Normalized Core Language

suhorng

November 22, 2014

1 Introduction

2 Syntax

$$
\begin{array}{rcl}
v & ::= & () \\
& | & n \in \mathbb{N} \\
& | & b \in \mathbb{B} \\
& | & x
\end{array}
\qquad
\begin{array}{rcl}
f & ::= & \lambda x.e \\
& | & v\ v \\
& | & \mathit{ref}\ v \\
& | & !v \\
& | & v := v
\end{array}
\qquad
\begin{array}{rcl}
e & ::= & v \\
& | & \textbf{let}\ x = f\ \textbf{in}\ e \\
& | & \textbf{if}\ v\ \textbf{then}\ e_1\ \textbf{else}\ e_2
\end{array}
$$

3 Transforming to NCL

4 An Abstract Machine

4.1 computation

Let $\kappa' = \langle \textbf{frame}\ \Gamma, y, e', \kappa \rangle$.

- $\langle \Gamma, \sigma, (\lambda x.e), y, e', \kappa \rangle \longmapsto \langle \sigma, \gamma(\Gamma, \sigma, \lambda x.e), \kappa' \rangle$
- $\langle \Gamma, \sigma, (v_1\ v_2), y, e', \kappa \rangle \longmapsto \langle \Gamma'', \sigma', e'', \kappa' \rangle$
  - $\langle \textbf{cl}\ \Gamma', x', e'' \rangle = \gamma(\Gamma, \sigma, x)$
  - $l \notin \mathrm{dom}(\sigma)$
  - $\Gamma'' = \Gamma'[x' := l]$
  - $\sigma' = \sigma[l := \gamma(\Gamma, \sigma, v)]$
- $\langle \Gamma, \sigma, (\texttt{ref}\ v), y, e', \kappa \rangle \longmapsto \langle \sigma', \langle \textbf{ref}\ l \rangle, \kappa' \rangle$
  - $l \notin \mathrm{dom}(\sigma)$
  - $\sigma' = \sigma[l := \gamma(\Gamma, \sigma, v)]$
- $\langle \Gamma, \sigma, (!v), y, e', \kappa \rangle \longmapsto \langle \sigma, \sigma(l), \kappa' \rangle$
  - $\langle \textbf{ref}\ l \rangle = \gamma(\Gamma, \sigma, v_1)$ and $l \in \mathrm{dom}(\sigma)$
- $\langle \Gamma, \sigma, (v_1\ \texttt{:=}\ v_2), y, e', \kappa \rangle \longmapsto \langle \sigma', \langle \textbf{unit} \rangle, \kappa' \rangle$
  - $\langle \textbf{ref}\ l \rangle = \gamma(\Gamma, \sigma, v_1)$ and $l \in \mathrm{dom}(\sigma)$
  - $\sigma' = \sigma[l := \gamma(\Gamma, \sigma, v_2)]$

4.2 expressions

- $\langle \Gamma, \sigma, v, \kappa \rangle \longmapsto \langle \sigma, \gamma(\Gamma, \sigma, v), \kappa \rangle$
- $\langle \Gamma, \sigma, (\texttt{let}\ x = f\ \texttt{in}\ e), \kappa \rangle \longmapsto \langle \Gamma, \sigma, f, x, e, \kappa \rangle$
- $\langle \Gamma, \sigma, (\texttt{if}\ v\ \texttt{then}\ e_1\ \texttt{else}\ e_2), \kappa \rangle \longmapsto \langle \Gamma, \sigma, e, \kappa \rangle$
  - $e = \begin{cases} e_1, & \text{if } \gamma(\Gamma, \sigma, v) = \langle \textbf{bool}\ \mathit{true} \rangle \\ e_2, & \text{if } \gamma(\Gamma, \sigma, v) = \langle \textbf{bool}\ \mathit{false} \rangle \end{cases}$

4.3 values

- $\langle \sigma, v, \langle \textbf{frame}\ \Gamma, x, e, \kappa \rangle \rangle \longmapsto \langle \Gamma', \sigma', e, \kappa \rangle$
  - $l \notin \mathrm{dom}(\sigma)$
  - $\Gamma' = \Gamma[x := l]$
  - $\sigma' = \sigma[l := v]$

The function $\gamma(\Gamma, \sigma, v)$ is defined by

- $\gamma(\Gamma, \sigma, ()) = \langle \textbf{unit} \rangle$
- $\gamma(\Gamma, \sigma, n) = \langle \textbf{int}\ n \rangle$
- $\gamma(\Gamma, \sigma, b) = \langle \textbf{bool}\ b \rangle$
- $\gamma(\Gamma, \sigma, x) = \sigma(\Gamma(x))$
- $\gamma(\Gamma, \sigma, \lambda x.e) = \langle \textbf{cl}\ \Gamma, x, e \rangle$