


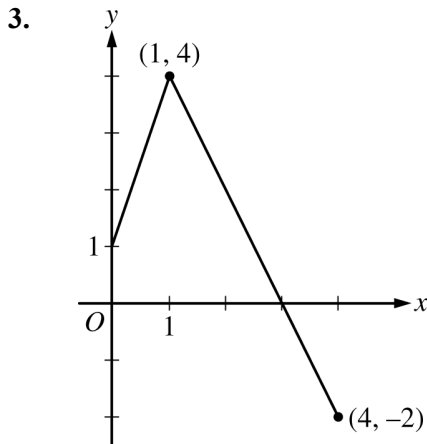
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1.  If  $f(x) = \ln(e^{2x})$ , then  $f'(x) =$

(A) 1  
(B) 2  
(C)  $2x$   
(D)  $e^{-2x}$   
(E)  $2e^{-2x}$

2. An equation of the line tangent to the graph of  $f(x) = x(1 - 2x)^3$  at the point  $(1, -1)$  is

(A)  $y = -7x + 6$   
(B)  $y = -6x + 5$   
(C)  $y = -2x$   
(D)  $y = 2x - 3$   
(E)  $y = 7x - 8$



Graph of  $f$

The graph of the function  $f$ , consisting of two line segments, is shown in the figure above. Let  $g$  be the function given by  $g(x) = 2x + 1$ , and let  $h$  be the function given by  $h(x) = f(g(x))$ . What is the value of  $h'(1)$ ?

(A) -4  
(B) -2  
(C) 4  
(D) 6  
(E) nonexistent

4. If  $y = \left(\frac{x}{x+1}\right)^5$ , then  $\frac{dy}{dx} =$

6

(A)  $5(1+x)^4$

(B)  $\frac{x^4}{(x+1)^4}$

(C)  $\frac{5x^4}{(x+1)^4}$

(D)  $\frac{5x^4}{(x+1)^6}$

(E)  $\frac{5x^4(2x+1)}{(x+1)^6}$

5. If  $f(x) = (x^2 - 3)^4$ , then  $f'(1) =$

(A)  $-64$

(B)  $-32$

(C)  $-16$

(D)  $32$

6. If  $y = (x^3 + 1)^2$ , then  $\frac{dy}{dx} =$

(A)  $(3x^2)^2$

(B)  $2(x^3 + 1)$

(C)  $2(3x^2 + 1)$

(D)  $3x^2(x^3 + 1)$

(E)  $6x^2(x^3 + 1)$

7. If  $f$  and  $g$  are twice differentiable functions such that  $g(x) = e^{f(x)}$  and  $g''(x) = h(x)e^{f(x)}$ , then  $h(x) =$


(A)  $f'(x) + f''(x)$

(B)  $f'(x) + (f''(x))^2$

(C)  $(f'(x) + f''(x))^2$

(D)  $(f'(x))^2 + f''(x)$

(E)  $2f'(x) + f''(x)$

8.  If  $y = \arctan(e^{2x})$ , then  $\frac{dy}{dx} =$

(A)  $\frac{2e^{2x}}{\sqrt{1-e^{4x}}}$


(B)  $\frac{2e^{2x}}{1+e^{4x}}$

(C)  $\frac{e^{2x}}{1+e^{4x}}$

(D)  $\frac{1}{\sqrt{1-e^{4x}}}$

(E)  $\frac{1}{1+e^{4x}}$

6

9.  If  $f(x) = e^{\tan^2 x}$ , then  $f'(x) =$
- (A)  $e^{\tan^2 x}$   
(B)  $\sec^2 x e^{\tan^2 x}$   
(C)  $\tan^2 x e^{\tan^2 x - 1}$   
(D)  $2 \tan x \sec^2 x e^{\tan^2 x}$   
(E)  $2 \tan x e^{\tan^2 x}$
10. If  $y = \cos^2 3x$ , then  $dy/dx =$
- (A)  $-6 \sin 3x \cos 3x$   
(B)  $-2 \cos 3x$   
(C)  $2 \cos 3x$   
(D)  $6 \cos 3x$   
(E)  $2 \sin 3x \cos 3x$
11. If  $f(x) = x^2 + 2x$ , then  $\frac{d}{dx}(f(\ln x)) =$
- (A)  $\frac{2 \ln x + 2}{x}$   
(B)  $2x \ln x + 2x$   
(C)  $2 \ln x + 2$   
(D)  $2 \ln x + \frac{2}{x}$   
(E)  $\frac{2x + 2}{x}$
12. If  $f(x) = e^{(2/x)}$ , then  $f'(x) =$
- (A)  $2e^{(2/x)} \ln x$   
(B)  $e^{(2/x)}$   
(C)  $e^{(-2/x^2)}$   
(D)  $-\frac{2}{x^2} e^{(2/x)}$   
(E)  $-2x^2 e^{(2/x)}$
13. If  $f(x) = e^{1/x}$ , then  $f'(x) =$
- (A)  $-\frac{e^{1/x}}{x^2}$   
(B)  $-e^{1/x}$   
(C)  $\frac{e^{1/x}}{x}$   
(D)  $\frac{e^{1/x}}{x^2}$   
(E)  $\frac{1}{x} e^{(1/x) - 1}$

6

14. If  $y = (x/x+1)^5$ , then  $dy/dx$ 

- (A)  $5(1+x)^4$   
(B)  $\frac{x^4}{(x+1)^4}$   
(C)  $\frac{5x^4}{(x+1)^4}$   
(D)  $\frac{5x^4}{(x+1)^6}$   
(E)  $\frac{5x^4(2x+1)}{(x+1)^6}$

15. If  $y = \sin^3 x$ , then  $\frac{dy}{dx} =$ 

- (A)  $\cos^3 x$   
(B)  $3 \cos^2 x$   
(C)  $3 \sin^2 x$   
(D)  $-3 \sin^2 x \cos x$   
(E)  $3 \sin^2 x \cos x$

16.

$x$	3	7
$h(x)$	7	22
$h'(x)$	5	10

Selected values of the increasing function  $h$  and its derivative  $h'$  are shown in the table above. If  $g$  is a differentiable function such that  $h(g(x)) = x$  for all  $x$ , what is the value of  $g'(7)$ ?

- (A)  $-1/10$   
(B)  $1/10$   
(C)  $1/5$   
(D)  $7/5$

17. If  $f(x) = \cos(3x)$ , then  $f'(\frac{\pi}{9}) =$ 

- (A)  $\frac{3\sqrt{3}}{2}$   
(B)  $\frac{\sqrt{3}}{2}$   
(C)  $-\frac{\sqrt{3}}{2}$   
(D)  $-\frac{3}{2}$   
(E)  $-\frac{3\sqrt{3}}{2}$

6

18. If  $f(x) = \cos^3(4x)$ , then  $f'(x) =$

- (A)  $3\cos^2(4x)$
- (B)  $-12\cos^2(4x) \sin(4x)$
- (C)  $-3\cos^2(4x) \sin(4x)$
- (D)  $12\cos^2(4x) \sin(4x)$
- (E)  $-4\sin^3(4x)$

19. Let  $f$  and  $g$  be differentiable functions such that

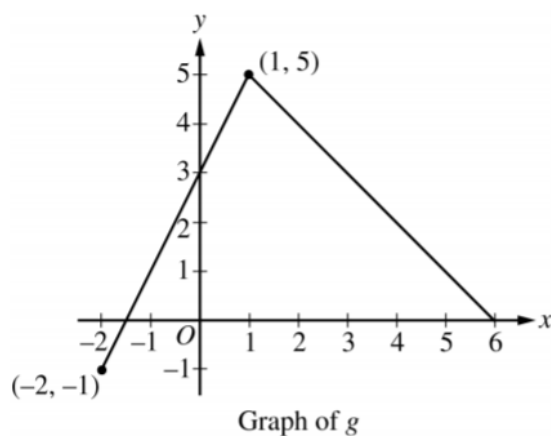
$$f(1) = 2, \quad f'(1) = 3, \quad f'(2) = -4,$$

$$g(1) = 2, \quad g'(1) = -3, \quad g'(2) = 5.$$

If  $h(x) = f(g(x))$ , then  $h'(1) =$

- (A) -9
- (B) -4
- (C) 0
- (D) 12
- (E) 15

20.



The graph of the function  $g$  is shown above. If  $f$  is the function given by  $f(x) = g(g(x))$ , what is the value of  $f'(0)$ ?

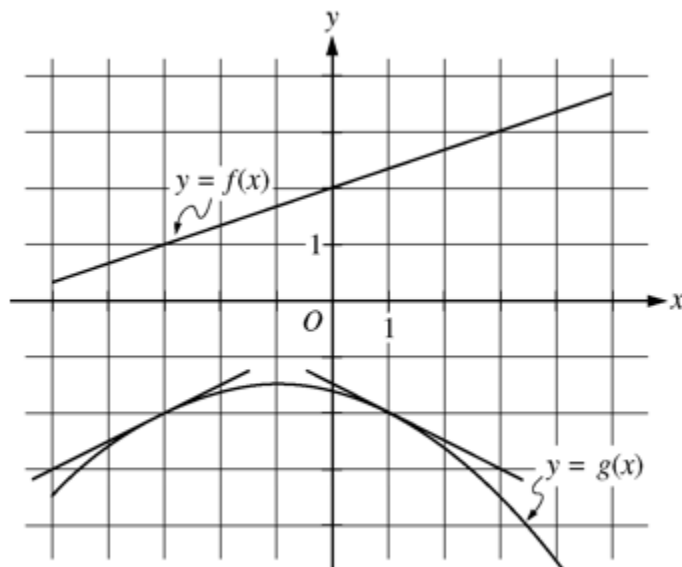
- (A) -2
- (B) -1
- (C) 2
- (D) 3

21. If  $y = (x^3 - \cos x)^5$  then  $y' =$

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- (A)  $5(x^3 - \cos x)^4$   
 (B)  $5(3x^2 + \sin x)^4$   
 (C)  $5(3x^2 + \sin x)$   
 (D)  $5(3x^2 + \sin x)^4 \cdot (6x + \cos x)$   
 (E)  $5(x^3 - \cos x)^4 \cdot (3x^2 + \sin x)$

22.



The figure above shows the graphs of the functions  $f$  and  $g$ . The graphs of the lines tangent to the graph of  $g$  at  $x = -3$  and  $x = 1$  are also shown. If  $B(x) = g(f(x))$ , what is  $B'(-3)$ ?

- (A)  $-\frac{1}{2}$   
 (B)  $-\frac{1}{6}$   
 (C)  $\frac{1}{6}$   
 (D)  $\frac{1}{3}$   
 (E)  $\frac{1}{2}$

6

23.

$x$	$f(x)$	$g(x)$	$f'(x)$	$g'(x)$
-1	-5	1	3	0
0	-2	0	1	1
1	0	-3	0	0.5
2	5	-1	5	2

The table above gives values of the differentiable functions  $f$  and  $g$  and of their derivatives  $f'$  and  $g'$ , at selected values of  $x$ . If  $h(x) = f(g(x))$ , what is the slope of the graph of  $h$  at  $x = 2$ ?

- (A) -10
- (B) -6
- (C) 5
- (D) 6
- (E) 10

24.

For  $x > 0$ ,  $\frac{d}{dx} \left( \int_0^{2x} \ln(t^3 + 1) dt \right) =$


- (A)  $\ln(x^3 + 1)$
- (B)  $\ln(8x^3 + 1)$
- (C)  $2 \ln(x^3 + 1)$
- (D)  $2 \ln(8x^3 + 1)$
- (E)  $24x^2 \ln(8x^3 + 1)$

25.

For  $x > 0$ ,  $\frac{d}{dx} \int_1^{\sqrt{x}} \frac{1}{1+t^2} dt =$

- (A)  $\frac{1}{2\sqrt{x}(1+x)}$
- (B)  $\frac{1}{2\sqrt{x}(1+\sqrt{x})}$
- (C)  $\frac{1}{1+x}$
- (D)  $\frac{\sqrt{x}}{1+x}$
- (E)  $\frac{1}{1+\sqrt{x}}$

26.

 Let  $f(x) = \int_0^{x^2} \sin t dt$ . At how many points in the closed interval  $[0, \sqrt{\pi}]$  does the instantaneous rate of change of  $f$  equal the average rate of change of  $f$  on that interval?

6

- (A) Zero
- (B) One
- (C) Two
- (D) Three
- (E) Four

27. If  $f$  is a differentiable function and  $y = \sin(f(x^2))$  what is  $\frac{dy}{dx}$  when  $x = 3$ ?

- (A)  $\cos(f'(9))$
- (B)  $6\cos(f(9))$
- (C)  $(f'(9)\cos(f(9)))$
- (D)  $(6f'(9)\cos(f(9)))$

28. If  $f(x) = x^2 - 4$  and  $g$  is a differentiable function of  $x$ , what is the derivative of  $f(g(x))$ ?

- (A)  $2g(x)$
- (B)  $2g'(x)$
- (C)  $2xg'(x)$
- (D)  $2g(x)g'(x)$
- (E)  $2g(x) - 4$

29.

If  $f(x) = (2x^2 + 5)^7$ , then  $f'(x) =$

- (A)  $7(4x)^6$
- (B)  $7(2x^2 + 5)^6$
- (C)  $14x^2(2x^2 + 5)^6$
- (D)  $28x(2x^2 + 5)^6$

30.

If  $f(x) = \cos^2(3x - 5)$ , then  $f'(x) =$

- (A)  $6\cos(3x - 5)$
- (B)  $-3\sin^2(3x - 5)$
- (C)  $-2\sin(3x - 5)\cos(3x - 5)$
- (D)  $-6\sin(3x - 5)\cos(3x - 5)$



6

31.

$x$	$f(x)$	$f'(x)$	$g(x)$	$g'(x)$
-2	-6	9	-10	16
1	5	-3	3	-2
3	0	7	8	3

The table above gives values of  $f$ ,  $f'$ ,  $g$ , and  $g'$  for selected values of  $x$ . If  $h(x) = f(g(x))$ , what is the value of  $h'(1)$ ?

- (A) -19  
(B) -14  
(C) 7  
(D) 9

32.

$x$	$f(x)$	$f'(x)$	$g(x)$	$g'(x)$
-1	6	5	3	-2
1	3	-3	-1	2
3	1	-2	2	3

The table above gives values of  $f$ ,  $f'$ ,  $g$ , and  $g'$  at selected values of  $x$ . If  $h(x) = f(g(x))$ , then  $h'(1) =$

- (A) 5  
(B) 6  
(C) 9  
(D) 10  
(E) 12

33. If  $f(x) = ae^{-ax}$  for  $a > 0$ , then  $f'(x) =$

- (A)  $e^{-ax}$   
(B)  $ae^{-ax}$   
(C)  $a^2e^{-ax}$   
(D)  $-ae^{-ax}$   
(E)  $-a^2e^{-ax}$

34. If  $f'(x) = \frac{(x-2)^3(x^2-4)}{16}$  and  $g(x) = f(x^2 - 1)$ , what is  $g'(2)$ ?

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- (A) 2
- (B)  $\frac{5}{4}$
- (C)  $\frac{5}{8}$
- (D)  $\frac{5}{16}$
- (E) 0

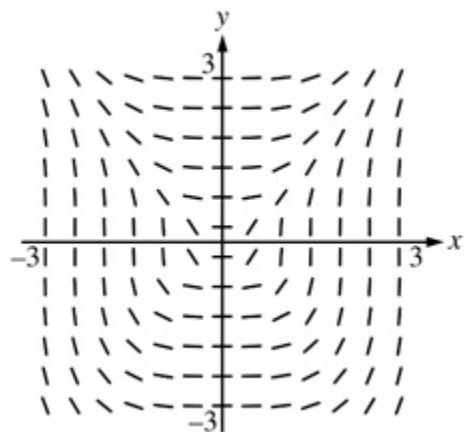
35.  $\frac{d}{dx}(\ln e^{2x}) =$

- (A)  $1/e^{2x}$
- (B)  $2/e^{2x}$
- (C)  $2x$
- (D) 1
- (E) 2

36. If  $y = x^2 \sin 2x$ , then  $\frac{dy}{dx} =$

- (A)  $2x \cos 2x$
- (B)  $4x \cos 2x$
- (C)  $2x(\sin 2x + \cos 2x)$
- (D)  $2x(\sin 2x - x \cos 2x)$
- (E)  $2x(\sin 2x + x \cos 2x)$

37.



Shown above is a slope field for which of the following differential equations?

6

- (A)  $\frac{dy}{dx} = \frac{x}{y}$
- (B)  $\frac{dy}{dx} = \frac{x^2}{y^2}$
- (C)  $\frac{dy}{dx} = \frac{x^3}{y}$
- (D)  $\frac{dy}{dx} = \frac{x^2}{y}$
- (E)  $\frac{dy}{dx} = \frac{x^3}{y^2}$

38. If  $f(x) = e^{2x}(x^3 + 1)$ , then  $f'(2) =$

- (A)  $6e^4$
- (B)  $21e^4$
- (C)  $24e^4$
- (D)  $30e^4$

39. If  $f(x) = \tan(2x)$ , then  $f'(\frac{\pi}{6}) =$

- (A)  $\sqrt{3}$
- (B)  $2\sqrt{3}$
- (C) 4
- (D)  $4\sqrt{3}$
- (E) 8

40. If  $y = \cos 2x$ , then  $\frac{dy}{dx} =$

- (A)  $-2\sin 2x$
- (B)  $-\sin 2x$
- (C)  $\sin 2x$
- (D)  $2 \sin 2x$
- (E)  $2 \sin x$

41.

If  $f(x) = \sin^2(3 - x)$ , then  $f'(0) =$

- (A)  $-2 \cos 3$
- (B)  $-2 \sin 3 \cos 3$
- (C)  $6 \cos 3$
- (D)  $2 \sin 3 \cos 3$
- (E)  $6 \sin 3 \cos 3$

6

42. If  $f(x) = (x^2 - 2x - 1)^{\frac{2}{3}}$ , then  $f'(0)$  is

- (A)  $\frac{4}{3}$
- (B) 0
- (C)  $-\frac{2}{3}$
- (D)  $-\frac{4}{3}$
- (E) -2

43. If  $f(x) = \sin(e^{-x})$ , then  $f'(x) =$

- (A)  $-\cos(e^{-x})$
- (B)  $\cos(e^{-x}) + e^{-x}$
- (C)  $\cos(e^{-x}) - e^{-x}$
- (D)  $e^{-x} \cos(e^{-x})$
- (E)  $-e^{-x} \cos(e^{-x})$

44. If  $f(x) = \ln(x + 4 + e^{-3x})$ , then  $f'(0)$  is

- (A)  $-\frac{2}{5}$
- (B)  $\frac{1}{5}$
- (C)  $\frac{1}{4}$
- (D)  $\frac{2}{5}$
- (E) nonexistent

45. If  $f(x) = \ln(x + 4 + e^{-3x})$ , then  $f'(0)$  is

- (A)  $-\frac{2}{5}$
- (B)  $\frac{1}{5}$
- (C)  $\frac{1}{4}$
- (D)  $\frac{2}{5}$
- (E) nonexistent

46.  $\frac{d}{dx}(\sin^3(x^2)) =$

- (A)  $\cos^3(x^2)$
- (B)  $3\sin^2(x^2)$
- (C)  $6x\sin^2(x^2)$
- (D)  $3\sin^2(x^2) \cos(x^2)$
- (E)  $6x\sin^2(x^2) \cos(x^2)$

6

47.  $\frac{d}{dx} \ln \left| \cos\left(\frac{\pi}{x}\right) \right|$  is

(A)  $\frac{-\pi}{x^2 \cos\left(\frac{\pi}{x}\right)}$

(B)  $-\tan\left(\frac{\pi}{x}\right)$

(C)  $\frac{1}{\cos\left(\frac{\pi}{x}\right)}$

(D)  $\frac{\pi}{x} \tan\left(\frac{\pi}{x}\right)$

(E)  $\frac{\pi}{x^2} \tan\left(\frac{\pi}{x}\right)$

48. If  $y = x^2 - 2x$  and  $u = 2x + 1$ , then  $\frac{dy}{du} =$

(A)  $\frac{2(x^2+x-1)}{(2x+1)^2}$

(B)  $6x^2 - 3x - 2$

(C)  $4x$

(D)  $x - 1$

(E)  $\frac{1}{x-1}$

49. If  $f(x) = \ln(\ln x)$ , then  $f'(x) =$

(A)  $1/x$

(B)  $1/\ln x$

(C)  $\ln x/x$

(D)  $x$

(E)  $1/x \ln x$

50.

If  $f(x) = (x - 1)(x^2 + 2)^3$ , then  $f'(x) =$

(A)  $6x(x^2+2)^2$

(B)  $6x(x - 1)(x^2 + 2)^2$

(C)  $(x^2 + 2)^2(x^2 + 3x - 1)$

(D)  $(x^2 + 2)^2(7x^2 - 6x + 2)$

(E)  $-3(x - 1)(x^2 + 2)^2$

51. If  $f(x) = (x - 1)^{\frac{3}{2}} + \frac{e^{x-2}}{2}$ , then  $f'(2) =$

6

- (A) 1
- (B)  $\frac{3}{2}$
- (C) 2
- (D)  $\frac{7}{2}$
- (E)  $\frac{3+e}{2}$

52. The slope of the line tangent to the graph of  $y = \ln(1 - x)$  at  $x = -1$  is

- (A) -1
- (B)  $-1/2$
- (C)  $1/2$
- (D)  $\ln 2$
- (E) 1

53. If  $f$  and  $g$  are twice differentiable and if  $h(x) = f(g(x))$ , then  $h''(x) =$

- (A)  $f''(g(x))[g'(x)]^2 + f'(g(x))g''(x)$
- (B)  $f''(g(x))g'(x) + f'(g(x))g''(x)$
- (C)  $f''(g(x))[g'(x)]^2$
- (D)  $f''(g(x))g''(x)$
- (E)  $f''(g(x))$

54. If  $\frac{d}{dx} f(x) = g(x)$  and if  $h(x) = x^2$ , then  $\frac{d}{dx} (f(h(x))) =$

- (A)  $g(x^2)$
- (B)  $2xg(x)$
- (C)  $g'(x)$
- (D)  $2xg(x^2)$
- (E)  $x^2g(x^2)$

55. If  $f(x) = \sin(x^2 + \pi)$ , then  $f'(\sqrt{2\pi}) =$

- (A)  $-2\sqrt{2\pi}$
- (B) -2
- (C) -1
- (D)  $\cos(2\sqrt{2\pi})$

56. If  $f$  is the function given by  $f(x) = e^{x/3}$ , which of the following is an equation of the line tangent to the graph of  $f$  at the point  $(3 \ln 4, 4)$ ?

6

- (A)  $y - 4 = \frac{4}{3}(x - 3 \ln 4)$
- (B)  $y - 4 = 4(x - 3 \ln 4)$
- (C)  $y - 4 = 12(x - 3 \ln 4)$
- (D)  $y - 3 \ln 4 = 4(x - 4)$

57. If  $f(x) = \sqrt{x^2 - 4}$  and  $g(x) = 3x - 2$ , then the derivative of  $f(g(x))$  at  $x = 3$  is

- (A)  $\frac{7}{\sqrt{5}}$
- (B)  $\frac{14}{\sqrt{5}}$
- (C)  $\frac{18}{\sqrt{5}}$
- (D)  $\frac{15}{\sqrt{21}}$
- (E)  $\frac{30}{\sqrt{21}}$

58. The slope of the line tangent to the graph of  $y = \ln(1-x)$  at  $x = -1$  is

- (A) -1
- (B) -1/2
- (C) 1/2
- (D)  $\ln 2$
- (E) 1

59. If  $f(x) = (\ln x)^2$ , then  $f''(\sqrt{e}) =$

- (A)  $\frac{1}{e}$
- (B)  $\frac{2}{e}$
- (C)  $\frac{1}{2\sqrt{e}}$
- (D)  $\frac{1}{\sqrt{e}}$
- (E)  $\frac{2}{\sqrt{e}}$

60.

Let  $h$  be a differentiable function, and let  $f$  be the function defined by  $f(x) = h(x^2 - 3)$ . Which of the following is equal to  $f'(2)$ ?

- (A)  $h'(1)$
- (B)  $4h'(1)$
- (C)  $4h'(2)$
- (D)  $h'(4)$
- (E)  $4h'(4)$

6

61. If  $\frac{d}{dx}(f(x)) = g(x)$  and  $\frac{d}{dx}(g(x)) = f(x^2)$ , then  $\frac{d^2}{dx^2}(f(x^3)) =$
- (A)  $f(x^6)$   
(B)  $g(x^3)$   
(C)  $3x^2g(x^3)$   
(D)  $9x^4f(x^6) + 6xg(x^3)$   
(E)  $f(x^6) + g(x^3)$
62.  $\frac{d}{dx}\left(2(\sin \sqrt{x})^2\right) =$
- (A)  $4 \cos\left(\frac{1}{2\sqrt{x}}\right)$   
(B)  $4 \sin \sqrt{x} \cos \sqrt{x}$   
(C)  $\frac{2 \sin \sqrt{x}}{\sqrt{x}}$   
(D)  $\frac{2 \sin \sqrt{x} \cos \sqrt{x}}{\sqrt{x}}$
63. If  $f(x) = (\cos(\sqrt{x}) - \ln(x^2))^3$ , then  $f'(x) =$
- (A)  $3\left(-\frac{1}{2\sqrt{x}}\sin(\sqrt{x}) - \frac{2}{x}\right)^2$   
(B)  $3(\cos(\sqrt{x}) - \ln(x^2))^2 \cdot \left(-\sin(\sqrt{x}) - \frac{1}{x^2}\right)$   
(C)  $3(\cos(\sqrt{x}) - \ln(x^2))^2 \cdot \left(\frac{1}{2\sqrt{x}}\cos(\sqrt{x}) - \frac{2}{x}\right)$   
(D)  $3(\cos(\sqrt{x}) - \ln(x^2))^2 \cdot \left(-\frac{1}{2\sqrt{x}}\sin(\sqrt{x}) - \frac{2}{x}\right)$
64. Let  $f(x) = 5x^4$  and  $g(x) = e^{2x} + x$ . If  $h$  is the function defined by  $h(x) = f(g(x))$ , which of the following gives a correct expression for  $h'(x)$ ?
- (A)  $20(g(x))^3 = 20(e^{2x} + x)^3$   
(B)  $20(g'(x))^3 = 20(2e^{2x} + 1)^3$   
(C)  $20(g(x))^3 \cdot g'(x) = 20(e^{2x} + x)^3 \cdot (2e^{2x} + 1)$   
(D)  $5(g'(x))^4 = 5(2e^{2x} + 1)^4$
65. Let  $f(x) = x^3$  and  $g(x) = \frac{x}{x-1}$ . If  $h$  is the function defined by  $h(x) = f(g(x))$ , which of the following gives a correct expression for  $h'(x)$ ?



6

- (A)  $3(g(x))^2 = 3\left(\frac{x}{x-1}\right)^2$   
(B)  $3(g'(x))^2 = 3\left(\frac{(x-1)-x}{(x-1)^2}\right)^2$   
(C)  $3(g(x))^2 g'(x) = 3\left(\frac{x}{x-1}\right)^2 \cdot \frac{(x-1)-x}{(x-1)^2}$   
(D)  $(g'(x))^3 = \left(\frac{(x-1)-x}{(x-1)^2}\right)^3$

66. Let  $f$  be the function defined by  $f(x) = e^{h(x)}$ , where  $h$  is a differentiable function. Which of the following is equivalent to the derivative of  $f$  with respect to  $x$ ?

- (A)  $e^{h(x)}$   
(B)  $e^{h'(x)}$   
(C)  $h'(x)e^{h(x)}$   
(D)  $h(x)e^{h(x)-1}$

67. If  $f(x) = \sqrt[3]{5x^2-7}$ , then  $f'(x) =$

- (A)  $\frac{10x}{3} (5x^2-7)^{-\frac{2}{3}}$   
(B)  $\frac{1}{3} (5x^2-7)^{-\frac{2}{3}}$   
(C)  $\frac{3}{4} (5x^2-7)^{\frac{4}{3}}$   
(D)  $\frac{1}{3} (10x)^{-\frac{2}{3}}$

68. If  $y = \sqrt{3x^2+1}$ , then  $\frac{dy}{dx} =$

- (A)  $\frac{1}{2\sqrt{6x}}$   
(B)  $\frac{1}{2\sqrt{3x^2+1}}$   
(C)  $\frac{3x}{\sqrt{3x^2+1}}$   
(D)  $3x\sqrt{3x^2+1}$

69. If  $f(x) = \sqrt{x^4+8}$ , then  $f'(-1) =$

- (A)  $-\frac{4}{3}$   
(B)  $-\frac{2}{3}$   
(C)  $-\frac{1}{6}$   
(D)  $\frac{1}{6}$

70. If  $f(x) = \sin(e^{3x})$ , then  $f'(x) =$

6

- (A)  $\cos(e^{3x})$
- (B)  $\cos(3e^{3x})$
- (C)  $e^{3x} \cos(e^{3x})$
- (D)  $3e^{3x} \cos(e^{3x})$

71. If  $f(x) = (e^{3x} + \sin(2x))^4$ , then  $f'(x) =$

- (A)  $4(3e^{3x} + 2 \cos(2x))^3$
- (B)  $4(e^{3x} + \sin(2x))^3(e^{3x} + \cos(2x))$
- (C)  $4(e^{3x} + \sin(2x))^3(3e^{3x} + 2 \sin(2x))$
- (D)  $4(e^{3x} + \sin(2x))^3(3e^{3x} + 2 \cos(2x))$

72. Let  $f$  be the function defined by  $f(x) = \sin(h(x))$ , where  $h$  is a differentiable function. Which of the following is equivalent to the derivative of  $f$  with respect to  $x$ ?

- (A)  $\cos(h(x))$
- (B)  $\cos(h'(x))$
- (C)  $\cos(h(x))h'(x)$
- (D)  $\sin(h(x))h'(x)$

73.  $\int \frac{x^2+1}{(x^3+3x-5)^3} dx =$

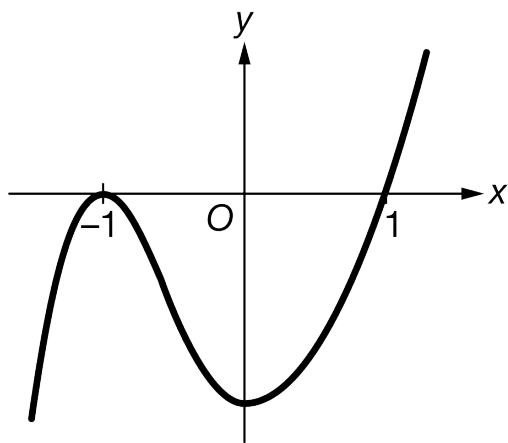
- (A)  $-\frac{3}{2} \cdot \frac{1}{(3x^2+3)^2} + C$
- (B)  $-\frac{1}{6} \cdot \frac{1}{(3x^2+3)^2} + C$
- (C)  $-\frac{3}{2} \cdot \frac{1}{(x^3+3x-5)^2} + C$
- (D)  $-\frac{1}{6} \cdot \frac{1}{(x^3+3x-5)^2} + C$

74.  $\frac{d}{dx}(x^3 \sec(2x)) =$

- (A)  $6x^2 \sec(2x) \tan(2x)$
- (B)  $2x^3 \tan^2(2x) + 3x^2 \sec(2x)$
- (C)  $x^3 \sec(2x) \tan(2x) + 3x^2 \sec(2x)$
- (D)  $2x^3 \sec(2x) \tan(2x) + 3x^2 \sec(2x)$

6

75.

Graph of  $f$ 

The figure above shows the graph of a differentiable function  $f$ . If  $g(x) = f(x^2)$ , which of the following statements is true?

- (A)  $g'(-1) < 0$
- (B)  $g'(-1) > 0$
- (C)  $g'(1) < 0$
- (D)  $g'(1) = 0$