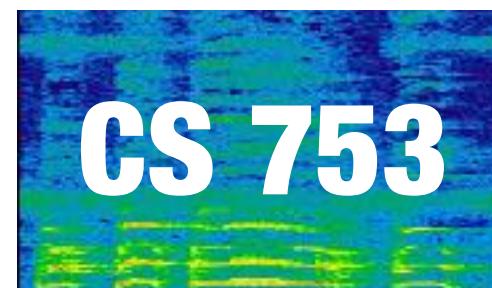


Search and Decoding

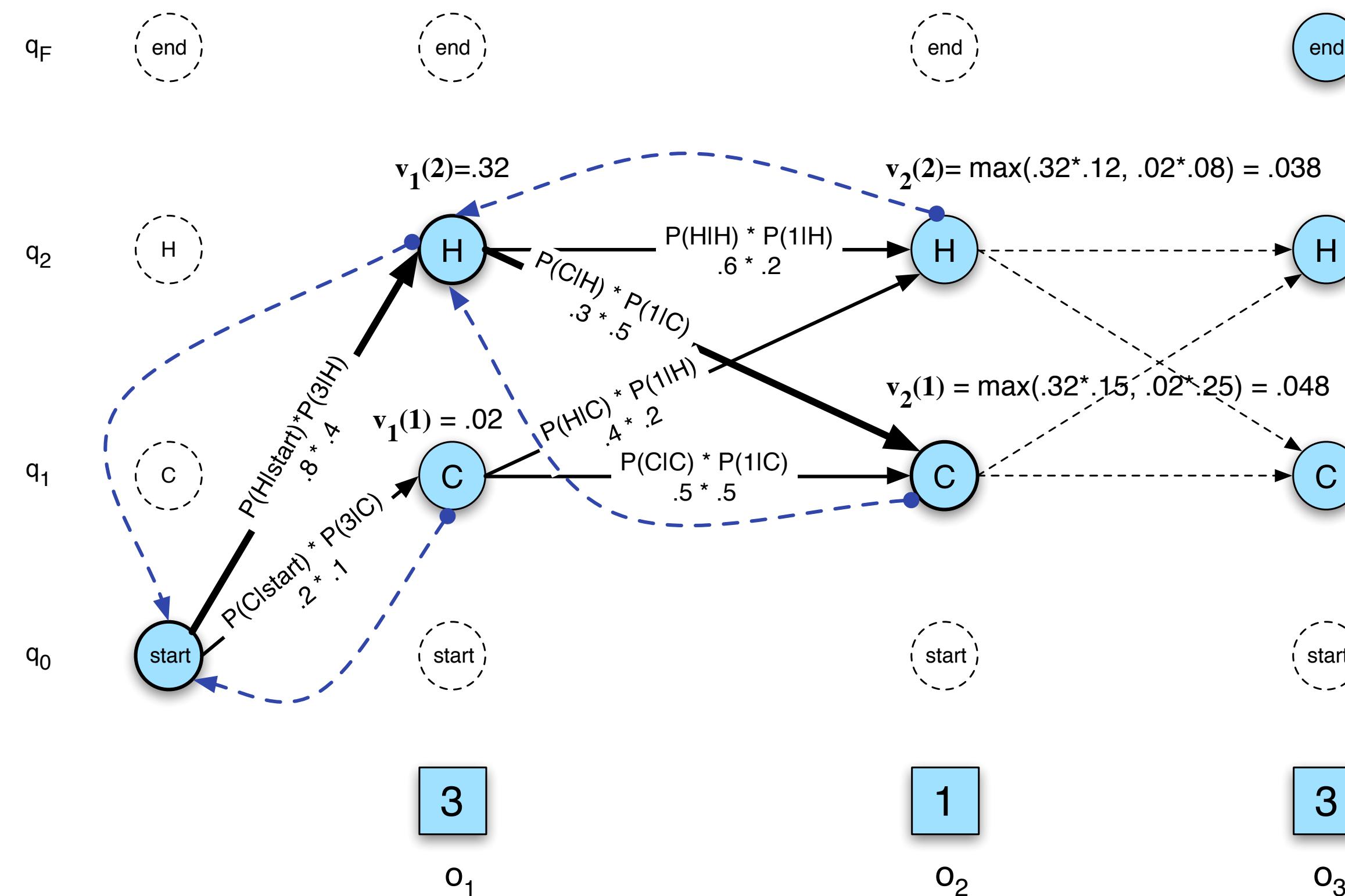
Lecture 16



Instructor: Preethi Jyothi

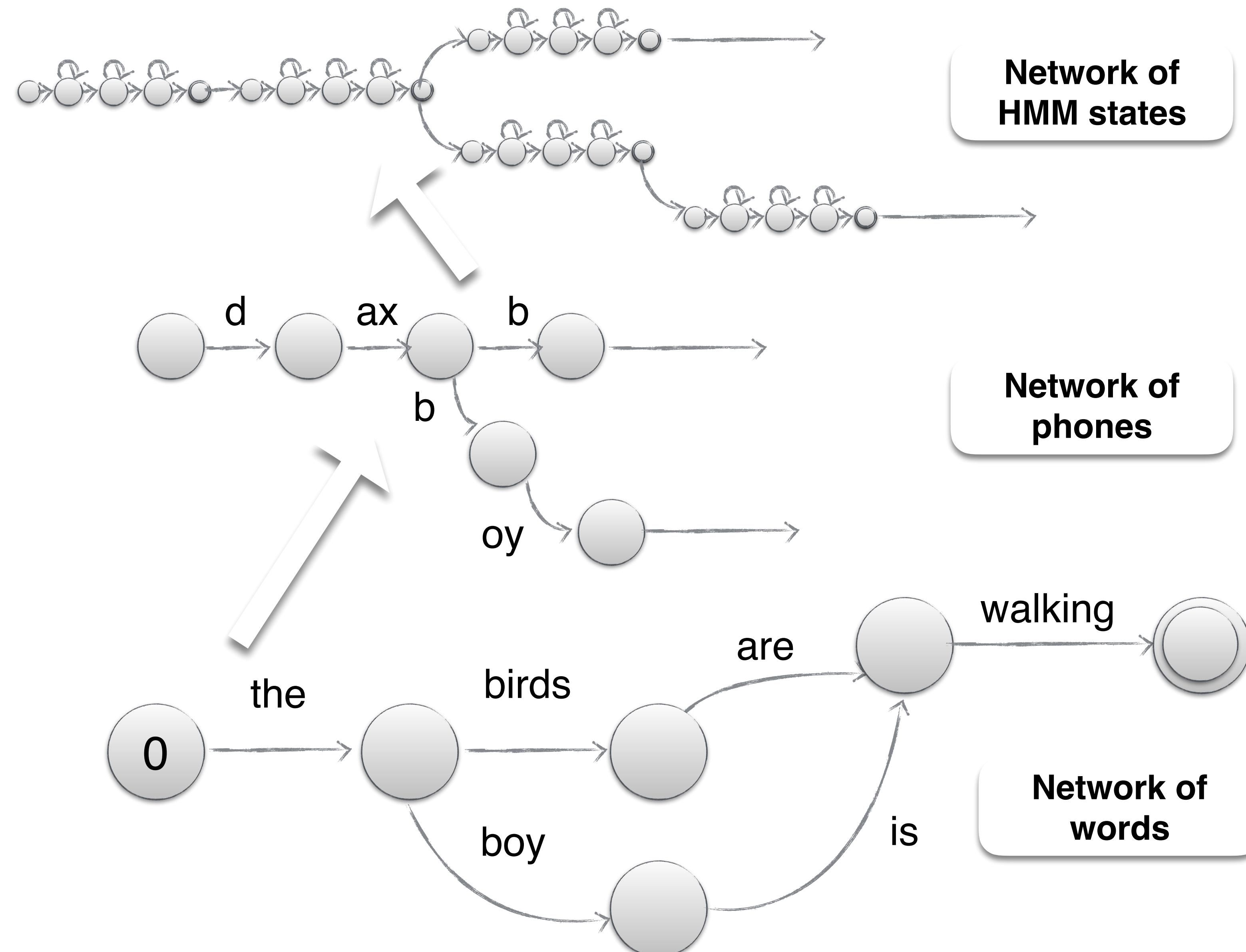
Recall Viterbi search

- Viterbi search finds the most probable path through a trellis of time on the X-axis and states on the Y-axis

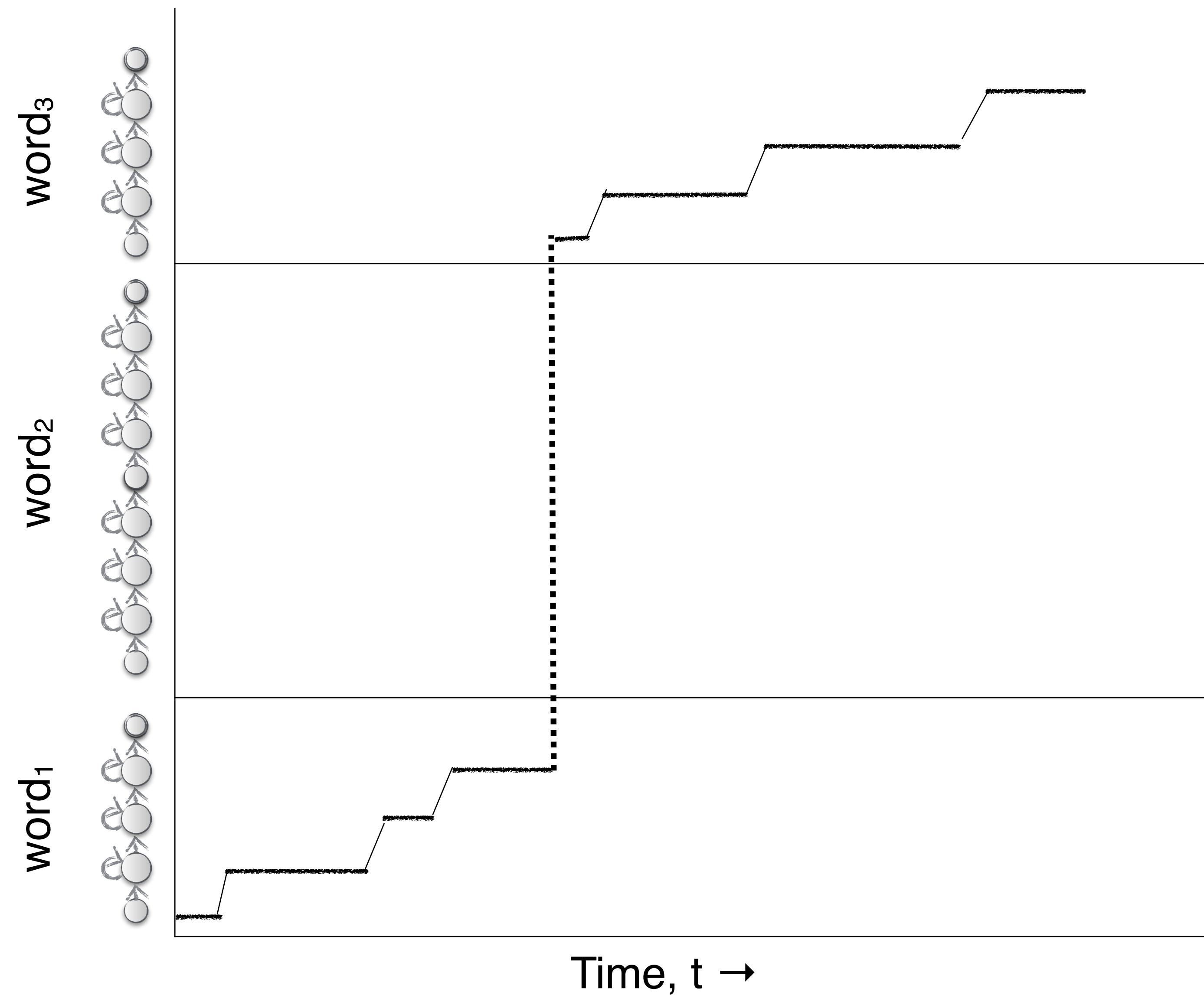


- Viterbi algorithm: Only needs to maintain information about the most probable path at each state

ASR Search Network



Time-state trellis



Viterbi search over the large trellis

- Exact search is infeasible for large vocabulary tasks
 - Unknown word boundaries
 - Ngram language models greatly increase the search space
- Solutions
 - Compactly represent the search space using WFST-based optimisations
 - Beam search: Prune away parts of the search space that aren't promising

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Two main WFST Optimizations

- Use determinization to reduce/eliminate redundancy

Recall not all weighted transducers are determinizable

To ensure determinizability of $L \circ G$, introduce disambiguation symbols in L to deal with homophones in the lexicon

read : r eh d #1
red : r eh d #2

Propagate the disambiguation symbols as self-loops back to C and H. Resulting machines are \tilde{H} , \tilde{C} , \tilde{L}

Two main WFST Optimizations

- Use determinization to reduce/eliminate redundancy
- Use minimization to reduce space requirements

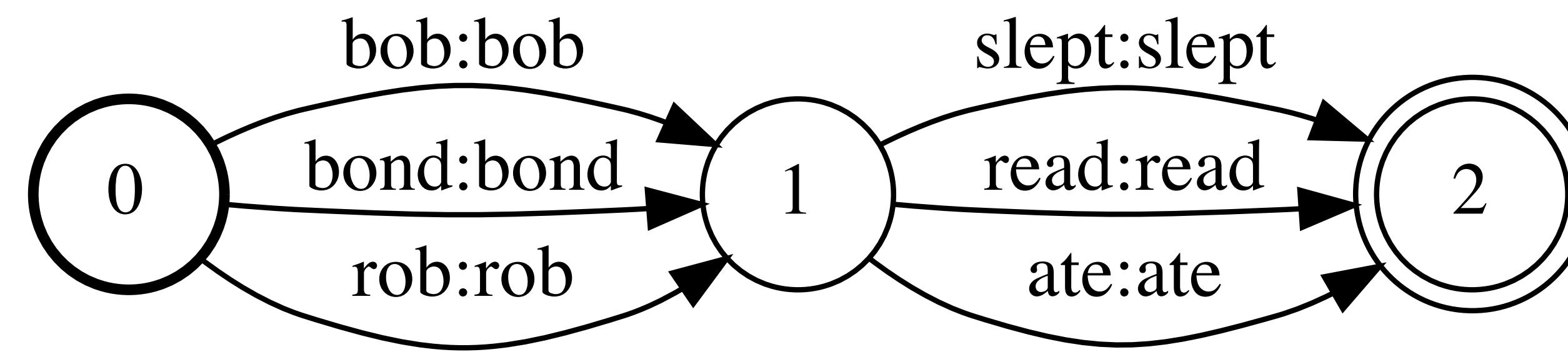
Minimization ensures that the final composed machine has minimum number of states

Final optimization cascade:

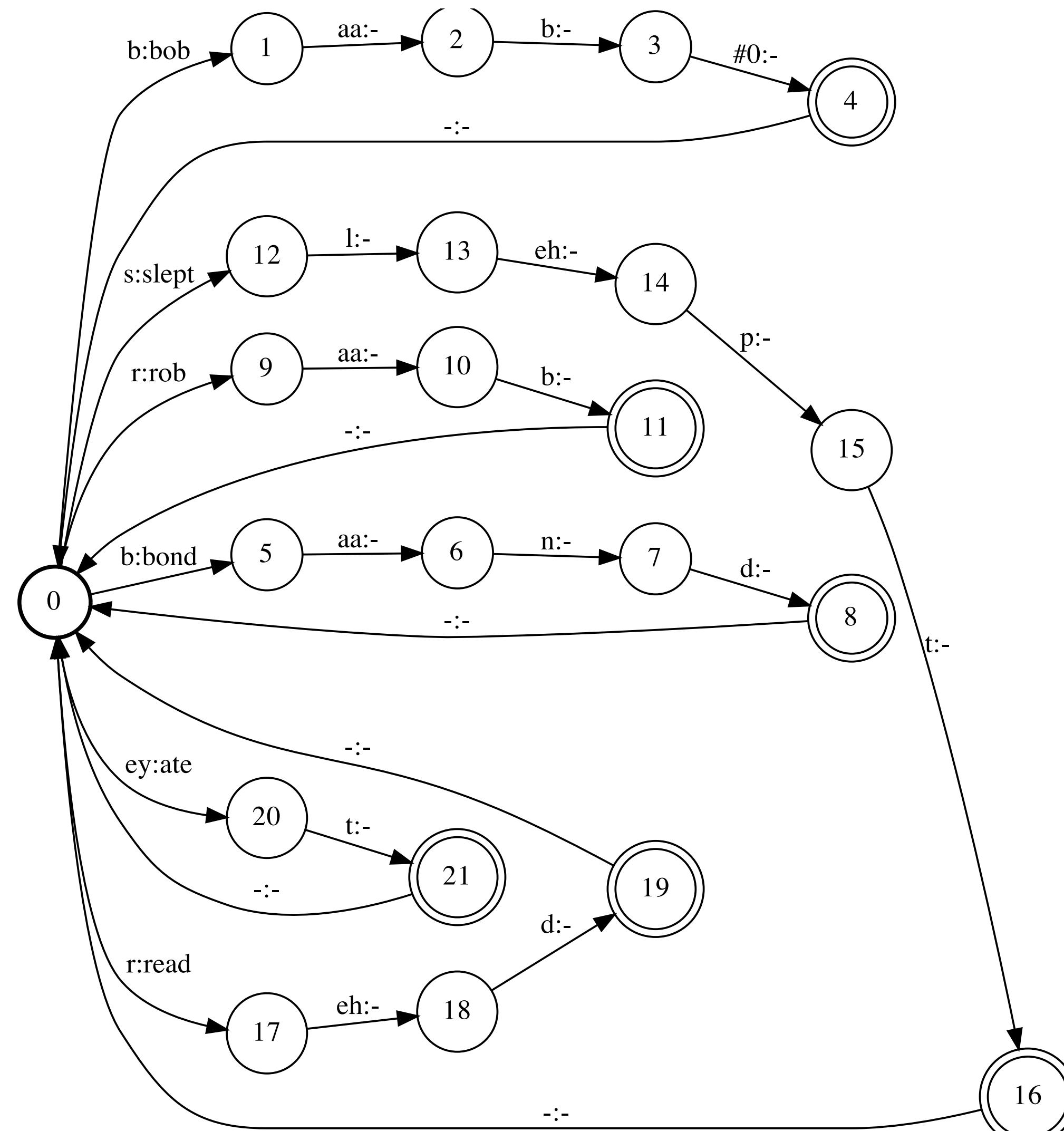
$$N = \pi_\epsilon(\min(\det(\tilde{H} \circ \det(\tilde{C} \circ \det(\tilde{L} \circ G)))))$$

Replaces disambiguation symbols
in input alphabet of \tilde{H} with ϵ

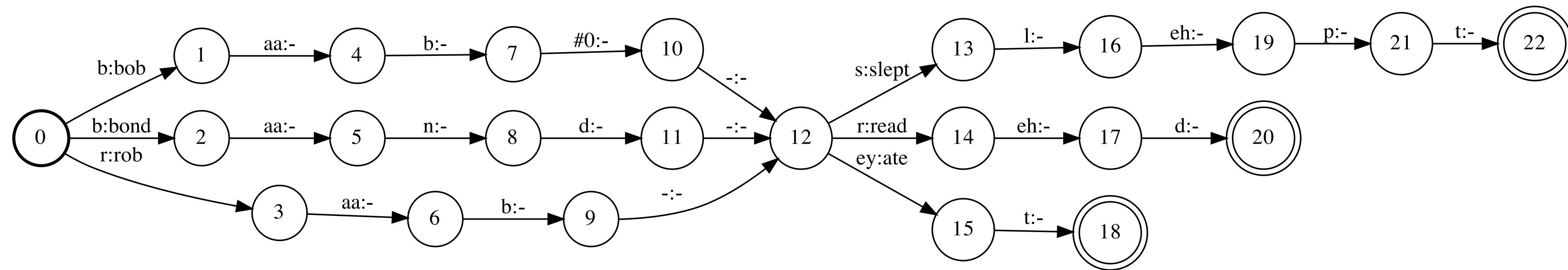
Example G



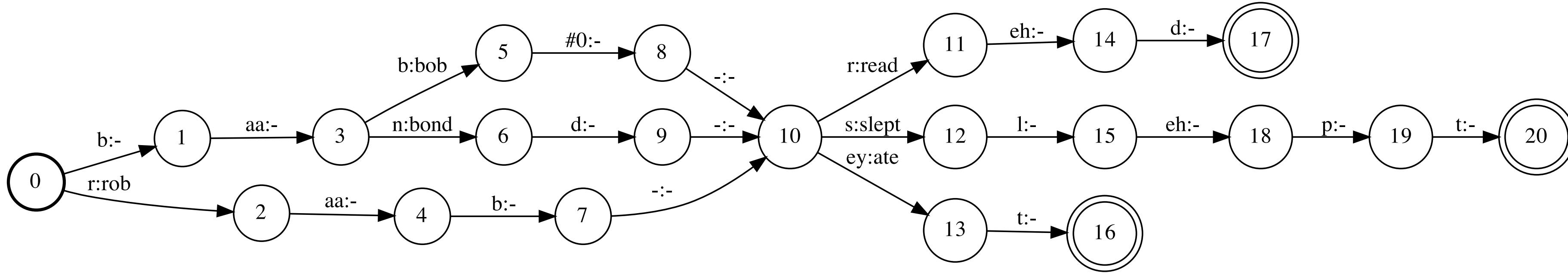
Example L̂ :Lexicon with disambig symbols



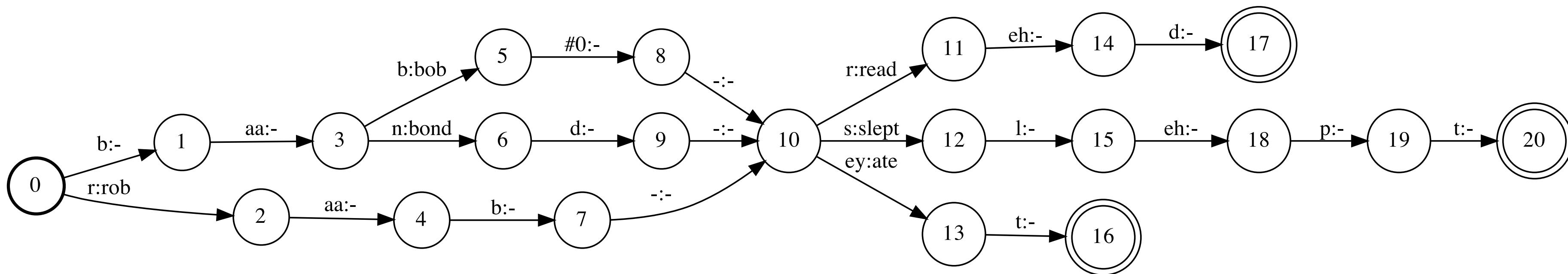
L . **G**



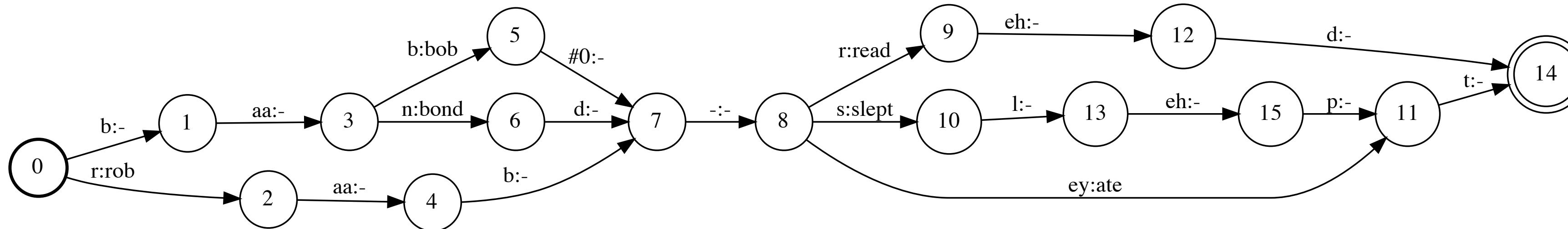
$$\det(\tilde{\mathbf{L}} \circ \mathbf{G})$$



$$\det(\tilde{\mathbf{L}} \circ \mathbf{G})$$



$$\min(\det(\tilde{\mathbf{L}} \circ \mathbf{G}))$$



1st pass recognition networks (40K vocab)

transducer	x real-time
$C \circ L \circ G$	12.5
$C \circ \text{det}(L \circ G)$	1.2
$\text{det}(H \circ C \circ L \circ G)$	1.0

Recognition speeds for systems with an accuracy of 83%

Static and dynamic networks

- What we've seen so far: Static decoding graph
 - $H \circ C \circ L \circ G$
 - Determinize/minimize to make this graph more compact
- Another approach: Dynamic graph expansion
 - Dynamically build the graph with active states on the fly
 - Do on-the-fly composition with the language model G
 - $(H \circ C \circ L) \circ G$

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Beam pruning

- At each time-step t , only retain those nodes in the time-state trellis that are within a fixed threshold δ (beam width) of the best path
- Given active nodes from the last time-step:
 - Examine nodes in the current time-step ...
 - ... that are reachable from active nodes in the previous time-step
 - Get active nodes for the current time-step by only retaining nodes with hypotheses that score close to the score of the best hypothesis

Viterbi beam search decoder

- Time-synchronous search algorithm:
 - For time t , each state is updated by the best score from all states in time $t-1$
 - Beam search prunes unpromising states at every time step.
 - At each time-step t , only retain those nodes in the time-state trellis that are within a fixed threshold δ (beam width) of the score of the best hypothesis.

Beam search algorithm

Initialization: current states := initial state

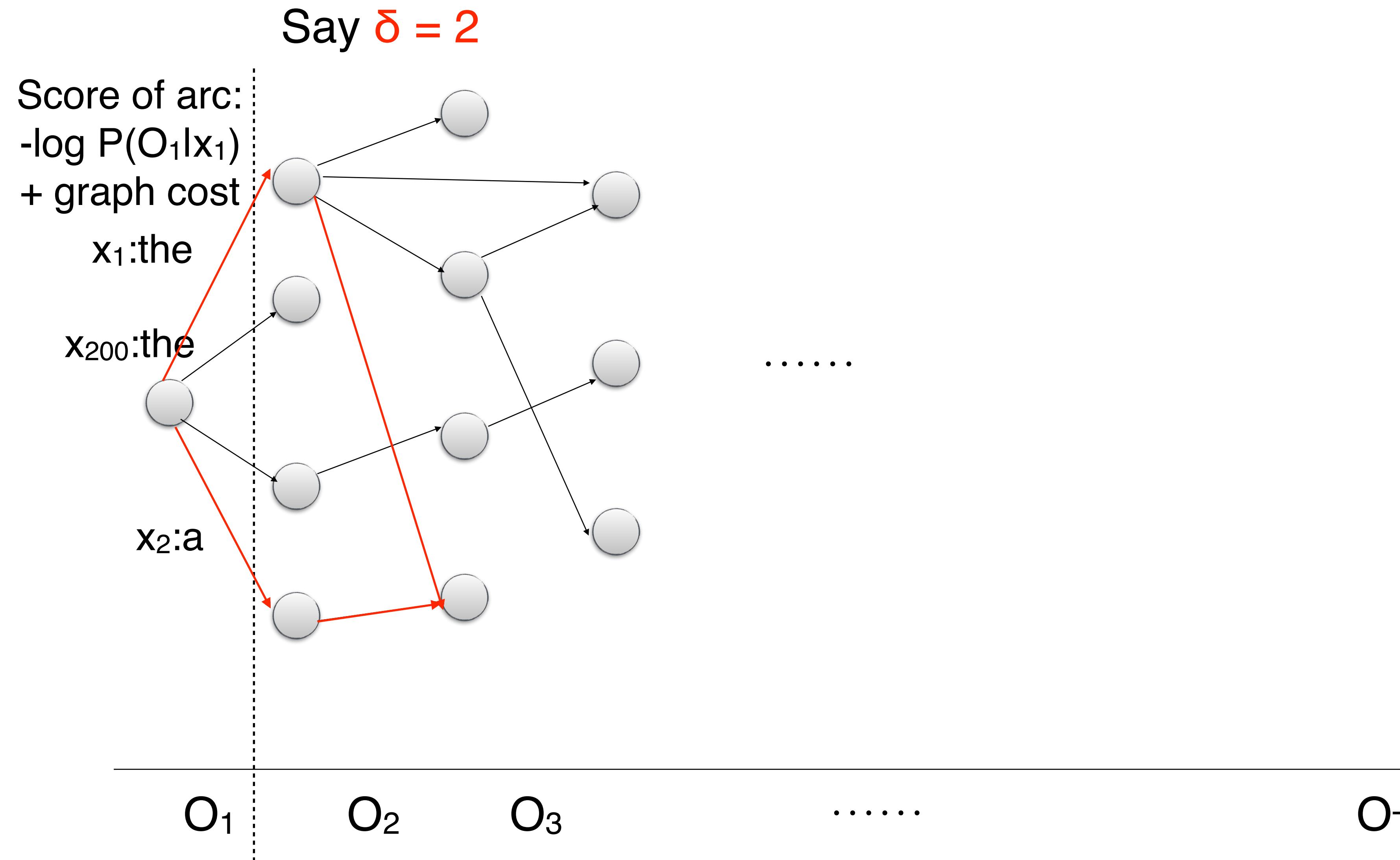
while (current states do not contain the goal state) do:

 successor states := NEXT(current states)
 where NEXT is next state function

 score the successor states

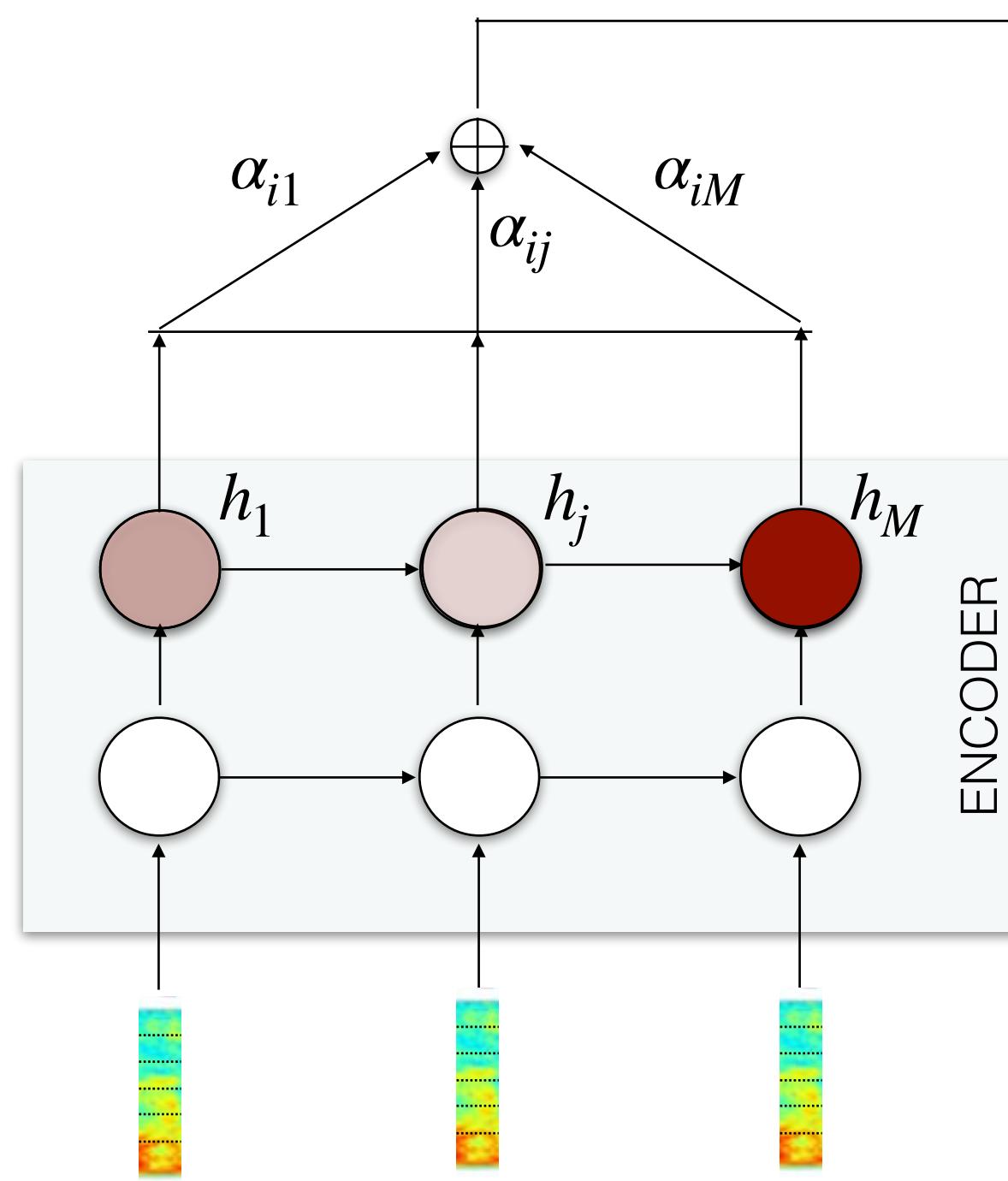
 set current states to a pruned set of successor states using
 beam width δ
 only retain those successor states that are within
 δ times the best path weight

Beam search over the decoding graph

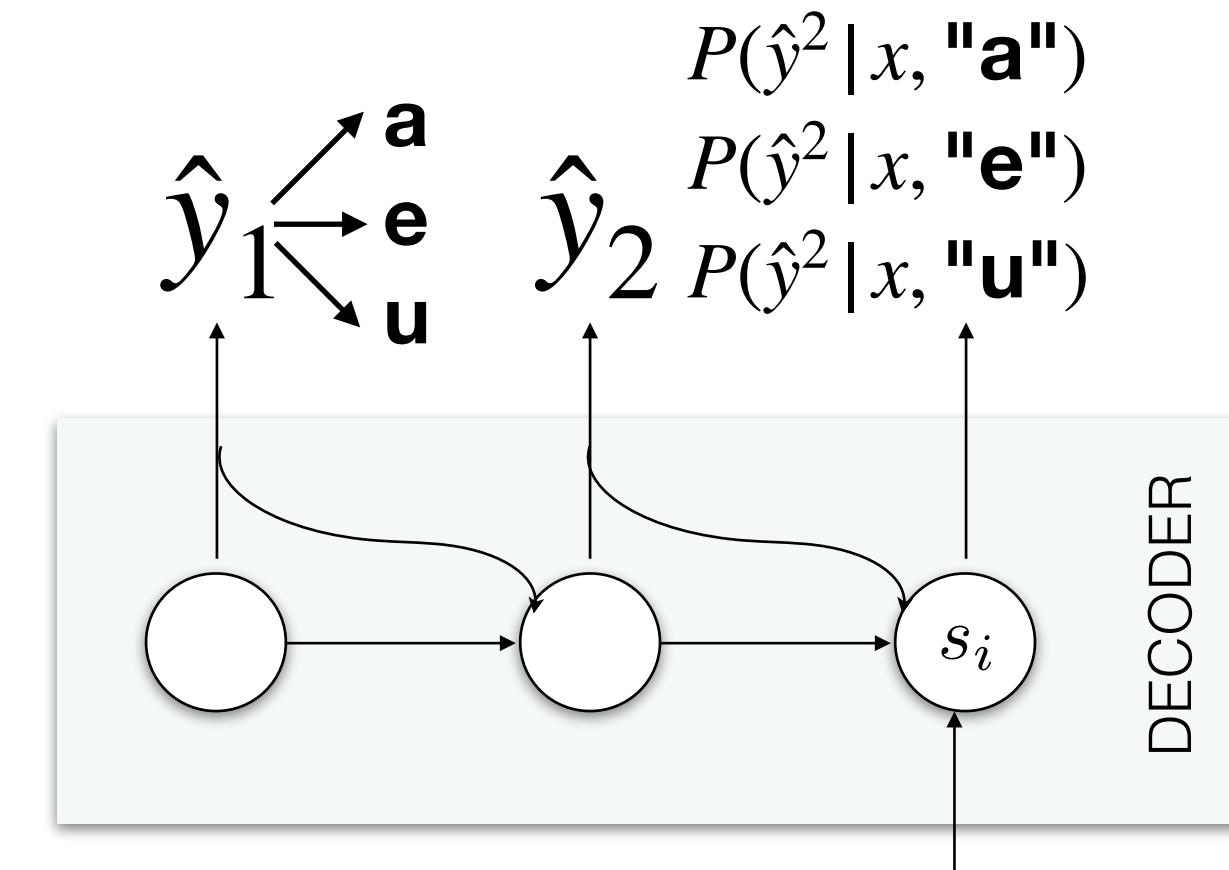


Beam search in a seq2seq model

Say $\delta = 3$



$$c_i = \sum_j \alpha_{ij} h_j$$



Lattices

- “**Lattices**” are useful when more than one hypothesis is desired from a recognition pass
- A lattice is a weighted, directed acyclic graph which encodes a large number of ASR hypotheses weighted by acoustic model +language model scores specific to a given utterance

Lattice Generation

- Say we want to decode an utterance, U , of T frames.
- Construct a sausage acceptor for this utterance, X , with $T+1$ states and arcs for each context-dependent HMM state at each time-step
- Search the following composed machine for the best word sequence corresponding to U :

$$D = X \circ HCLG$$

Lattice Generation

- For all practical applications, we have to use beam pruning over D such that only a subset of states/arcs in D are visited. Call this resulting pruned machine, B .
- Word lattice, say L , is a further pruned version of B defined by a lattice beam, β . L satisfies the following requirements:
 - L should have a path for every word sequence within β of the best-scoring path in B
 - All scores and alignments in L correspond to actual paths through B
 - L does not contain duplicate paths with the same word sequence