

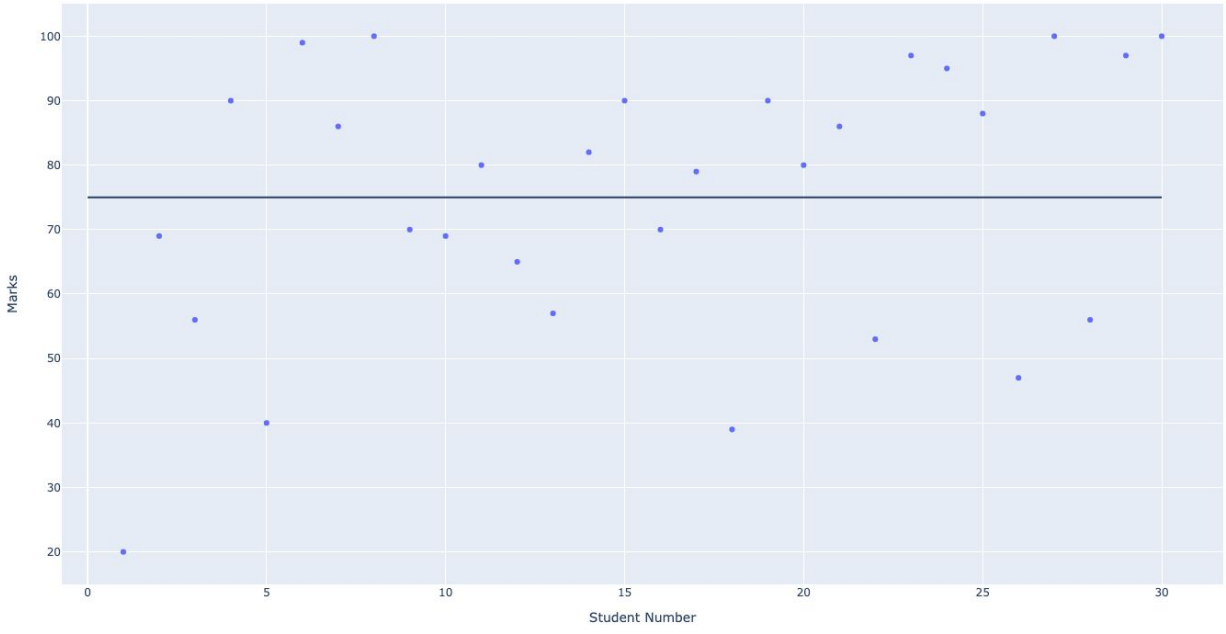
Topic	Introduction to Standard Deviation	
Class Description	Students will get an introduction to the Standard Deviation, what it is and why it is used.	
Class	C105	
Class time	45 mins	
Goal	<ul style="list-style-type: none"> To make students understand why the standard deviation is important and where it is used. To help students understand the formula for standard deviation, and write code for it. 	
Resources Required	<ul style="list-style-type: none"> Teacher Resources <ul style="list-style-type: none"> Visual Code studio Laptop with internet connectivity Earphones with mic Notebook and pen Student Resources <ul style="list-style-type: none"> Visual Code studio Laptop with internet connectivity Earphones with mic Notebook and pen 	
Class structure	Warm Up Teacher-led Activity Student-led Activity Wrap up	5 mins 15 min 15 min 10 min
<u>CONTEXT</u> <ul style="list-style-type: none"> Understanding more about data and central tendency 		
Class Steps	Teacher Action	Student Action
Step 1: Warm Up (5 mins)	Hi,How are you doing today? In the last class, we learnt about how	ESR: Varied

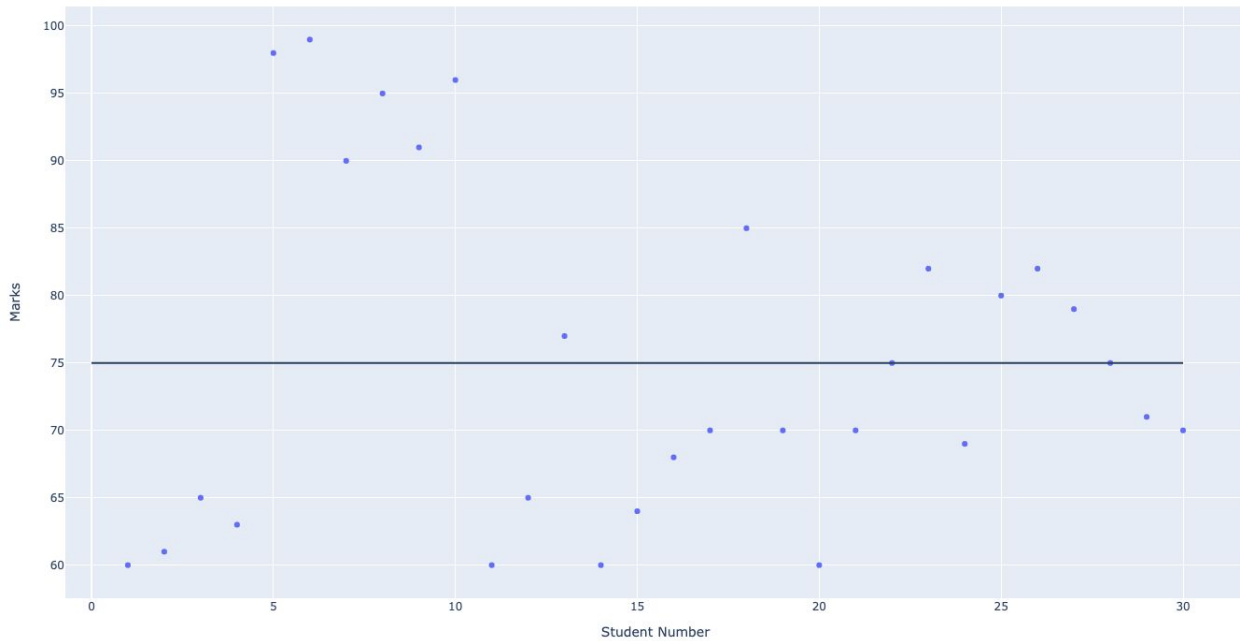
	<p>we can calculate the mean, median and mode.</p> <p>The mean, median and mode are all statistical terms used to find the central tendency of our data, through which we can say that the tendency for random data points in a data set would be around the mean, median or mode.</p>	
	<p>Today, we are going to understand what this means, by plotting scatter plots for marks of students in two different classrooms.</p>	-
	<p>You already know how to calculate the mean, the median and the mode. You also know how we can plot a scatter plot. Let's get into it.</p>	-
Teacher Initiates Screen Share		
<p style="text-align: center;"><u>CHALLENGE</u></p> <ul style="list-style-type: none"> Take the 2 data files, calculate the average marks scored in both the classrooms (mean) and plot the data in 2 different graphs. 		
Step 2: Teacher-led Activity (15 min)	<p>We will write 2 python programs. One to calculate the mean and plot a scatter plot on marks of student for class 1, the other to calculate the mean and plot a scatter plot on marks of student for class 2.</p>	-
	<p>Prompt the student to guide you through this, since they have already learnt how to calculate the mean and they have learnt how to plot a scatter plot.</p>	-

	<p>Let's start with the marks from class 1.</p> <p>Ask the student to guide you through on how you read the csv, derive the list of marks for students and calculate the mean (average) from it. code:-</p> <pre>import csv with open('class1.csv', newline='') as f: reader = csv.reader(f) file_data = list(reader) #To remove headers from CSV file_data.pop(0) total_marks = 0 total_entries = len(file_data) for marks in file_data: total_marks += float(marks[1]) mean = total_marks / total_entries print("Mean (Average) is -> "+str(mean))</pre> <p>Note that when printing, we are converting the mean from float type to string type with the str() method. Float types are numbers having a decimal value. In Python, we have to make sure to convert integers or floats as string.</p>	<p><Students should ask you to first import csv></p> <p><asks you to read the contents of the csv and remove the headers from the data></p> <p><asks you to calculate the total marks of all the students in the classroom and find the total number of students></p> <p><Tells the formula (Sum of Marks of all the students/ Total Students)></p>
--	---	--

	Run the code to see the average	
	<p>You should see the average as 75. Ask the student to help you plot a scatter plot for this data.</p> <p>Ask the student about what should be the X and the Y coordinates of the data.</p>	<p>X Coordinate should be the number of students, and the Y Coordinate should be the number of marks obtained.</p>
	<p>Plot the scatter plot based on the data. Ask the student to help you with the code, guiding you through and adding the following code to the existing file -</p> <pre>import pandas as pd import plotly.express as px df = pd.read_csv("class1.csv") fig = px.scatter(df, x="Student Number", y="Marks") fig.update_layout(shapes=[dict(type= 'line', y0= mean, y1= mean, x0= 0, x1= total_entries)]) fig.show()</pre> <p>One thing, that is different in this code from the previous one is that we are</p>	<p><Student should ask you to import the plotly and pandas library></p> <p><Student should ask you to read the csv file using Pandas></p> <p><Student should ask you to create a scatter plot with X coordinate as the Student Number and Y Coordinate as the Marks></p> <p><Students should ask you to display the graph></p>

	also displaying the line of average in our graph with the following code.	
	<pre>fig.update_layout(shapes=[dict(type= 'line', y0= mean, y1= mean, x0= 0, x1= total_entries)])</pre>	
	<p>In this code, we are saying that we want to update our figure, which is a scatter plot, and we want to add a shape to it.</p> <p>For the shapes, we have to define the attributes of that shape.</p> <p>Here, we are saying that we want the shape to be of type="line".</p> <p>Here, since we have marks in the Y Axis, Can we say that the average also lies in the Y Axis?</p> <p>In the code mentioned above, the X0 is the point from where the line will start in the X Coordinate, and X1 is the point where the line will end in the X Coordinate. We set the X0 as 0 and X1 as the total number of entries.</p> <p>Similarly, Y0 is the point from where the line is starting in the Y axis, and</p>	Yes

	<p>Y1 is the point where the line will end. Since our mean lies in the Y axis, we will keep the Y0 and Y1 the same.</p> <p>Our graph would look something like this.</p>	
		
	<p>Ask the student to help you replicate the steps for the second CSV, having marks of students from another class.</p>	<p>Students should help you repeat the steps you have repeated so far, to plot the graph and calculate mean for the second set of data.</p>
	<p>The mean for the second class should also be the same as 75. The graph would look something like this.</p>	-



Here, if we look closely, we can see that this second graph's Y Axis does not start with 0, since there are no values below 60.

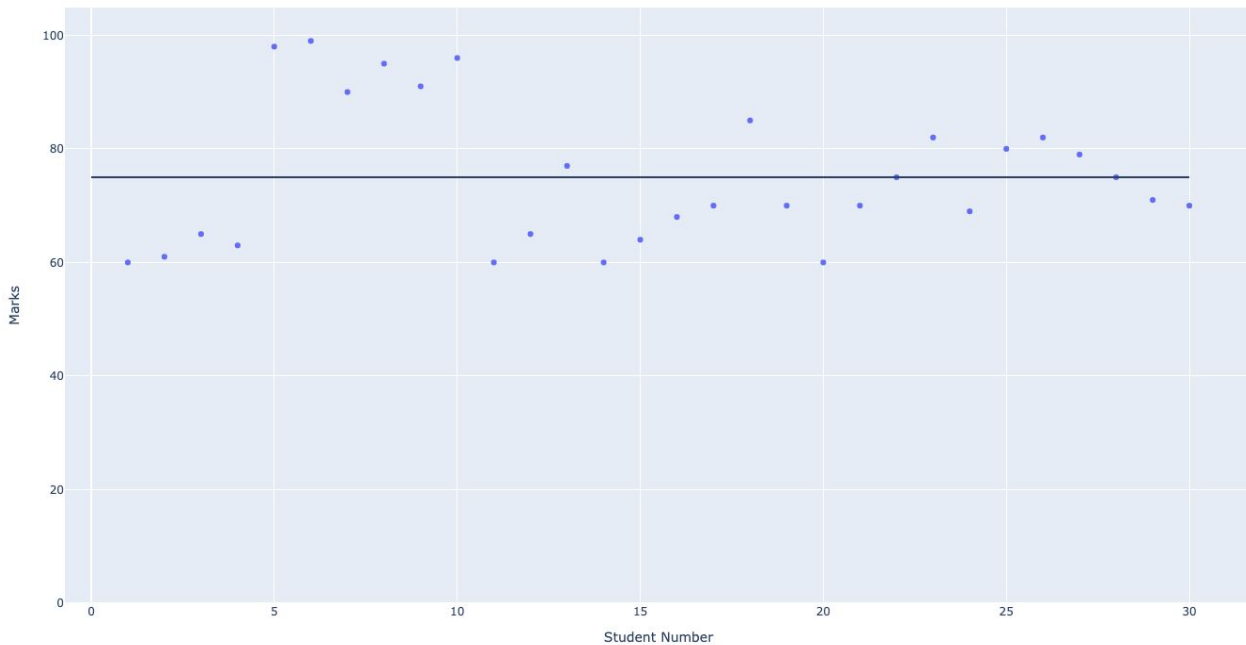
To make both the graphs consistent with each other, we will add the following line **before fig.show()**.

```
fig.update_yaxes(rangemode="tozero")
```

This line will update the figure's Y Axis, and we are asking the code to start the range of the Y Axis to 0.

The Graph now looks like the following.

Student observes and asks questions.



Let's compare the 2 graphs now. Both of the graphs have the same average, which is 75. Average is considered to be the central value of a data set which can be used to represent a data.

In here, If we look closely, we can see that while all the points are close to the line in the second graph, they are pretty far away in the first graph.

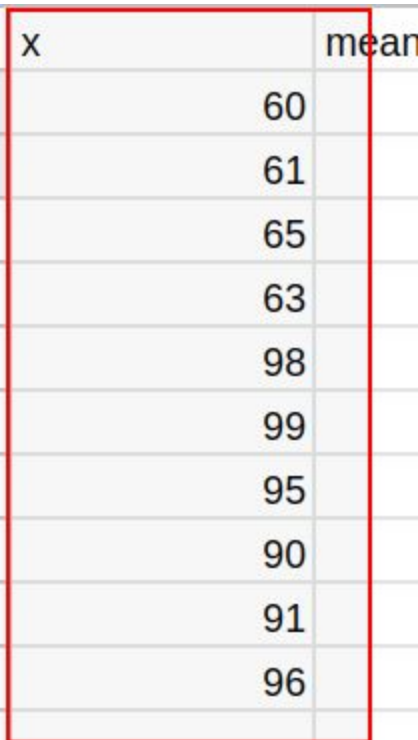
In the first graph, where the lowest point is 20 and the average is 75, is it fair that 75 is used to represent 20?

No

We need to find out how much our data is spreading out from the central tendency. Just by looking at the graph, we can clearly see that the

Varied Response

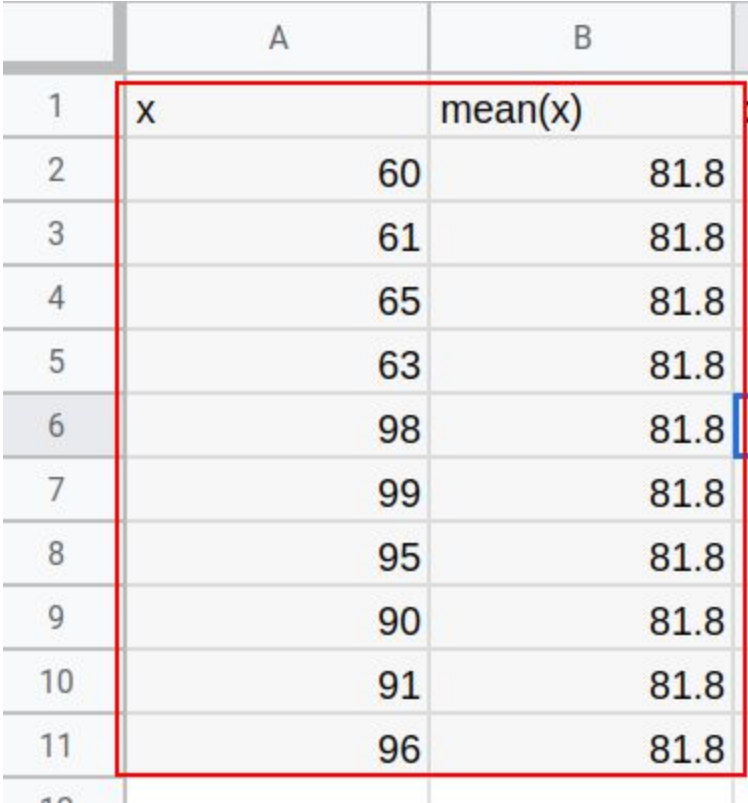
	<p>data spread in graph 1 is much more than the data spread in graph 2.</p> <p>The question is, by how much? Can we represent this with a number, of how much data spread each of the graphs represents from their central tendency?</p>	
	<p>We can say that the central tendency, or the average does not tell us much about the data.</p> <p>Standard deviation is a measure of how spread out a data set is.</p> <p>Without calculating the standard deviation of the data, we cannot know whether the data is close to average or whether the data is spread out over a wide range.</p> <p>So, let's see how we calculate the standard deviation.</p>	Varied or No response
	<p>The formula to calculate standard deviation is</p> $s = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n-1}}$ <p>where:- <i>X_i</i> is the each value in the dataset . <i>X</i> -bar is the mean of the values. <i>N</i> is the number of values in a dataset. Now we'll break down this formula and solve it step by step.</p>	

	<Teacher opens a new google sheet, names the column as X and adds a data set to it.	-
		
	<p>1. Calculate the average/mean of the numbers,</p> $\bar{x}.$ <p>In the next column the teacher adds a title as mean x. Can you tell me how we find the mean ?</p> <p>Perfect.</p> <p><Teacher selects a block below the title “mean x” and types “=Average”. Some suggestions pop up . Teacher</p>	<p>ESR:</p> <p>we calculate the sum of the values and then divide them by the number of values.</p>

selects the Average. Then select the whole list and press enter.

x		81.8 x	x-m
	60	=AVERAGE(A2:A11)	
	61		
	65		
	63		
	98		
	99		
	95		
	90		
	91		
	96		

1	x	mean(x)
2	60	81.8
3	61	
4	65	
5	63	
6	98	
7	99	
8	95	
9	90	
10	91	
11	96	

	<p>So 81.8 is the mean.</p> <p><Teacher hovers the cursor to the small blue square, it becomes + and then clicks it and drags it till the final value. this applies the formula to all the selected cells</p>	<p>Student observes and asks questions</p>																																				
 <table border="1"> <thead> <tr> <th></th><th>A</th><th>B</th></tr> </thead> <tbody> <tr> <td>1</td><td>x</td><td>mean(x)</td></tr> <tr> <td>2</td><td>60</td><td>81.8</td></tr> <tr> <td>3</td><td>61</td><td>81.8</td></tr> <tr> <td>4</td><td>65</td><td>81.8</td></tr> <tr> <td>5</td><td>63</td><td>81.8</td></tr> <tr> <td>6</td><td>98</td><td>81.8</td></tr> <tr> <td>7</td><td>99</td><td>81.8</td></tr> <tr> <td>8</td><td>95</td><td>81.8</td></tr> <tr> <td>9</td><td>90</td><td>81.8</td></tr> <tr> <td>10</td><td>91</td><td>81.8</td></tr> <tr> <td>11</td><td>96</td><td>81.8</td></tr> </tbody> </table>				A	B	1	x	mean(x)	2	60	81.8	3	61	81.8	4	65	81.8	5	63	81.8	6	98	81.8	7	99	81.8	8	95	81.8	9	90	81.8	10	91	81.8	11	96	81.8
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9	90	81.8																																				
10	91	81.8																																				
11	96	81.8																																				
	<p>2. Subtract the mean from each number (x)</p> <p>$(x_i - \bar{x})$.</p> <p>we'll write it as x - mean(x).</p> <p><In next column teacher gives title as "x-mean(x)".></p> <p>we'll subtract the mean from the main value.</p>	-																																				

<Teacher types =minus and selects the first value and the mean and presses enter. Add a comma(,) in between 2 numbers.
Then clicks on the blue circle and drags down till last value

	A	B	C
	x	mean(x)	
2	60	81.8	=MINUS(A2,B2)
3	61	81.8	
4	65	81.8	
5	63	81.8	
6	98	81.8	
7	99	81.8	
8	95	81.8	
9	90	81.8	
0	91	81.8	
1	96	81.8	

A	B	C
x	mean(x)	x-mean(x)
60	81.8	-21.8
61	81.8	-20.8
65	81.8	-16.8
63	81.8	-18.8
98	81.8	16.2
99	81.8	17.2
95	81.8	13.2
90	81.8	8.2
91	81.8	9.2
96	81.8	14.2

3. Square each of the differences,

$$(x_i - \bar{x})^2$$

In the next column of the sheet teacher gives the title

“(x-mean(x))sq”.

The next step is to square the difference between the main value and the mean.

To do that in the column we'll write “=POW” and select the first suggestion. POW takes the number and the power as arguments. <Teacher types “=POW” and selects the first suggestion and then selects the first value of the x-mean(x) and gives power as 2 and presses enter. Then clicks on the blue box and drags till the last value>

A	B	C	D
x	mean(x)	x-mean(x)	$(x - \text{mean}(x))^2$
60	81.8	-21.8	475.24
61	81.8	-20.8	432.64
65	81.8	-16.8	282.24
63	81.8	-18.8	353.44
98	81.8	16.2	262.44
99	81.8	17.2	295.84
95	81.8	13.2	174.24
90	81.8	8.2	67.24
91	81.8	9.2	84.64
96	81.8	14.2	201.64

C	D
x-mean(x)	(x-mean(x))sq
-21.8	475.24
-20.8	432.64
-16.8	282.24
-18.8	353.44
16.2	262.44
17.2	295.84
13.2	174.24
8.2	67.24
9.2	84.64
14.2	201.64

	<p>4. Add up all of the results from Step 3 to get the sum of squares,</p> $\sum (x_i - \bar{x})^2.$ <p>In the next column teacher gives the heading as “sum(x-mean(x))sq”.</p> <p>Now we have to get the sum of the squares . To do that we'll use the sum function and select all the values from the results.</p> <p><Teacher writes “=sum” and selects all the values. Then clicks on the small blue box and drags it down till last value to apply the formula to all the cells></p>	
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		D	E
		(x-mean(x))sq	sum(x-mean(x))sq
		475.24	2629.6
		432.64	2629.6
		282.24	2629.6
		353.44	2629.6
		262.44	2629.6
		295.84	2629.6
		174.24	2629.6
		67.24	2629.6
		84.64	2629.6
		201.64	2629.6

D	E
(x-mean(x))sq	2629.6 × an(x))sq
475.24	=SUM(D2:D11)
432.64	
282.24	
353.44	
262.44	
295.84	
174.24	
67.24	
84.64	
201.64	

5. Divide the sum of squares (found in Step 4) by the number of numbers minus one; that is, $(n - 1)$.

$$\frac{\sum (x_i - \bar{x})^2}{n - 1}$$

<teacher gives the next column a title as “sum/n-1”

here we have to divide the sum that we found before by number of

Student observes and asks questions about the formula.

	<p>values -1. we have total of 10 values and according to formula we subtract 1 from it so we have 9 values.</p> <p>we'll use the divide function.</p> <p><Teacher types “=DIVIDE” . Divide takes 2 arguments, a number to divide and the divisor.</p> <p>Teacher selects the sum we got before as the number to divide and 9 as divisor. Then clicks the small blue box and drags it down to apply the formula to all the cells.></p>	
--	--	--

E	F
sum(x-mean(x))sq)	sum/n-1
2629.6	=DIVIDE(E2,9)
2629.6	
2629.6	
2629.6	
2629.6	
2629.6	
2629.6	
2629.6	
2629.6	
2629.6	

E	F	
sum(x-mean(x))sq	sum/n-1	(
2629.6	292.1777778	
2629.6	292.1777778	
2629.6	292.1777778	
2629.6	292.1777778	
2629.6	292.1777778	
2629.6	292.1777778	
2629.6	292.1777778	
2629.6	292.1777778	
2629.6	292.1777778	
2629.6	292.1777778	
2629.6	292.1777778	

	<p>6.Take the square root to get the result</p> $s = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n-1}}$ <p><Teacher gives next column the title as “(sum/n-1)sqrt”</p> <p>the final step is to take the square root of the results.</p>	
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	To get the square root we'll write "=sqrt" and pass the result from the 5th step to it. <Teacher types "=sqrt" and passes the result from the 5th step to it.>																																																	
<table><tr><th>F</th><th>G</th><th>F</th><th>G</th></tr><tr><td>sum/n-1</td><td>(sum/n-1)sqrt</td><td>sum/n-1</td><td>(sum/n-1)sqrt</td></tr><tr><td>292.177777 ?</td><td>=SQRT(F2)</td><td>292.1777778</td><td>17.09320853</td></tr><tr><td>292.1777778</td><td></td><td>292.1777778</td><td>17.09320853</td></tr><tr><td>292.1777778</td><td></td><td>292.1777778</td><td>17.09320853</td></tr><tr><td>292.1777778</td><td></td><td>292.1777778</td><td>17.09320853</td></tr><tr><td>292.1777778</td><td></td><td>292.1777778</td><td>17.09320853</td></tr><tr><td>292.1777778</td><td></td><td>292.1777778</td><td>17.09320853</td></tr><tr><td>292.1777778</td><td></td><td>292.1777778</td><td>17.09320853</td></tr><tr><td>292.1777778</td><td></td><td>292.1777778</td><td>17.09320853</td></tr><tr><td>292.1777778</td><td></td><td>292.1777778</td><td>17.09320853</td></tr><tr><td>292.1777778</td><td></td><td>292.1777778</td><td>17.09320853</td></tr></table>			F	G	F	G	sum/n-1	(sum/n-1)sqrt	sum/n-1	(sum/n-1)sqrt	292.177777 ?	=SQRT(F2)	292.1777778	17.09320853	292.1777778		292.1777778	17.09320853	292.1777778		292.1777778	17.09320853	292.1777778		292.1777778	17.09320853	292.1777778		292.1777778	17.09320853	292.1777778		292.1777778	17.09320853	292.1777778		292.1777778	17.09320853	292.1777778		292.1777778	17.09320853	292.1777778		292.1777778	17.09320853	292.1777778		292.1777778	17.09320853
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	So the deviation we got is 17.09320853. Now we know how to find the deviation using the formula. I have a challenge for you , Can you write a program to find the deviation ?	ESR: YES!! <Student takes up the challenge>																																																
Teacher Stops Screen Share																																																		
	Now it's your turn. Please share your screen with me.																																																	

- Ask Student to press ESC key to come back to panel
- Guide Student to start Screen Share
- Teacher gets into Fullscreen

ACTIVITY

- Write a program to find the deviation of given data set.

Step 3: Student-Led Activity (15 min)

<Teacher helps student create a **std_deviation.py** file.>
 We'll follow the steps that we used to find the deviation.
 We have our data in a csv file, So first we have to write code to read the data from the csv, sort it and store it in a variable called **data**.
 <Teacher helps student write the code to read the csv and sort it and store it in data variable>
 code:-
import csv
with open('data.csv', newline='') as f:
reader = csv.reader(f)
file_data = list(reader)

#sorting the data to get the list
data = file_data[0]

<Student opens the editor and creates a file named **std_deviation.py**>

<Student writes code to read the csv and sort it and store it in data variable>

```

std_deviation.py  data.csv
1
2  import math
3  import csv
4  with open('data.csv', newline='') as f:
5      reader = csv.reader(f)
6      file_data = list(reader)
7
8  #sorting the data to get the list
9  data = file_data[0]
10

```

step1 . finding the mean.
we'll already know how to find the mean. let's code for it.
<Teacher helps student to write code to find the mean>
code:-
def mean(data):
 n= len(data)
 total =0
 for x in data:
 total += int(x)

 mean = total / n
 return mean

<Student writes the code to find the mean >

```

1
2 import math
3 import csv
4 with open('data.csv', newline='') as f:
5     reader = csv.reader(f)
6     file_data = list(reader)
7
8     #sorting the data to get the list
9     data = file_data[0]
10
11
12 # finding mean
13 def mean(data):
14     n = len(data)
15     total = 0
16     for x in data:
17         total += int(x)
18
19     mean = total / n
20     return mean
21
22

```

Step 2. Subtract the mean from all the values and square them .
How can we do that?

<teacher helps student with the code>

code:-

```

# squaring and getting the values
squared_list= []
for number in data:
    a = int(number) - mean(data)
    a= a**2

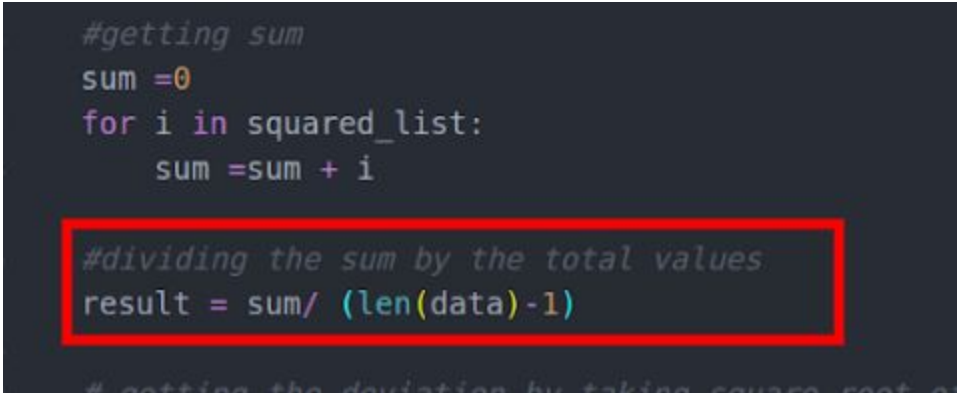
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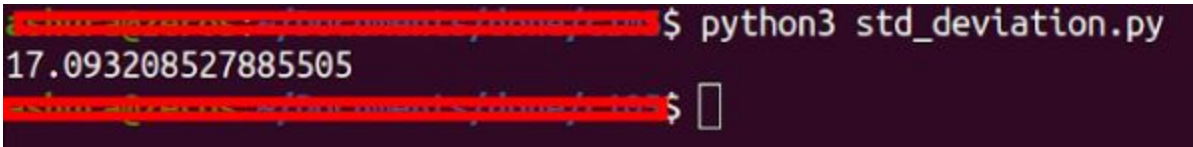
ESR:

We'll loop on the data list to access all the elements and then subtract the mean from the main value and square the result and append it to the list.

<Student codes to access the elements from the list using for loop then subtract

	squared_list.append(a)	the mean from the main value and square it.>
<pre> 22 23 24 # squaring and getting the values 25 squared_list= [] 26 for number in data: 27 a = int(number) - mean(data) 28 a= a**2 29 squared_list.append(a) 30 </pre>		
	<p>Step 3 . Get the sum of all the elements from the squared list.</p> <p><Teacher helps the student with the code></p> <p>code:-</p> <p>#getting sum</p> <p>sum =0</p> <p>for i in squared_list:</p> <p>sum =sum + i</p>	<Student codes to access the elements from the squared list and get the sum of it>
<pre> 30 31 #getting sum 32 sum =0 33 for i in squared_list: 34 sum =sum + i 35 </pre>		

	<p>Step 4 . Divide the sum by the number of values in the dataset.</p> <p>We already have the sum from the previous step , we have to divide it by the number of values .</p> <p><Teacher helps the student code to divide the sum by the length of the data and store it in the result variable></p> <p>code:</p> <p>#dividing the sum by the total values</p> <p>result = sum/ (len(data)-1)</p>	<p><Student codes to divide the sum by the length of the list.></p>
 <pre> #getting sum sum =0 for i in squared_list: sum =sum + i #dividing the sum by the total values result = sum/ (len(data)-1) </pre>		
	<p>step 5. get the square root of the result we got earlier from step 5.</p> <p>python has a math module which has a sqrt() . This function returns the square root of the given value.</p> <p>To use the sqrt() we need to import the math module first using “import math”</p>	<p><Student codes to import and using the math.sqrt() function to get the std_deviation></p>

	<p><Teacher helps the student with importing and using the math.sqrt() function to get the std_deviation and then print the std_deviation.></p>	
<pre>#dividing the sum by the total values result = sum/ (len(data)-1) # getting the deviation by taking square root of the result std_deviation = math.sqrt(result) print(std_deviation)</pre>		
	<p>Now run and test the code</p>	<p><student runs and tests the code></p>
		
	<p>As we see the deviation that we got by solving the formula is same as the deviation that we got from the program</p>	
<p>Teacher Guides Student to Stop Screen Share</p>		

FEEDBACK

- Appreciate the student for their class
- Get them the idea to find the deviation of multiple datasets

Step 4: Wrap-Up (5 min)	Let's quickly wrap up today's class. What did we learn?	ESR: We learned about the standard deviation. We learned how to find it using the formula. We wrote code to get the std deviation using the program.
	In next class we'll see how to find the correlation Excited for it?	Yes!
	Looking forward to the next class then	
<div style="display: flex; justify-content: space-between; align-items: center;"> <div>Teacher Clicks</div> <div style="background-color: red; color: white; padding: 5px 15px; border-radius: 10px;">✕ End Class</div> </div>		
Additional Activities	Encourage the student to write reflection notes in their reflection journal using markdown. Use these as guiding questions: <ul style="list-style-type: none"> • What happened today? <ul style="list-style-type: none"> - Describe what happened - Code I wrote • How did I feel after the class? 	The student uses the markdown editor to write her/his reflection in a reflection journal.

	<ul style="list-style-type: none"> • What have I learned about programming and developing games? • What aspects of the class helped me? What did I find difficult? 	
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Activity	Activity Name	Links
Teacher Activity 1	Final Solution	https://github.com/whitehatjr/Standard_deviation/tree/master/solution
Teacher Activity 2	code for graphs	https://github.com/whitehatjr/Standard_deviation/tree/master/graphs