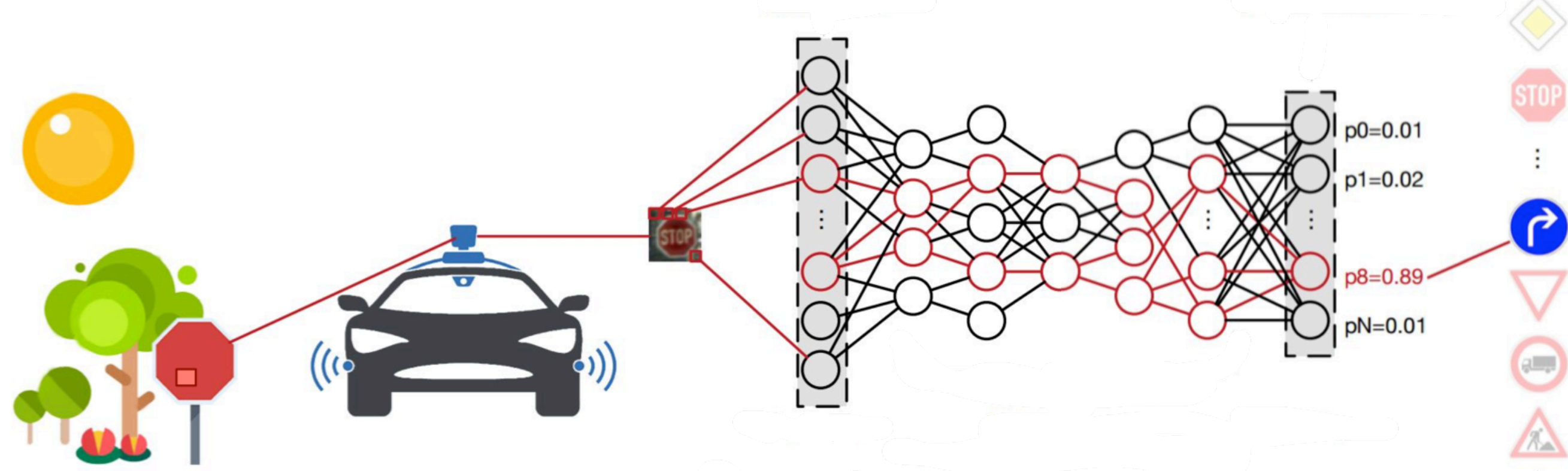


## Motivation

**Adversarial example:** small worst-case perturbation that forces a machine learning model to mishandle an input

- exists for image classification [1] and in the real world [2]



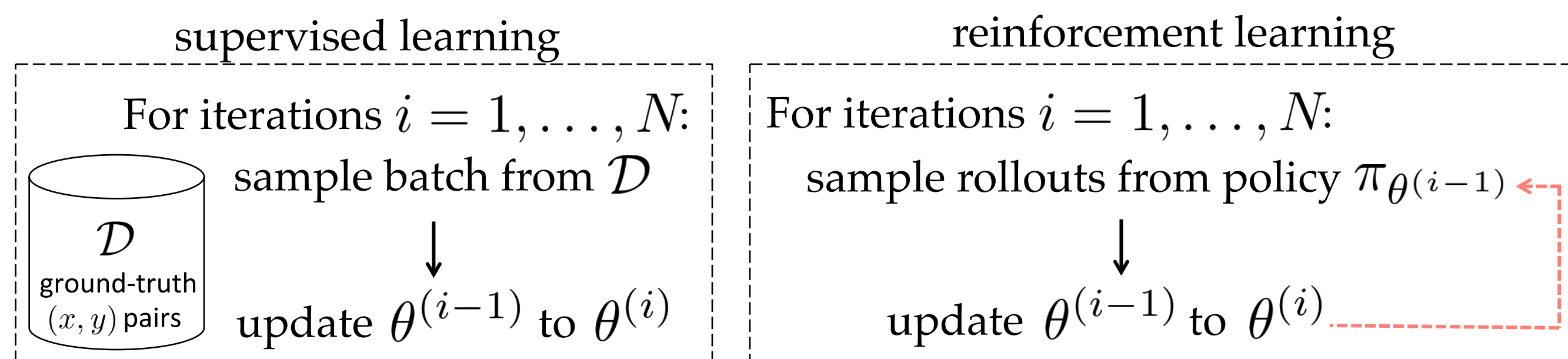
**Key finding:** Adversaries can degrade test-time behavior of policies trained with reinforcement learning, even when they do not have access to the policies

## Threat Model

white-box adversary:  $\theta' = \theta$

black-box adversary:

- adversary trains its own policy  $\pi_{\theta'}$  for the task
- requires *transferability*: can adversarial ex. designed to fool one policy also fool others trained for the same task?
- challenging because training data drawn from different distributions:

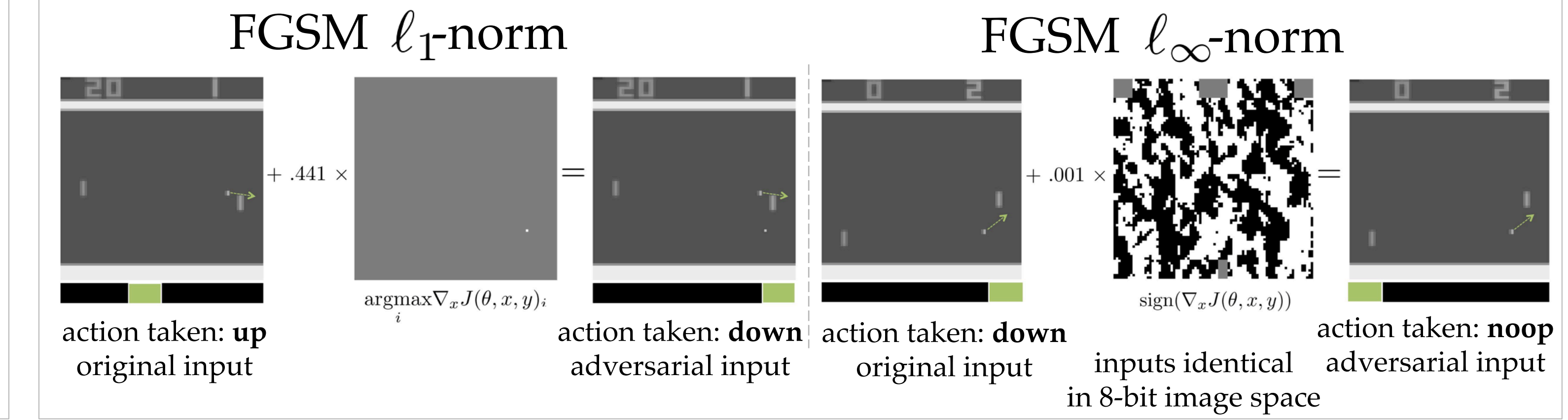


## Dormant Adversarial Examples

We introduce dormant attacks (on recurrent policies):

| Time:                | t | t+1 | ... | t+k-1 | t+k |                           |
|----------------------|---|-----|-----|-------|-----|---------------------------|
| w/o adversary        | ✓ | ✓   | ... | ✓     | ✓   |                           |
| w/ adversary         | ✗ | ✗   | ... | ✗     | ✗   | □ perturbation            |
| w/ dormant adversary | ✓ | ✓   | ... | ✓     | ✗   | ✓ optimal<br>✗ suboptimal |

## Examples of Adversarial Perturbations



## Crafting Adversarial Examples for Policies

Optimal perturbation  $\eta$ , given loss  $J(x)$ :  $\arg\max_{\eta} J(x + \eta)$

$$J(\theta, x, y) = - \sum_i y_i \log \pi_{\theta}(x)_i = - \log \arg\max_i \pi_{\theta}(x)_i$$

Fast gradient sign method (FGSM) [3] computes the optimal  $\eta$  for the linear approximation of  $J(x)$

Original version of FGSM constrains  $\|\eta\|_{\infty}$

Instead, we might want to constrain sparsity / magnitude

$$\eta = \begin{cases} \epsilon \text{sign}(\nabla_x J(\theta, x, y)) & \text{for } \|\eta\|_{\infty} \leq \epsilon \\ \epsilon \sqrt{d} \frac{\nabla_x J(\theta, x, y)}{\|\nabla_x J(\theta, x, y)\|_2} & \text{for } \|\eta\|_2 \leq \|\epsilon \mathbf{1}_d\|_2 \\ \text{maximally perturb dimensions with budget } \epsilon d & \text{for } \|\eta\|_1 \leq \|\epsilon \mathbf{1}_d\|_1 \end{cases}$$

## Crafting Dormant Adversarial Examples

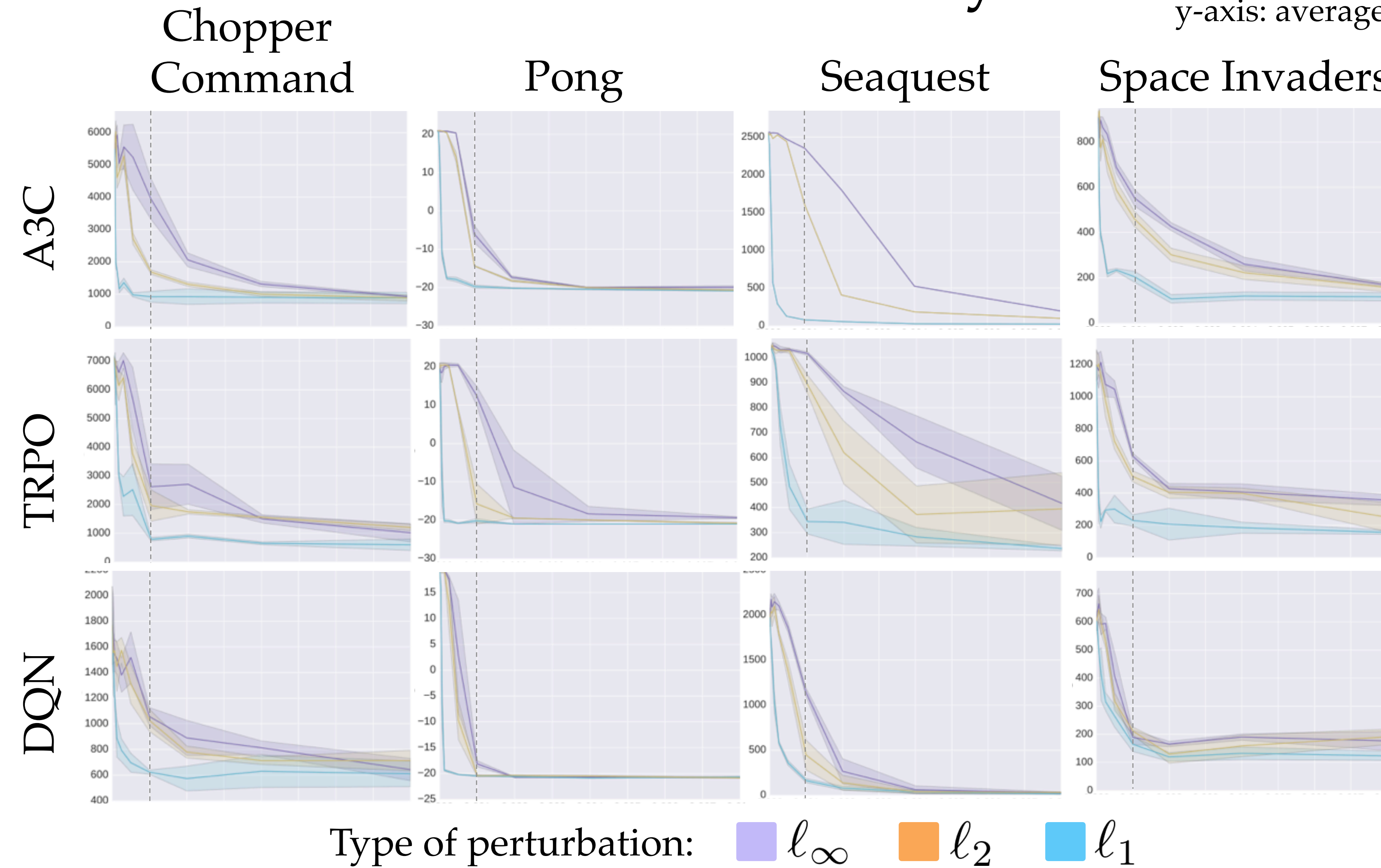
$$\arg\max_{\eta} J(\theta, x_t + \eta, y_t)$$

$$\text{subject to } d_i(\eta; \theta, x_{0:t}) = 0 \text{ for } i = 0, \dots, k-1, \\ d_k(\eta; \theta, x_{0:t}) = 1, \|\eta\| \leq \epsilon$$

$$\text{Optimize with dual ascent: } \eta^{(j)} = -\epsilon \left( \sum_{i=0}^{k-1} \lambda_i^{(j)} \text{sign}(\nabla_x J(\theta, x_{t+i}, y_{t+i})) \right) + \epsilon \lambda_k^{(j)} \text{sign}(\nabla_x J(\theta, x_{t+k}, y_{t+k})).$$

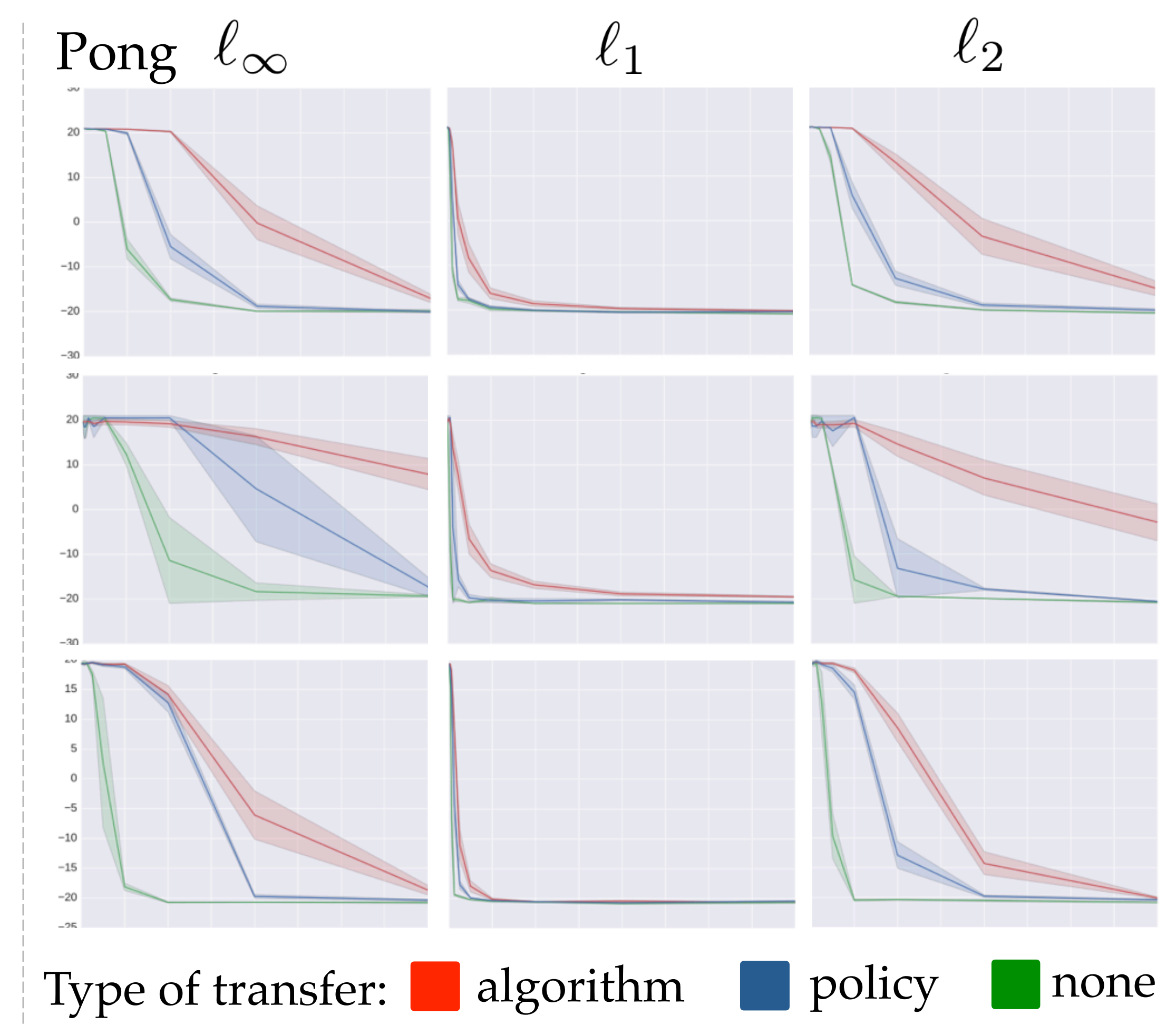
$$\lambda_i^{(j+1)} = \lambda_i^{(j)} + \alpha^{(j)} d_i(\eta^{(j)}; \theta, x_{0:t}) \text{ for } i = 0, \dots, k$$

## White-Box Adversary



- Across all games, adversarial perturbations significantly decrease performance, even for small  $\epsilon$
- Policies trained with DQN tend to be more vulnerable

## Black-Box Adversary

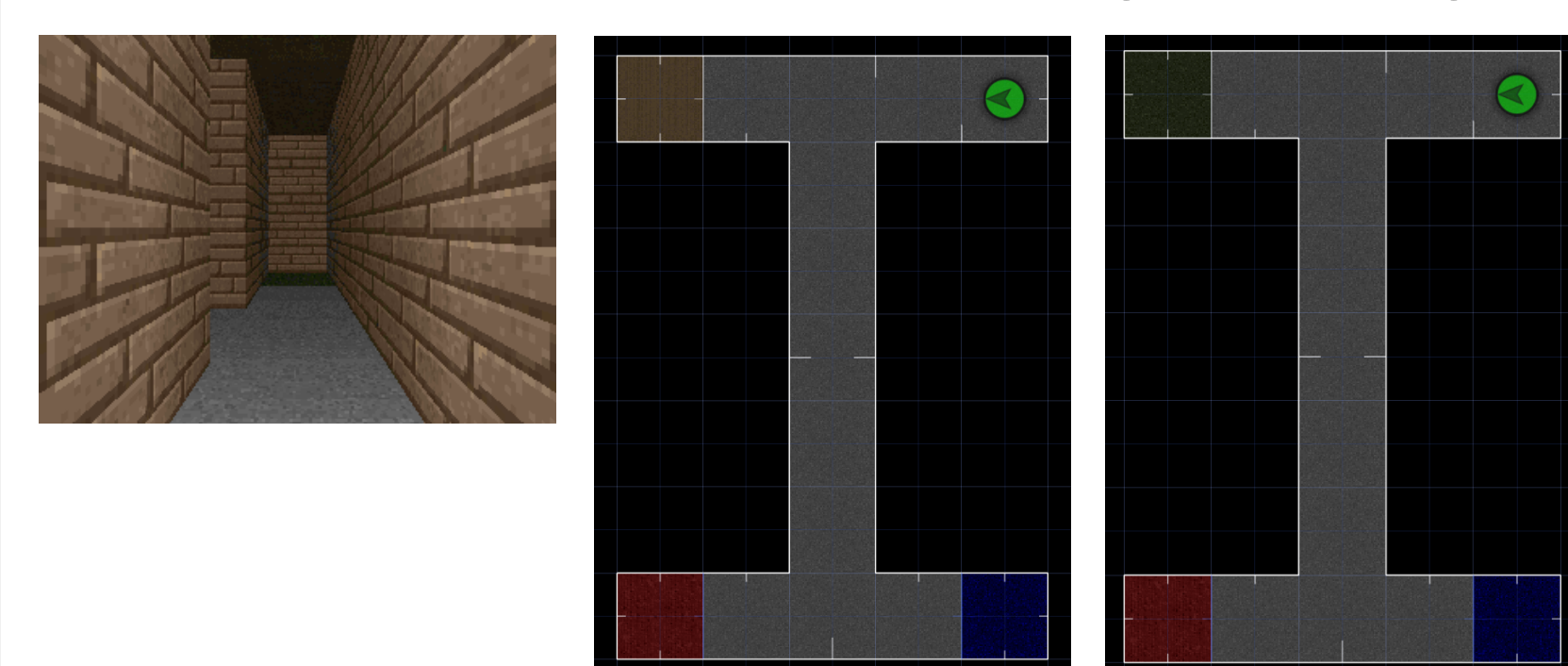


- $\ell_1$ -norm is particularly transferable, even across training algorithms

## Dormant Adversary

Task: Navigate I-maze [4]

in VizDoom [5] yellow marker: go to red goal green marker: go to blue goal



dormant adversarial examples computed through dual-ascent ( $k = 7$ )

