CS60050: Machine Learning

Assignment 3

Due date: Nov 8th

Q1. Suggest an algorithm for computing the bias term b in the dual SMO algorithm. Explain why this algorithm will always work.

Q2. Go back to implementation of logistic regression using SGD in the previous assignment. Implement the following variants:

- 1. Mini-batch SGD where you compute the stochastic gradient using a subset of examples of a specified size, say k. Vary k from from 0.1 % to 10% of the training set size.
- 2. Averaged SGD, where at the end of each iteration you maintain the average of last m iteration. Vary m as {1, 10, 100}
- 3. Minimum SGD, where at the end of each iteration you maintain the minimum of all previous iterations.

Compare the performance of the above methods for various values of m and k on the dataset Gisette available at:

https://www.csie.ntu.edu.tw/~cjlin/libsvmtools/datasets/binary.html

Plot the test set accuracy for the parameter in each iteration.

Q3. Generate a random dataset of 10 dimensional boolean variables, approx 1500 data points. Generate the class labels using a noisy version of the following function:

$$f(x) = x[10] + x[7] + 1$$
, where '+' denotes xoring.

The noise probability p (probability of flipping the output bit) can be varied from 0 to 50 % in steps of 10%. Train a decision tree using the ID3 algorithm implemented in weka. Plot the test set error as a function of p.

Q4. You have two coins with unknown probabilities of heads, denoted p and q respectively.

The first coin is chosen with probability π and the second coin is chosen with probability

- $(1-\pi)$. You toss the chosen coin and observe the outcome (head =1, tail =0).
 - 1. Write a latent variable model that describes the above scenario.
 - 2. Devise and EM algorithm to learn the parameters of the above model.
 - 3. Generate random data from the above model, and implement the EM algorithm to learn the parameters. Report both the original parameters and learned parameters.