since 1975.12.

# Solution Method: Robust Dynamic Programming

Step 1:

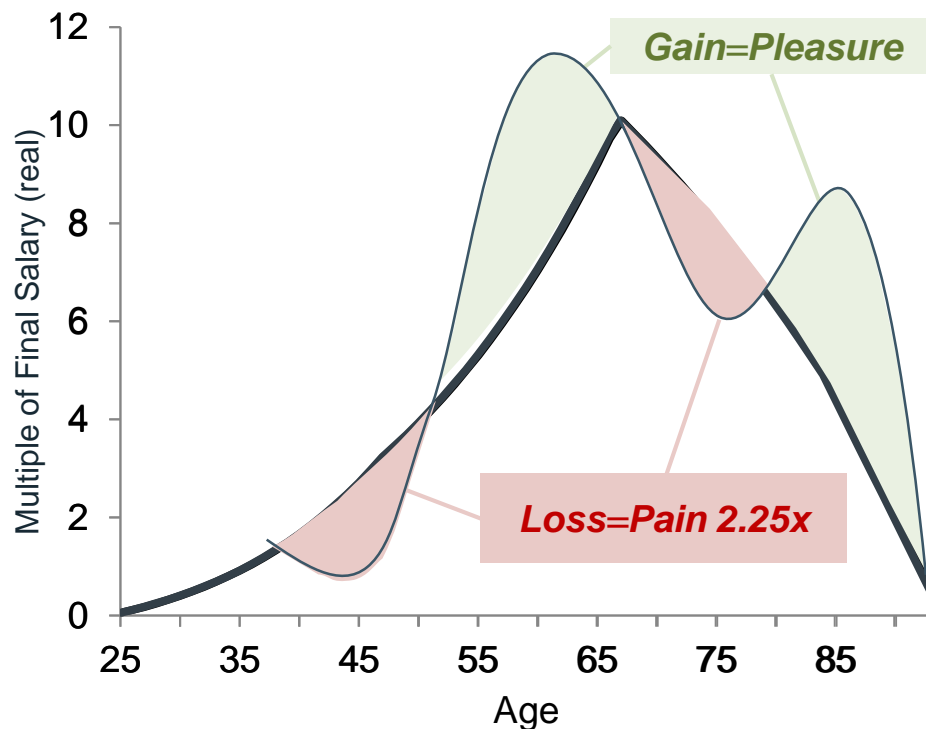
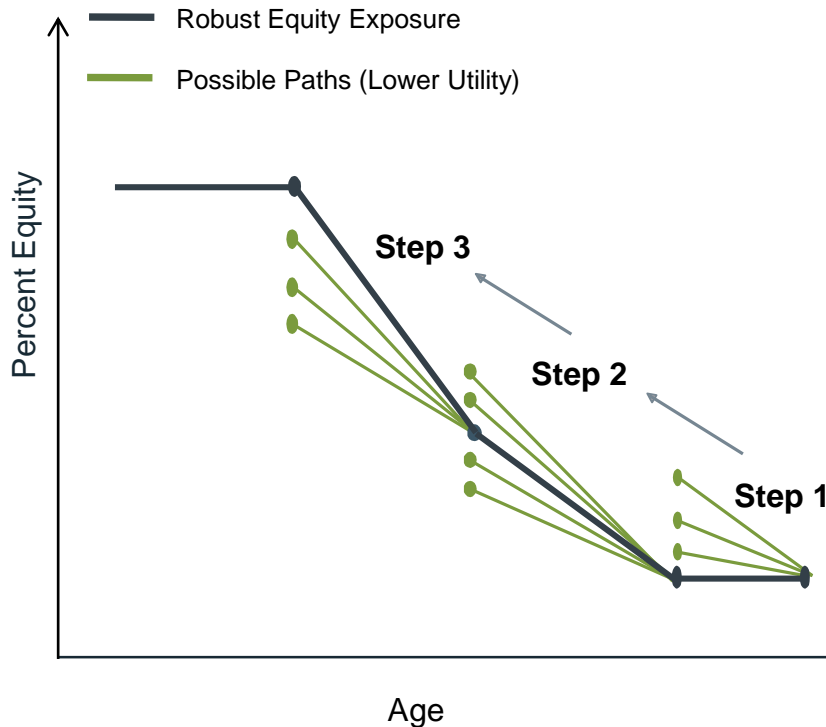
A strategy that funds retirement

Step 2:

Evil agent hits us with portfolio drawdowns

Step 3:

Calculate Welfare

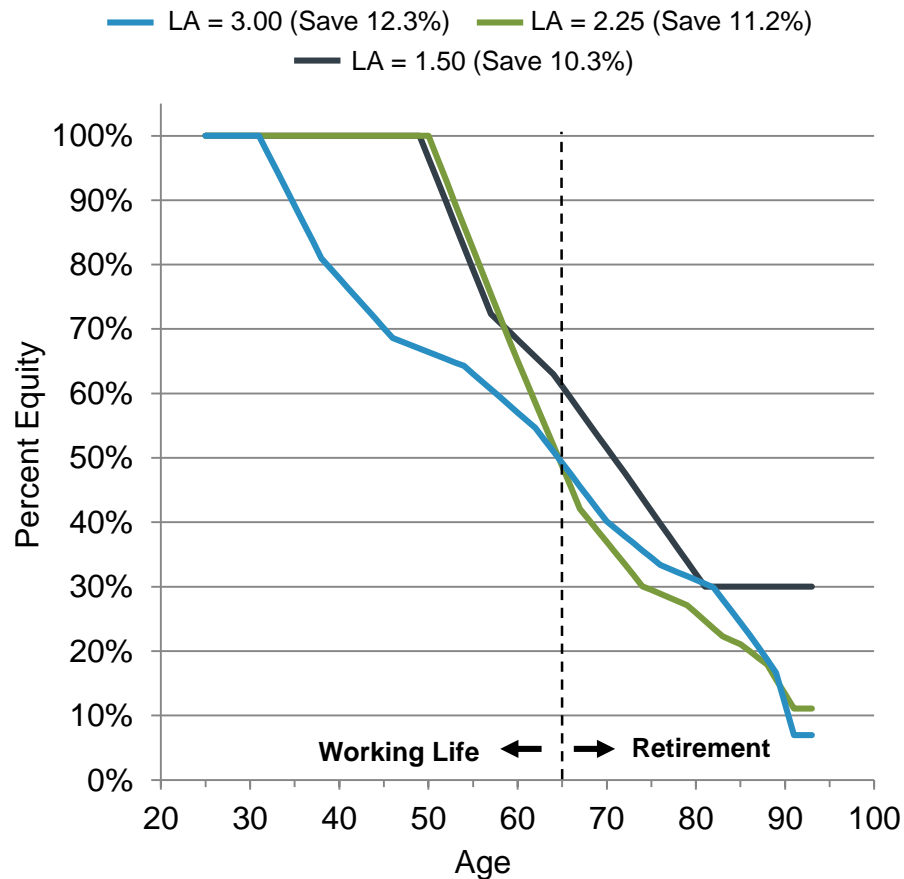


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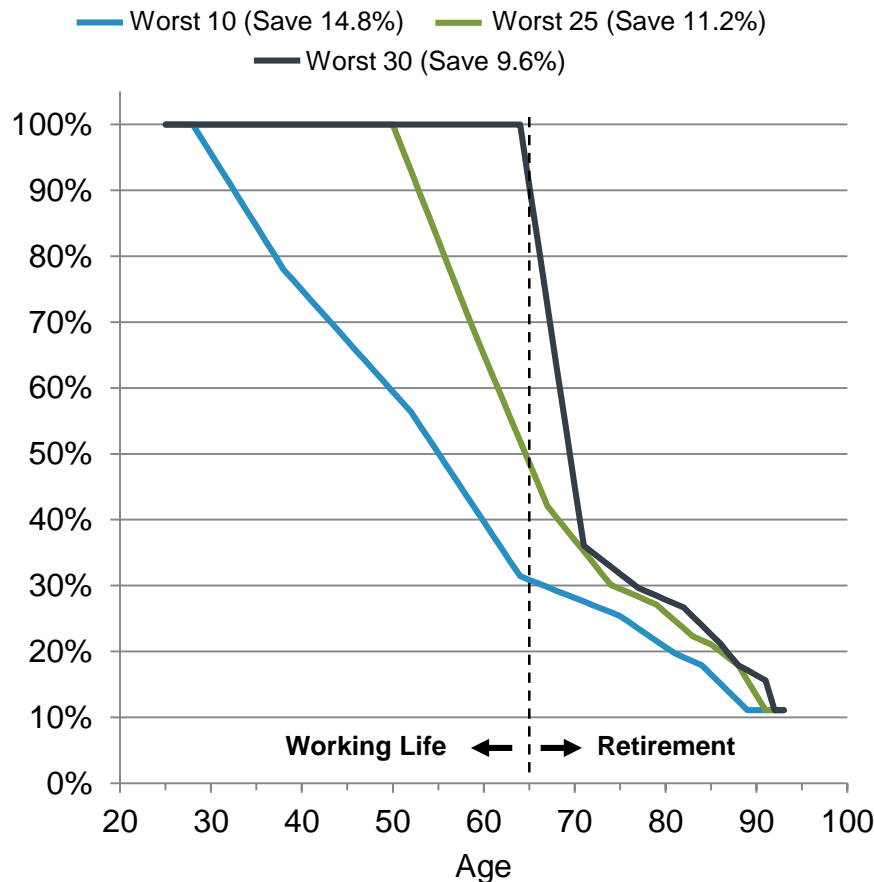
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# Impact of Preference Heterogeneity

## ASSESSING THE IMPACT OF HETEROGENEITY IN LOSS AVERSION



## ASSESSING THE IMPACT OF PESSIMISM (OVERWEIGHTING THE LEFT TAIL)



Sources: U.S. Equity: S&P 500 Global Financial Database (GFD) prior to 1926.07, Fama-French All Market since 1926.07. Non-U.S. Equity: 60% UK, 40% FRA equity prior to 1926 (per GFD relative weights, GFD WxUS (EAFE) 1926-1987, MSCI ACWIxUS since 1988. U.S. Bonds: UST10 (GFD) prior to 1975.12, Barclays US Agg since 1975.12.

# What We Are Currently Investigating

- Accounting for pervasive heterogeneity
  - Preference parameters
  - Labor income processes and their covariance with asset returns<sup>1</sup>
  - Contribution rates
- Modular vs. fully integrated investment design?
  - Mental accounting
  - Efficiency-robustness trade-off
- What is the appropriate level of customization?

<sup>1</sup> Guvenen et al. (2014). "The nature of countercyclical income risk," JPE.



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